

# Recent Precision Measurements of the Proton Structure at HERA

ICNFP 2013

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on behalf of the  and  collaborations

- Introduction
- HERA structure function data
- HERAFitter project
- Summary

# Introduction: Proton Structure

The proton is made up of point like constituents (partons)

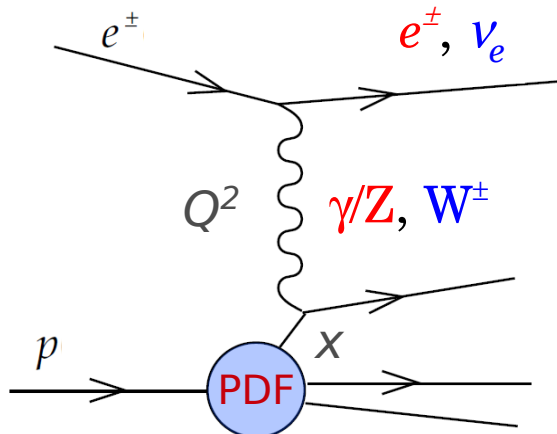
→ probability for a parton to carry a fraction  $x$  of proton momentum:

**Parton Distribution Functions (PDFs)**

**QCD factorisation:** hadronic cross section is a convolution of the PDFs and perturbatively calculable hard-scattering coefficients:

$$\sigma \approx \hat{\sigma} \otimes \text{PDF}$$

Deep Inelastic Scattering (DIS):  
unique opportunity to study the  
structure of the proton



**Neutral Current (NC):**  $ep \rightarrow eX$   
**Charged Current (CC):**  $ep \rightarrow \nu X$

**Kinematics:**

$Q^2$  - virtuality of exchanged boson

$x$  - Bjorken scaling variable

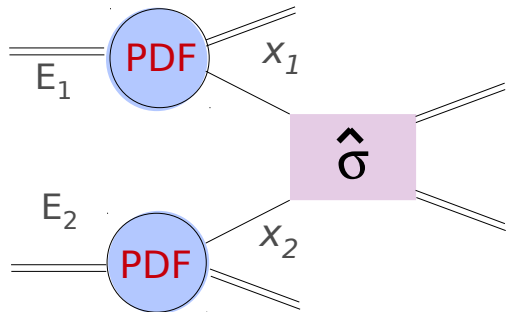
$y$  - inelasticity

$Q^2 = sxy$  ( $\sqrt{s}$  centre-of-mass energy)

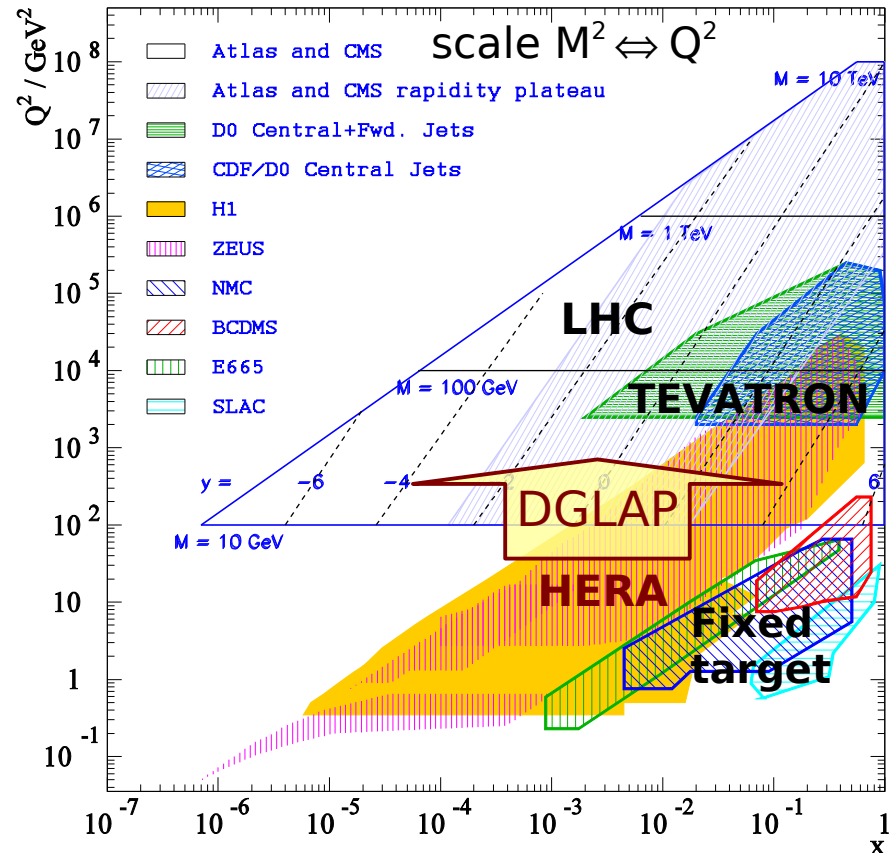
# Introduction: Proton Structure

PDFs are intrinsic property of nucleon, i.e. assumed to be process independent

→ same PDFs can be used to predict  $pp$  collisions



HERA covers the  $x$  range of the LHC  
evolution in  $Q^2$  via DGLAP



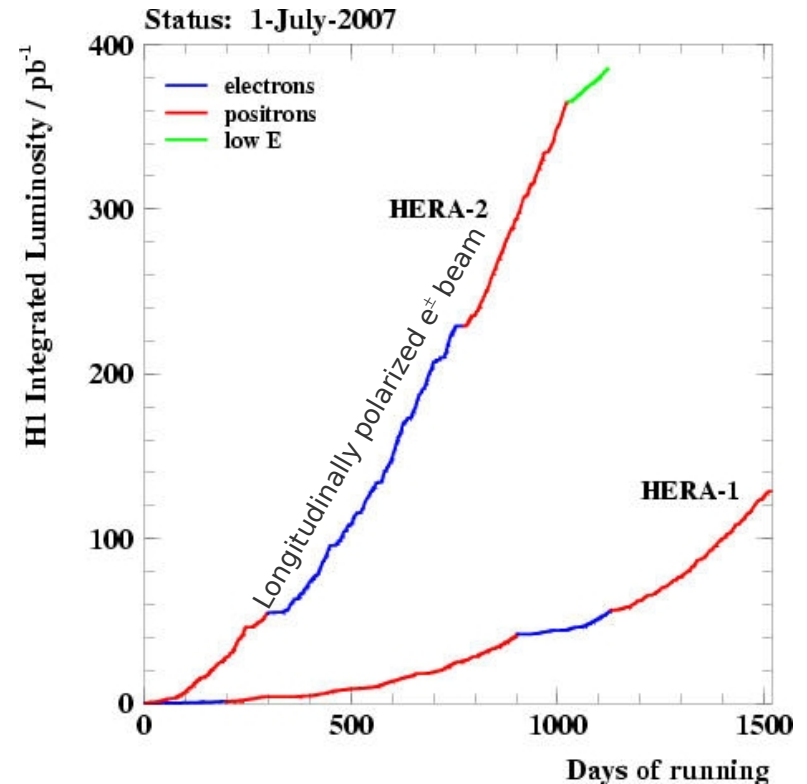
# HERA Collider

HERA was the worlds only  $e^{\pm}p$  collider



- $e^{\pm}(27.5 \text{ GeV}), p(460-920 \text{ GeV})$   
 $\sqrt{s} = 225-318 \text{ GeV}$

- Two collider experiments: **H1** and **ZEUS**
- $\sim 0.5 \text{ fb}^{-1}$  of luminosity recorded by each experiment

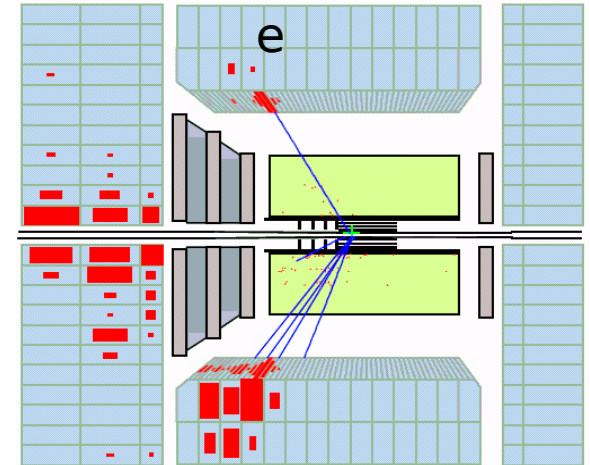
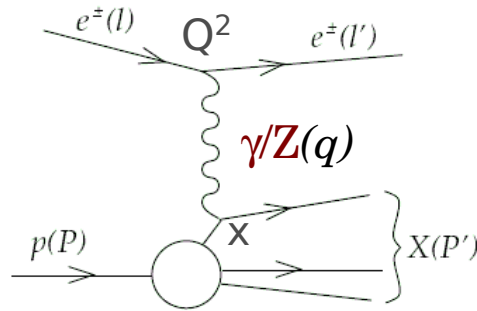


1994-2000: HERA I data  
2003-2007: HERA II data  
with longitudinal  $e^{\pm}$  polarisation:

$$P = \frac{N_R - N_L}{N_R + N_L}$$

# Neutral Current DIS Cross section

Neutral current DIS cross section:



$$\frac{d^2\sigma_{NC}^{e^\pm p}}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left[ Y_+ \tilde{F}_2^\pm \mp Y_- x \tilde{F}_3^\pm - y^2 \tilde{F}_L^\pm \right]$$

dominant contribution  $\uparrow$   
 important at high  $Q^2$   $\uparrow$   
 sizable at high  $y$   $\uparrow$

$$Y_\pm = 1 \pm (1 - y)^2$$

$$k = \frac{1}{4 \sin^2 \theta_w \cos^2 \theta_w} \frac{Q^2}{Q^2 + M_Z^2}$$

LO:  $F_2 \approx x \sum e_q^2 (q + \bar{q})$  (in NLO ( $\alpha_s g$ ) appear)

$$xF_3 \approx x \sum 2e_q a_q (q - \bar{q})$$

PDFs

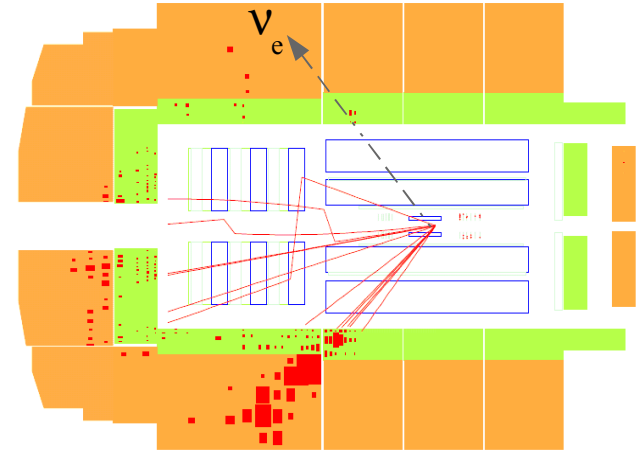
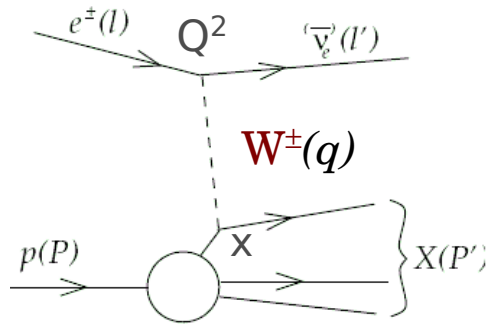
polarisation dependence  
 due to  $\gamma Z$  interference and  
 Z terms



$$\begin{aligned} \tilde{F}_2^\pm &= F_2 + k(-v_e \mp P_e a_e) F_2^{\gamma Z} + k^2(v_e^2 + a_e^2 \pm 2P_e v_e a_e) F_2^Z \\ x\tilde{F}_3^\pm &= k(-a_e \mp P_e v_e) xF_3^{\gamma Z} + k^2(2v_e a_e \pm P_e(v_e^2 + a_e^2)) xF_3^Z \end{aligned}$$

# Charged Current DIS Cross section

Charged current DIS cross section:



$$\frac{d^2\sigma_{CC}^{e^\pm p}}{dx dQ^2} = (1 \pm P_e) \frac{G_F^2}{2\pi x} \left( \frac{M_W^2}{Q^2 + M_W^2} \right)^2 \tilde{\sigma}_{CC}^{e^\pm p}$$

→ linear polarisation dependence

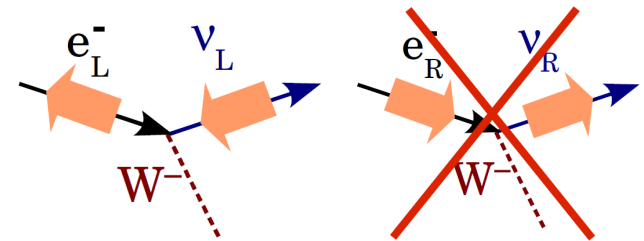
In SM weak interaction acts only on left-handed particles (right-handed anti-particles)

at LO  $e^+/e^-$  sensitive to different quark densities:

$$\tilde{\sigma}_{CC}^{e^+p} = x[\bar{u} + \bar{c}] + (1-y)^2 x[d + s]$$

$$\tilde{\sigma}_{CC}^{e^-p} = x[u + c] + (1-y)^2 x[\bar{d} + \bar{s}]$$

PDFs



# HERA Structure Function Data



Inclusive HERA I and II data

with typical precision:

NC:  $\sim 1.5\%$

CC:  $\sim 4\%$

neutral ( $\gamma/Z$ )

charged ( $W^\pm$ )

currents cross sections

at  $Q^2 \gtrsim M_{Z/W}^2$  scale

are similar:

EW unification

good agreement with  
the SM (HERAPDF 1.5)

arXiv:1208:6138

NEW

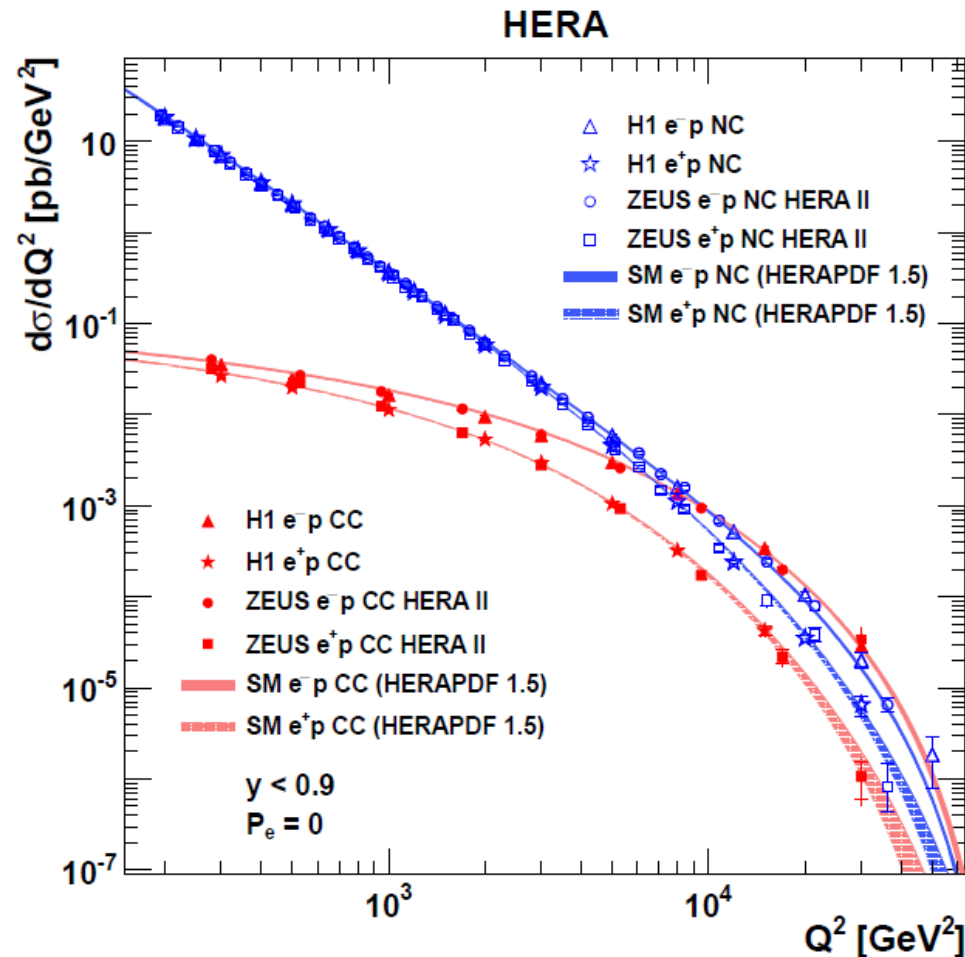
EPJC 70 (2010) 945

EPJC 62 (2009) 625

EPJC 61 (2009) 223

JHEP 1209:061 (2012)

NEW



# High $Q^2$ NC Cross Sections



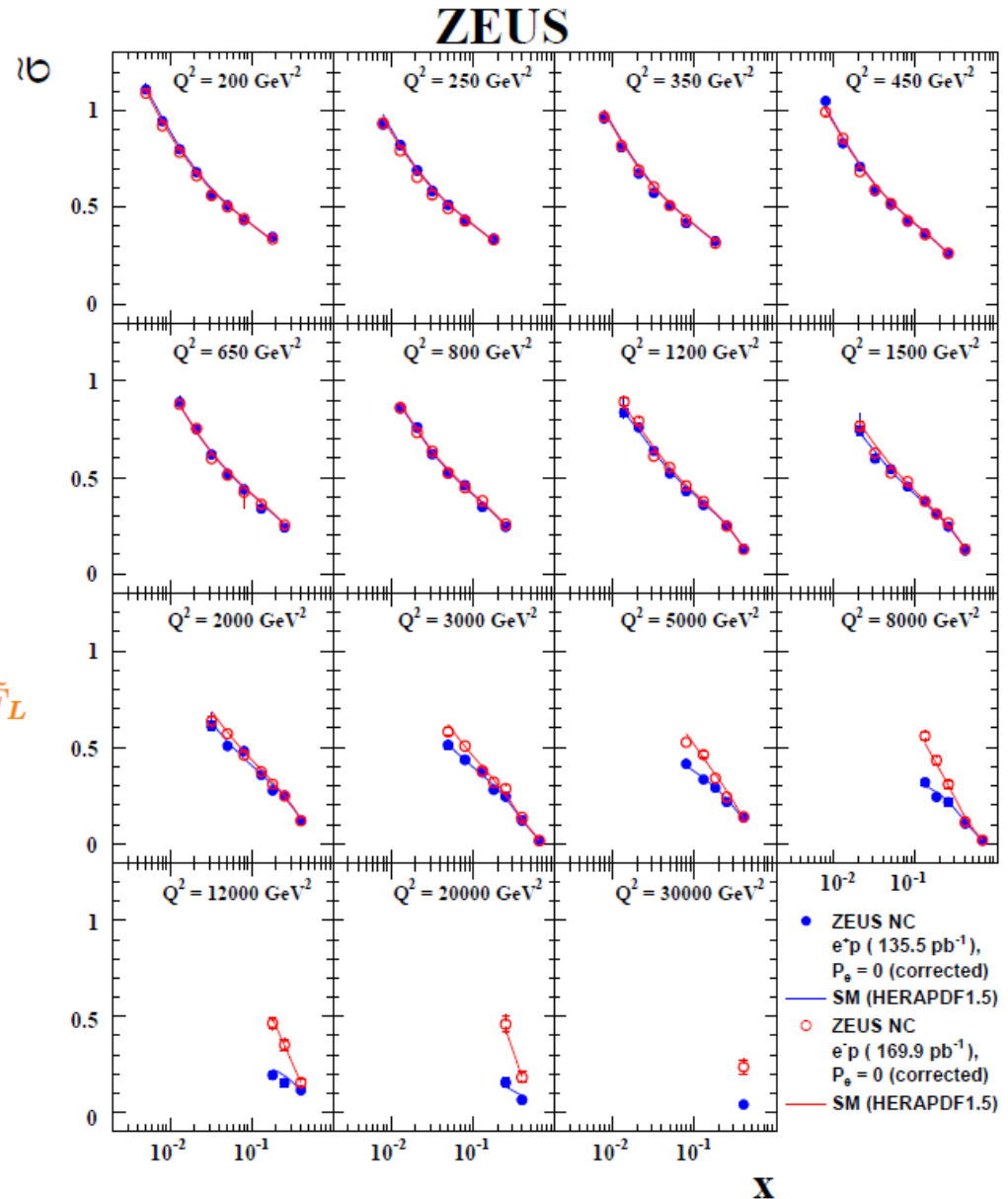
ZEUS: high  $Q^2$  NC HERA II data

→ good agreement with the SM (HERAPDF1.5)

At high  $Q^2$  difference between  $e^-$  and  $e^+$ :  $x\tilde{F}_3$  (sensitive to valence PDFs)

$$\tilde{\sigma}^\pm = \frac{d^2\sigma_{NC}^{e^\pm p}}{dx dQ^2} \frac{xQ^4}{2\pi\alpha^2} \frac{1}{Y_\pm} = \tilde{F}_2 \mp \frac{Y_-}{Y_+} x\tilde{F}_3 - \frac{y^2}{Y_+} \tilde{F}_L$$

$$x\tilde{F}_3 = \frac{Y_+}{2Y_-} [\tilde{\sigma}^- - \tilde{\sigma}^+]$$





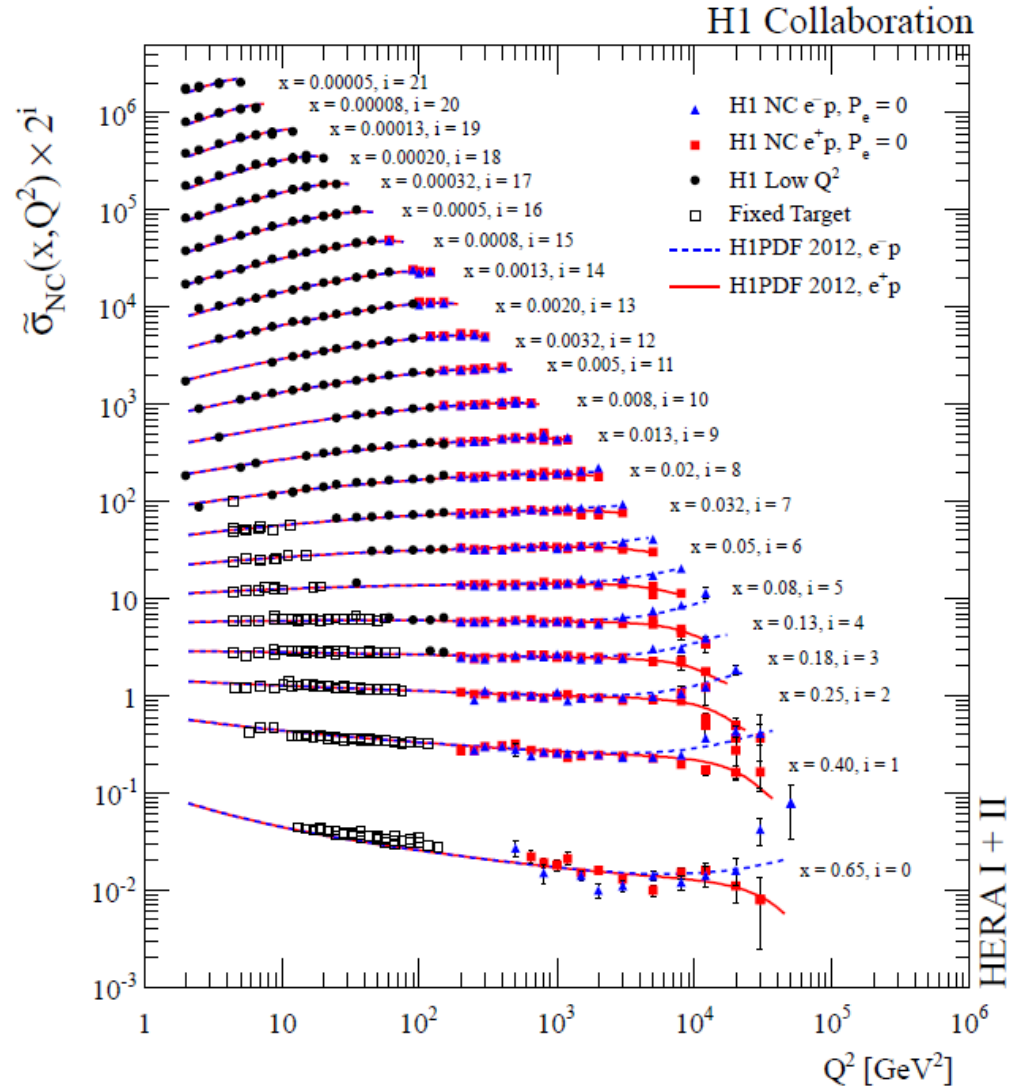
# High $Q^2$ NC Cross Sections



H1: combination of high  $Q^2$  HERA I and HERA II data

H1 precision 1.5% for  $Q^2 < 500 \text{ GeV}^2$

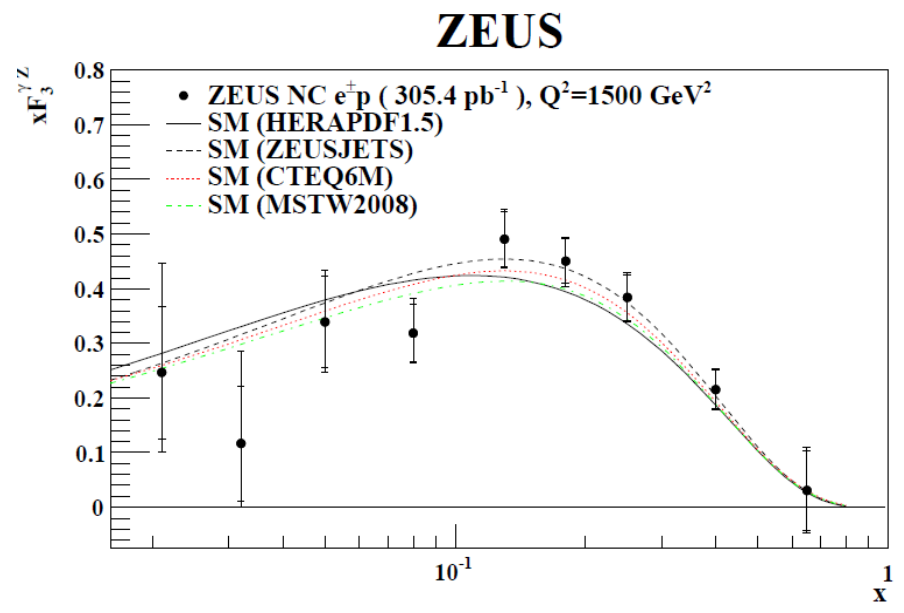
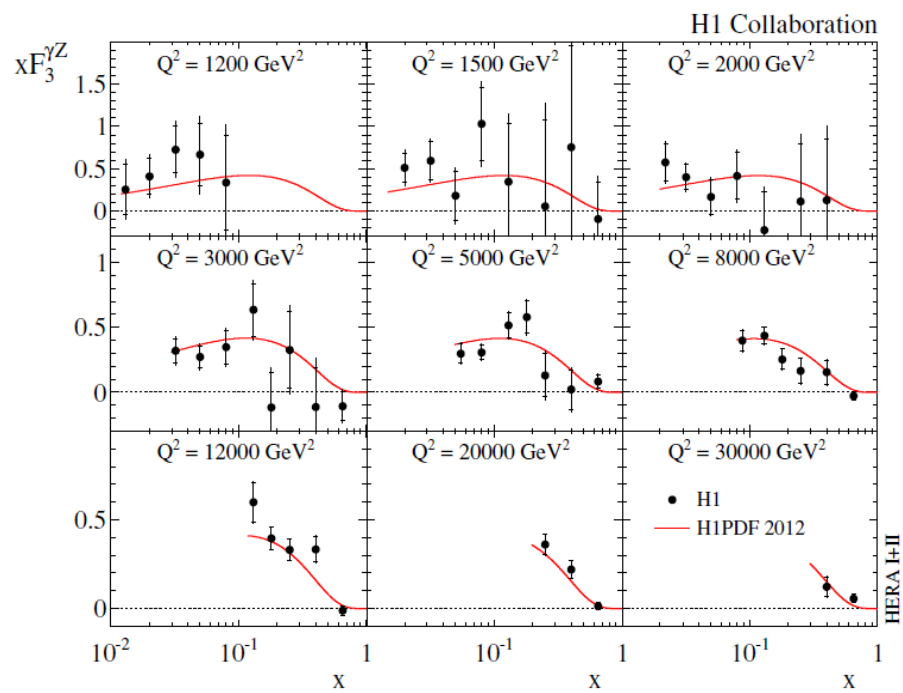
→ factor 2 reduction in error vs HERA I



## Structure function $x\tilde{F}_3$

$$x\tilde{F}_3 = \frac{Y_+}{2Y_-} [\tilde{\sigma}^- - \tilde{\sigma}^+]$$

dominant contribution from  $x\tilde{F}_3^{\gamma Z}$   $x\tilde{F}_3^{\gamma Z} \simeq x\tilde{F}_3 \frac{(Q^2 + M_Z^2)}{\alpha^2 \kappa Q^2}$



$$xF_3^{\gamma Z} \sim xq_{val}$$

# High $Q^2$ NC Cross Sections

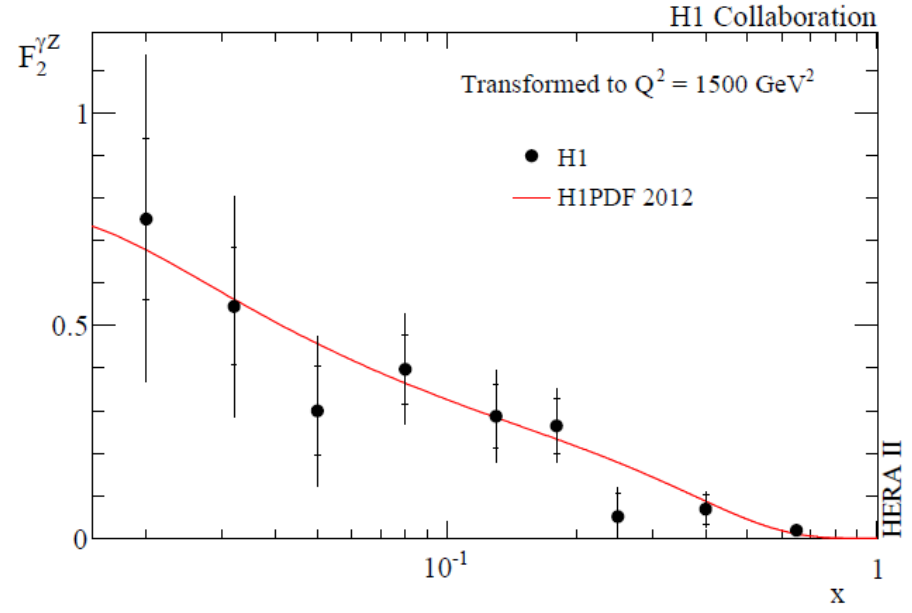


Measuring the difference in NC polarised cross sections  $F_2^{\gamma Z}$  can be accessed:

$$\frac{\sigma^\pm(P_L^\pm) - \sigma^\pm(P_R^\pm)}{P_L^\pm - P_R^\pm} = \frac{\kappa Q^2}{Q^2 + M_Z^2} \left[ \mp a_e F_2^{\gamma Z} + \frac{Y_-}{Y_+} v_e x F_3^{\gamma Z} - \frac{Y_-}{Y_+} \frac{\kappa Q^2}{Q^2 + M_Z^2} (v_e^2 + a_e^2) x F_3^Z \right]$$

$F_2^{\gamma Z}$  measurement is only possible because of  $e^+$  and  $e^-$ , L and R data

First measurement of  $F_2^{\gamma Z}$



$$F_2^{\gamma Z} \sim q + \bar{q}$$

# Polarisation Asymmetry in NC



The charge dependent polarisation asymmetries in neutral currents  
 → direct measure of EW effects

neglecting Z term generalised structure function  $F_2$  is expressed:

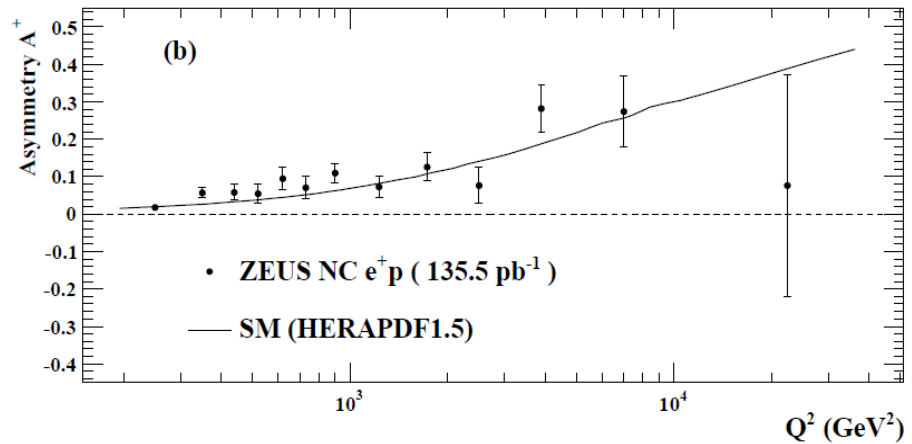
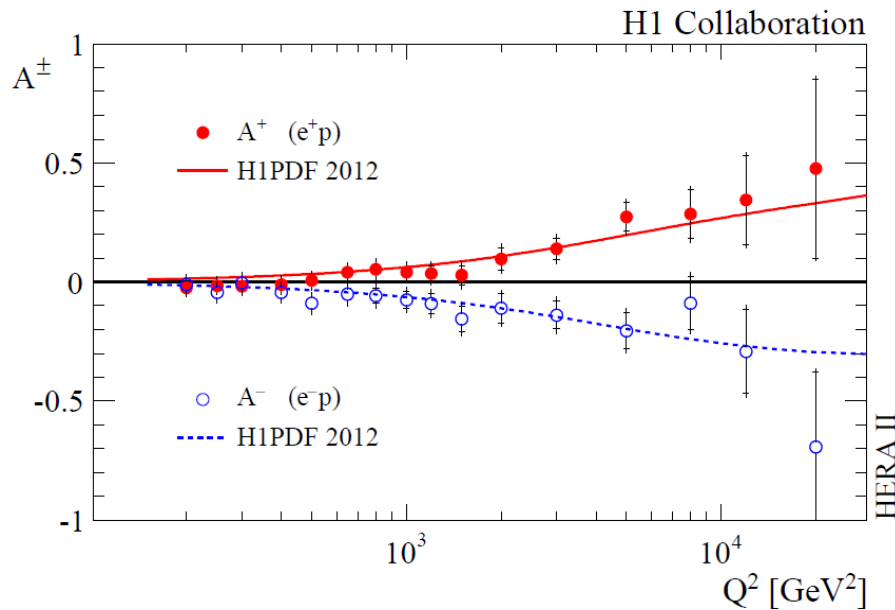
$$\tilde{F}_2^\pm \approx F_2 + k(-v_e \mp P_e a_e) F_2^{\gamma Z}$$

at LO:  $F_2^{\gamma Z} = x \sum 2e_q v_q (q + \bar{q})$

**Polarisation asymmetry  $A$**

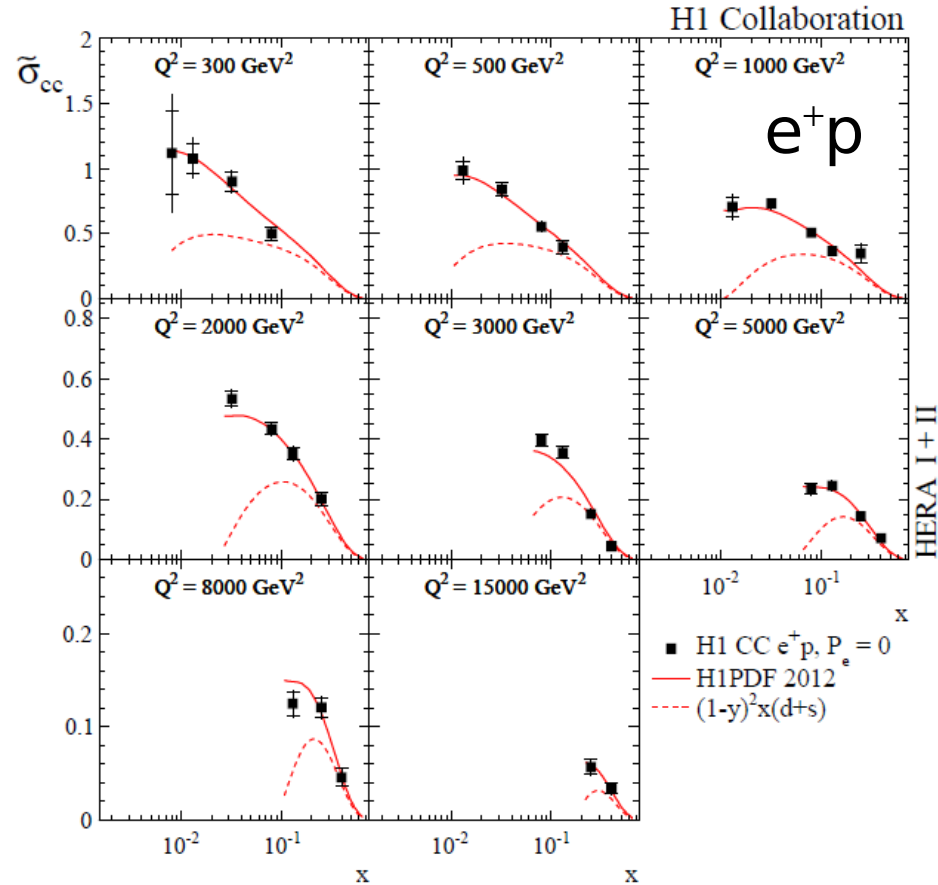
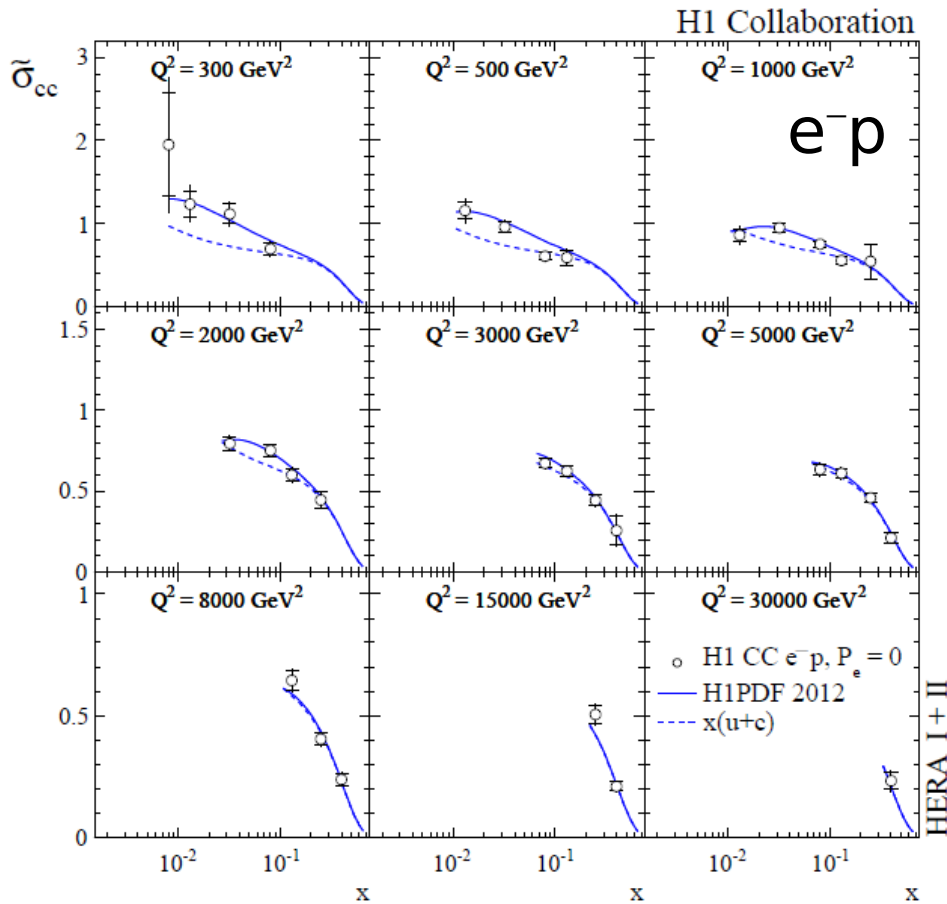
is proportional to a  $v_e v_q$  combination:

$$A^\pm = \frac{2}{P_R - P_L} \frac{\sigma^\pm(P_R) - \sigma^\pm(P_L)}{\sigma^\pm(P_R) + \sigma^\pm(P_L)} \simeq \mp k a_e \frac{F_2^{\gamma Z}}{F_2}$$



→ direct measurement of the parity violation

# Highlights from High $Q^2$ CC Measurement



HERA CC  $e^+/e^-$  measurements:

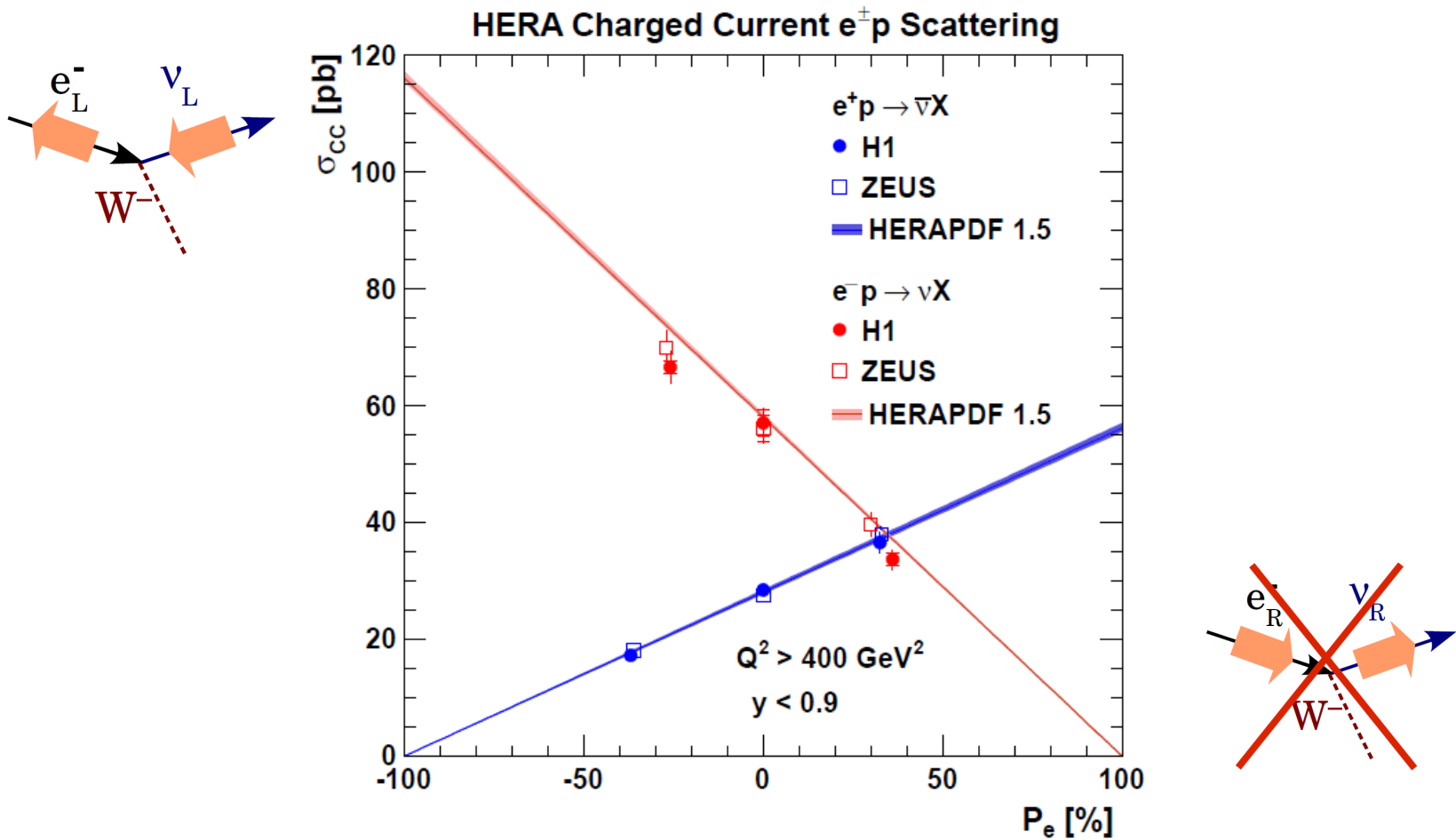
→ sensitivity to quark flavour

→ improvement in precision:  $e^+(e^-)p$  factor of 3(10) luminosity vs HERA I

# High $Q^2$ CC Cross Sections



Final measurement of polarisation dependence of CC cross sections from H1 and ZEUS



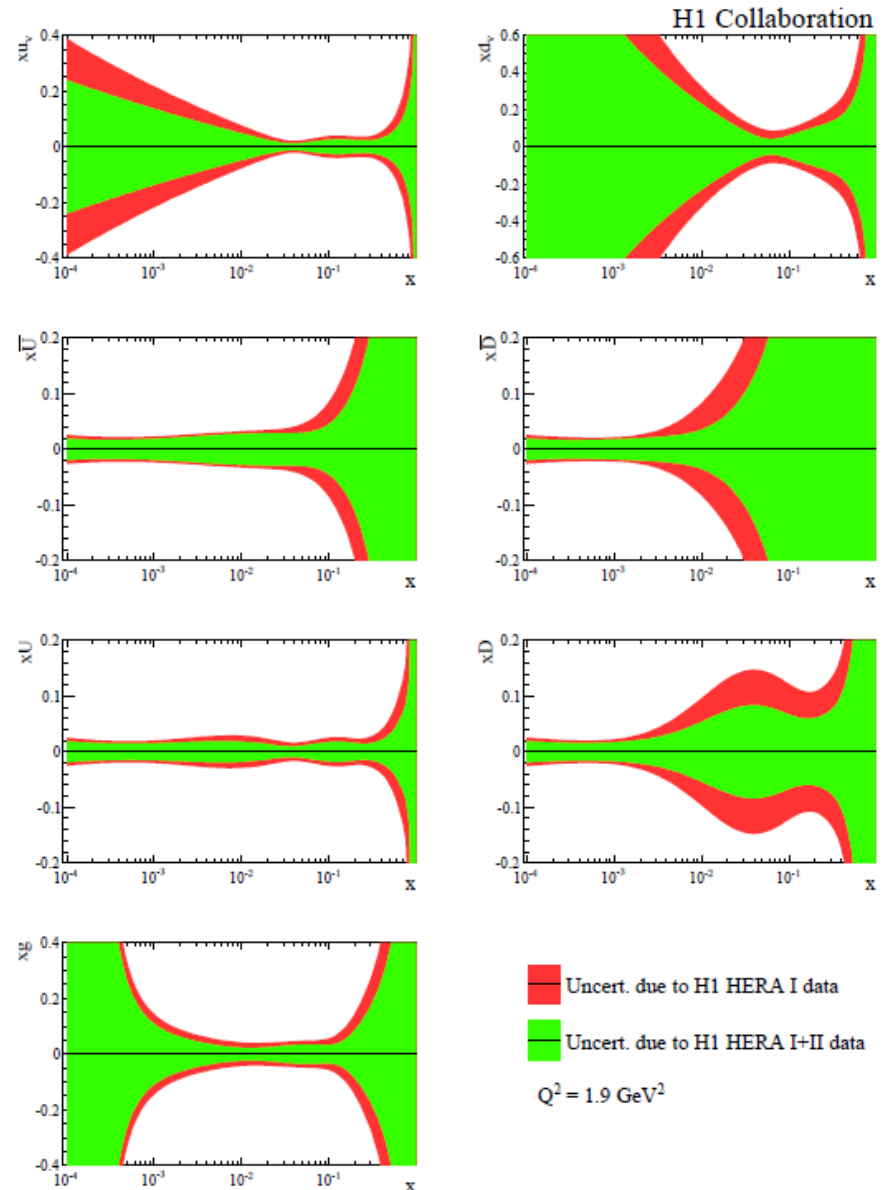
excludes limits on  $M_W^R$  below 214 ( $e^-$ ) and 194 ( $e^+$ ) at 95% CL

Results are consistent with the SM

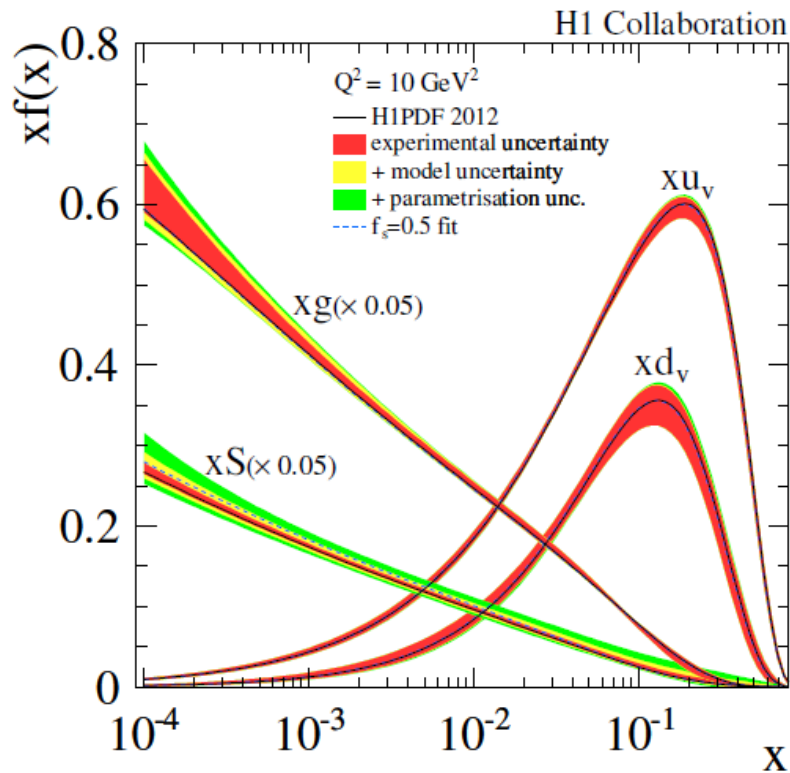
QCD analysis of final H1 NC,CC data

→ performed using HERAFitter

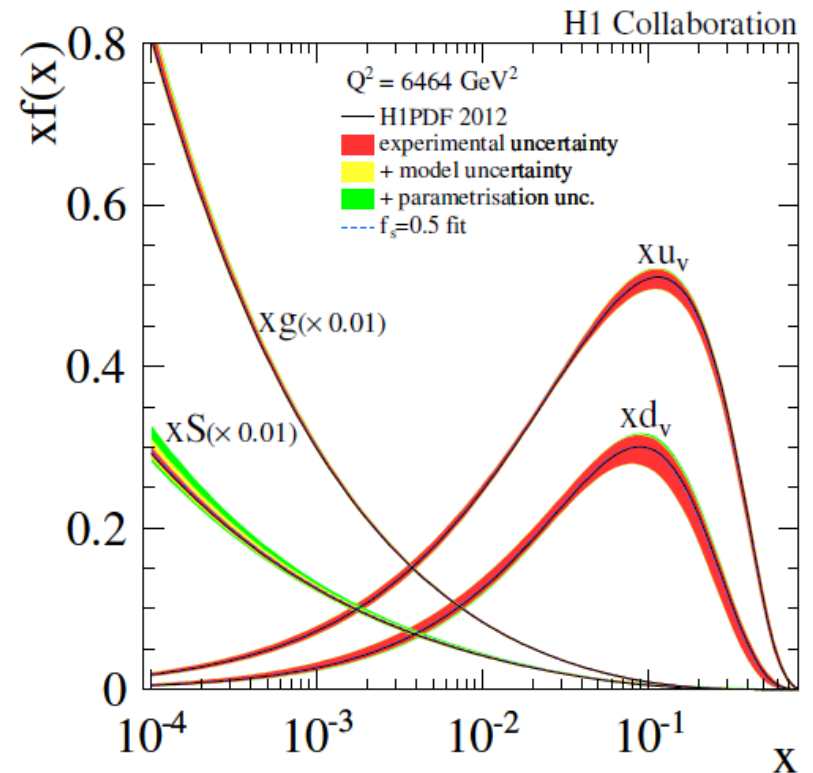
→ improvement in precision for all PDFs in full x range in particular for down-type quarks xD



$$Q^2 = 10 \text{ GeV}^2$$



$$Q^2 = M_W^2$$



Currently combination of final published H1 and ZEUS inclusive data is ongoing → input to **HERAPDF2.0**

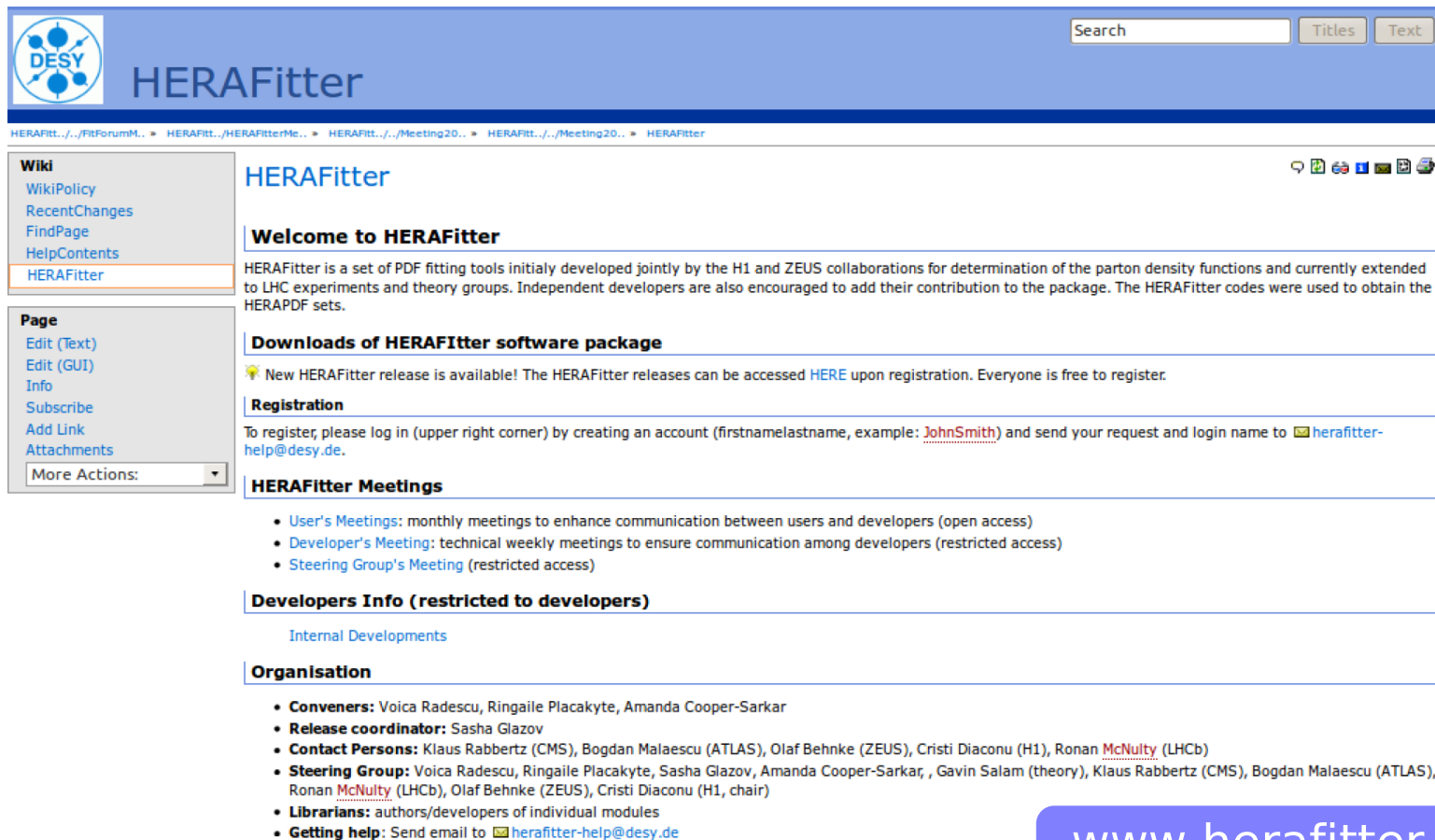


**HERAFitter** project is an open source QCD fit framework ready to extract PDFs and assess the impact of new data

→ open source, everyone is free to download and use it

→ developers: H1 and ZEUS, ATLAS, CMS, LHCb, active support by theory groups

HERAFitter-0.1.0: Sept 2011, HERAFitter-0.2.0: May 2012, **HERAFitter-0.3.1: March 2013**



The screenshot shows the HERAFitter project website. At the top left is the DESY logo and the text 'HERAFitter'. To the right is a search bar with 'Search' and 'Titles Text' buttons. Below the header is a navigation breadcrumb: 'HERAFitter -> HERAFitterMe...> HERAFitterMe...> HERAFitterMe...> HERAFitterMe...> HERAFitter'. On the left is a sidebar with 'Wiki' and 'Page' sections. The main content area has a 'HERAFitter' heading, a 'Welcome to HERAFitter' section, a 'Downloads of HERAFitter software package' section with a new release announcement, a 'Registration' section, a 'HERAFitter Meetings' section with a list of meetings, a 'Developers Info (restricted to developers)' section with 'Internal Developments', and an 'Organisation' section with a list of roles and names.

**Wiki**

- WikiPolicy
- RecentChanges
- FindPage
- HelpContents
- HERAFitter**

**Page**

- Edit (Text)
- Edit (GUI)
- Info
- Subscribe
- Add Link
- Attachments
- More Actions: ▾

**HERAFitter**

**Welcome to HERAFitter**

HERAFitter is a set of PDF fitting tools initially developed jointly by the H1 and ZEUS collaborations for determination of the parton density functions and currently extended to LHC experiments and theory groups. Independent developers are also encouraged to add their contribution to the package. The HERAFitter codes were used to obtain the HERAPDF sets.

**Downloads of HERAFitter software package**

🌟 New HERAFitter release is available! The HERAFitter releases can be accessed [HERE](#) upon registration. Everyone is free to register.

**Registration**

To register, please log in (upper right corner) by creating an account (firstnamelastname, example: [JohnSmith](#)) and send your request and login name to [herafitter-help@desy.de](mailto:herafitter-help@desy.de).

**HERAFitter Meetings**

- **User's Meetings:** monthly meetings to enhance communication between users and developers (open access)
- **Developer's Meeting:** technical weekly meetings to ensure communication among developers (restricted access)
- **Steering Group's Meeting** (restricted access)

**Developers Info (restricted to developers)**

[Internal Developments](#)

**Organisation**

- **Conveners:** Voica Radescu, Ringaile Placakyte, Amanda Cooper-Sarkar
- **Release coordinator:** Sasha Glazov
- **Contact Persons:** Klaus Rabbertz (CMS), Bogdan Malaescu (ATLAS), Olaf Behnke (ZEUS), Cristi Diaconu (H1), Ronan [McNulty](#) (LHCb)
- **Steering Group:** Voica Radescu, Ringaile Placakyte, Sasha Glazov, Amanda Cooper-Sarkar, Gavin Salam (theory), Klaus Rabbertz (CMS), Bogdan Malaescu (ATLAS), Ronan [McNulty](#) (LHCb), Olaf Behnke (ZEUS), Cristi Diaconu (H1, chair)
- **Librarians:** authors/developers of individual modules
- **Getting help:** Send email to [herafitter-help@desy.de](mailto:herafitter-help@desy.de)

## experimental input

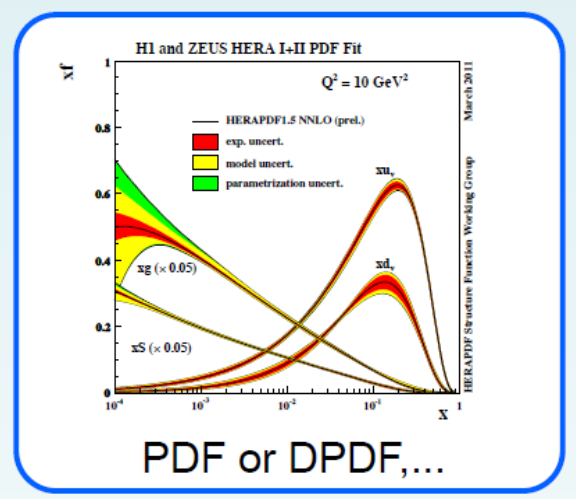
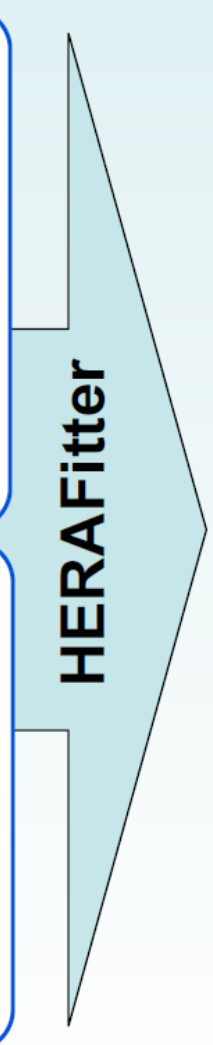
**experiments:**  
HERA, Tevatron, LHC, fixed target

**processes:**  
NC, CC DIS, jets, diffraction, heavy quarks (c,b,t) Drell-Yan, W production

## theoretical calculations/tools

Heavy quark schemes:	MSTW, CTEQ, ABM
Jets, W, Z production:	fastNLO, Applgrid
Top production	NNLO (Hathor)
QCD Evolution	DGLAP (QCDNUM)
	$k_T$ factorisation
Alternative tools	NNPDF reweighting
Other models	Dipole model

- + Different error treatment models
- + Tools for data combination (HERAaverager)



- $\alpha_S(M_Z), m_c, m_b, m_t, f_s, \dots$
- Theory predictions
- Benchmarking
- Comparison of schemes

<https://www.herafitter.org/HERAFitter/HERAFitter/results>



“Determination of the strange quark density of the proton from ATLAS measurements of the  $W \rightarrow l\nu$  and  $Z \rightarrow ll$  cross sections”

[Phys.Rev.Lett. 109 \(2012\) 012001](#)

“Measurement of the inclusive jet cross section in pp collisions at  $\sqrt{s} = 2.76$  TeV and comparison to the inclusive jet cross section at  $\sqrt{s} = 7$  TeV using the ATLAS detector”

[arXiv:1304:4739](#)

“Measurement of the high-mass Drell-Yan differential cross-section in pp collisions at  $\sqrt{s} = 7$  TeV with the ATLAS detector”

[arXiv:1304:4192](#)



In **CMS** several analyses are using HERAFitter for PDF constraints  
→ jets, DY, W+charm data



“Combination and QCD Analysis of Charm Production Cross Section Measurements in Deep Inelastic ep Scattering at HERA”

[Eur. Phys. J. C73 \(2013\) 2311](#)

“Inclusive Deep Inelastic Scattering at High  $Q^2$  with Longitudinally Polarised Lepton Beams at HERA”

[JHEP 1209 \(2012\) 061](#)



LHeC impact studies [J.Phys.G39 \(2012\)](#)

**Theory:** updates of ACOT scheme module (with CTEQ group)  
inclusion of photon PDF in QCDNUM (publication is planned)

# Summary



HERA provides unique determinations of the proton structure

- final HERA II neutral and charged current data published
- H1-ZEUS combination and HERAPDF2.0 determination ongoing

[www.h1.desy.de](http://www.h1.desy.de)

[www-zeus.desy.de](http://www-zeus.desy.de)

[www.desy.de/h1zeus/combined\\_results/index.php](http://www.desy.de/h1zeus/combined_results/index.php)



## HERAFitter

multi-functional QCD framework well integrated into the high energy community (both, experimental and theory)

- open to everyone and anyone can contribute
- well integrated in the LHC analyses

[www.herafitter.org](http://www.herafitter.org)

# Back-up slides

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# HERA Structure Function Data

## HERA I inclusive data

→ combination of H1 and ZEUS sets

JHEP 1001:109 (2010)

## HERA II inclusive data

→ combination of preliminary H1 and ZEUS sets

→ new published data



- full HERA II NC and CC data JHEP 1209:061 (2012)

- increase of integrated luminosity by factor of 3(10) for  $e^+(e^-)p$  sets

- significantly improved systematic uncertainties

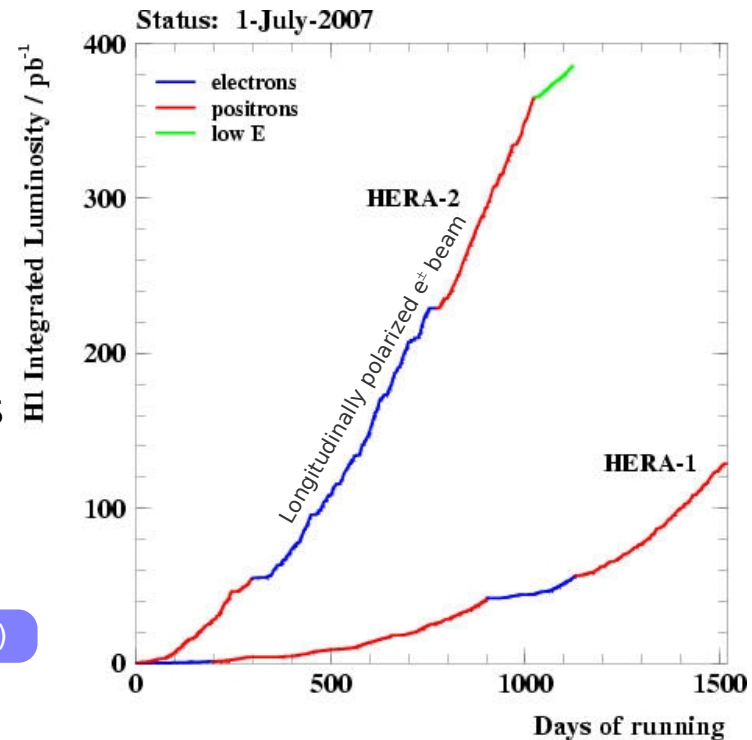
- integrated luminosity determined with elastic QED Compton events

Eur.Phys. J. C72 (2012), 2163



- last  $e^+p$  NC period EPJC 12 08 066

→ currently in process of combination (H1 and ZEUS, HERA I and II)



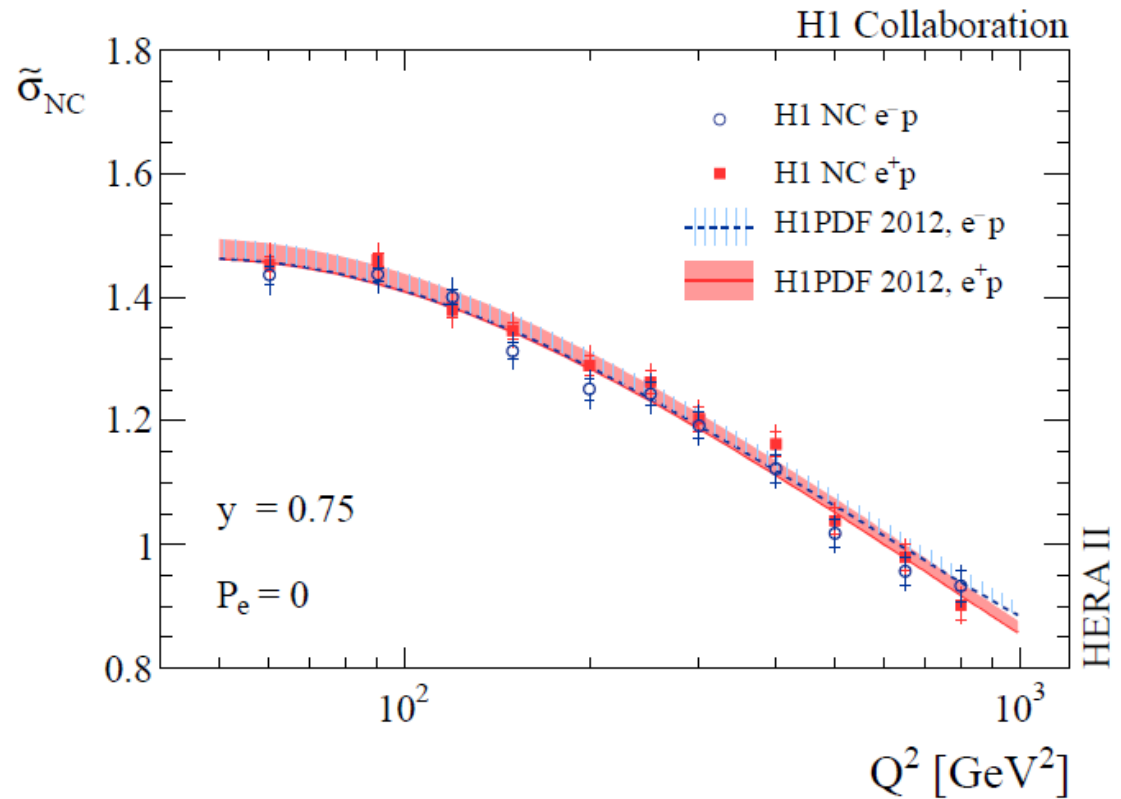
# NC High $y$ Cross Sections



The measurement of neutral current cross sections in high  $y$  region ( $0.63 < y < 0.9$ )

→ sensitive to  $F_L$  structure function measurement

→ good agreement with the SM (H1PDF 2012)



# Deep Inelastic Scattering (DIS)

## Structure function factorisation:

each **structure function** can be written as a convolution of a hard-scattering coefficient **C** and non-perturbative parton distributions:

$$F_2^V(x, Q^2) = \sum_{i=q, \bar{q}, g} \int_x^1 dz \times C_2^{V,i}\left(\frac{x}{z}, Q^2, \mu_F, \mu_R, \alpha_S\right) \times f_i(z, \mu_F, \mu_R)$$

determined using  
measured cross  
section

calculable in  
perturbative QCD

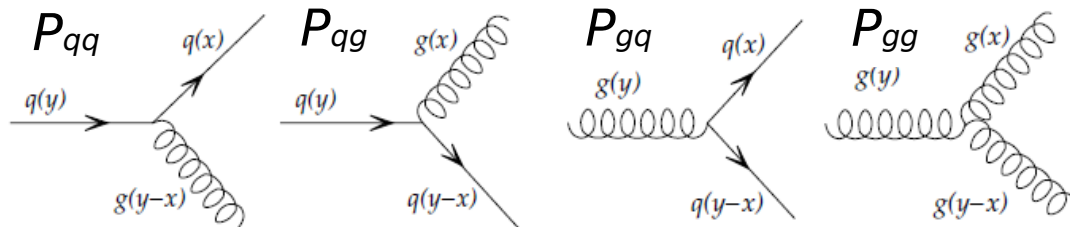
PDFs

PDF scale dependence is calculable in perturbative QCD  
(**DGLAP** evolution):

$$\frac{\partial q(x, Q^2)}{\partial \ln Q^2} \propto \int_x^1 \frac{dz}{z} \left[ q(z, Q^2) P_{qq}\left(\frac{x}{z}\right) + g(z, Q^2) P_{qg}\left(\frac{x}{z}\right) \right]$$

$$\frac{\partial g(x, Q^2)}{\partial \ln Q^2} \propto \int_x^1 \frac{dz}{z} \left[ q(z, Q^2) P_{gq}\left(\frac{x}{z}\right) + g(z, Q^2) P_{gg}\left(\frac{x}{z}\right) \right]$$

Probability via splitting functions:





# PDF Determination

Experimentally measured  $\sigma(x, Q^2) \rightarrow F_2(x, Q^2)$

$Q^2$  dependence of  $F_2$  is given in pQCD (**DGLAP** evolution equations)

$x$ -dependence of PDFs is not calculable in pQCD

- parametrise PDFs at the starting scale  $Q_0^2$
- evolve PDFs using **DGLAP** equations to  $Q^2 > Q_0^2$
- construct structure functions from PDFs and coefficient functions: predictions for every data point in  $(x, Q^2)$  - plane
- $\chi^2$ -fit to the experimental data

# HERAPDF strategy and settings

DGLAP at NLO → QCD predictions

PDFs parametrised (at starting scale  $Q^2_0$ ) using standard parametrisation form:

$$\begin{aligned}xg(x) &= A_g x^{B_g} (1-x)^{C_g}, \\xu_v(x) &= A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} \left(1 + E_{u_v} x^2\right), \\xd_v(x) &= A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}}, \\x\bar{U}(x) &= A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}}, \\x\bar{D}(x) &= A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.\end{aligned}$$

*A*: overall normalisation

*B*: small  $x$  behavior

*C*:  $x \rightarrow 1$  shape

The optimal number of parameters chosen by saturation of the  $\chi^2$

- central fit with:

10 free parameters for HERA I data

13 for HERA I+II data

$xg, xu_v, xd_v, x\bar{U}, x\bar{D}$

where  $x\bar{U}=x\bar{u}$  and  $x\bar{D}=x\bar{d}+x\bar{s}$  at the starting scale ( $x\bar{s}=f_s x\bar{D}$  with  $f_s=0.31$ )

$A_g, A_{u_v}, A_{d_v}$  are fixed by sum rules

extra constrains for small  $x$  behavior of d- and u-type quarks:

$B_{u_v}=B_{d_v}, B_{\bar{U}}=B_{\bar{D}}, A_{\bar{U}}=A_{\bar{D}}(1-f_s)$  for  $\bar{u}=\bar{d}$  as  $x \rightarrow 0$

# HERAFitter: Functionality

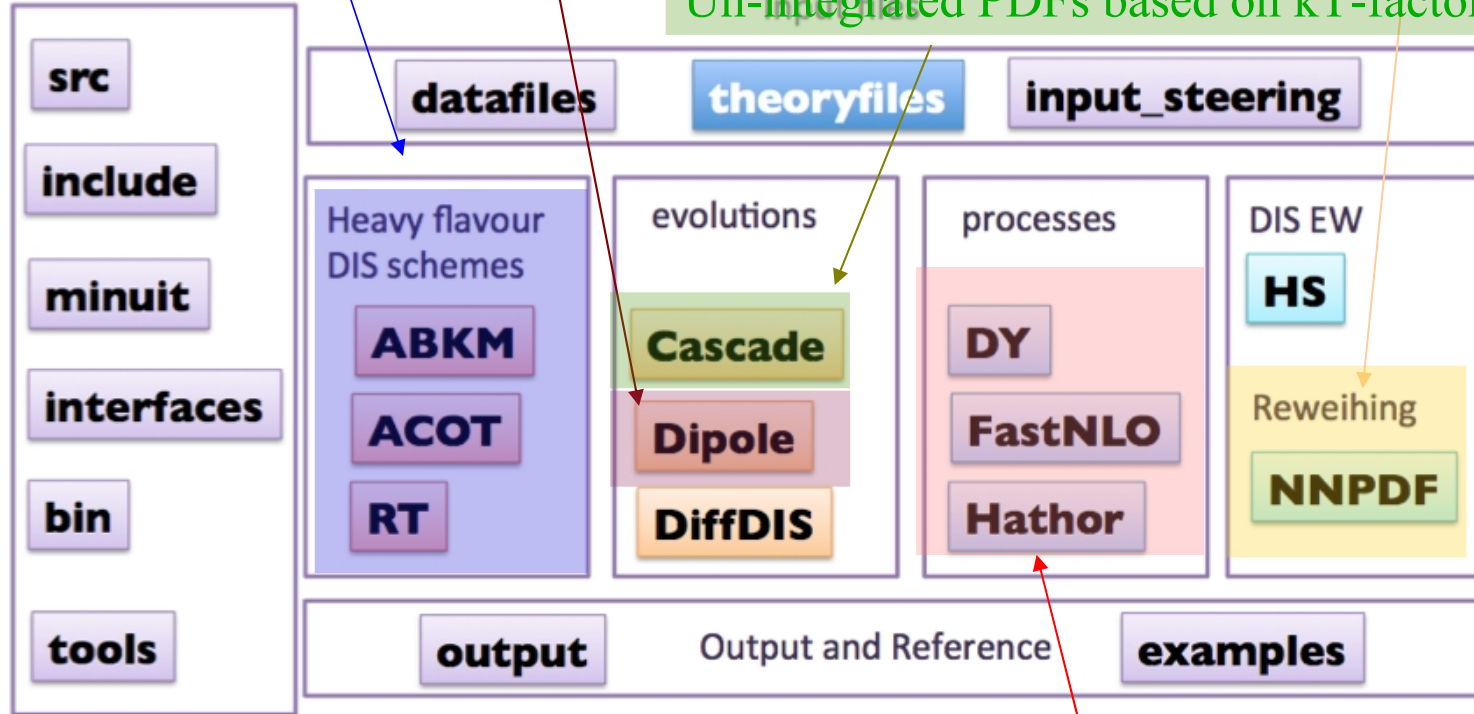
DIS: VFNS (ACOT, RT, ZM) and FFNS

Different dipole models

Regularisation techniques  
(data driven or external)

Un-integrated PDFs based on kT-factorisation

Common modules



Various  $\chi^2$  representations,  
Hessian and MC replica methods,  
various data uncertainty treatments,  
etc...

Interfaces to:  
APPLGRID  
FastNLO  
HATHOR



### Releases of the HERAFitter QCD analysis package

- Versioning convention: **i.j.k** with
  - **i** - stable release
  - **j** - beta release
  - **k** - bug fixes.
- The release notes can be found in this attachment: @HERAFitter\_release\_notes.pdf.

Date	Version	Files	Remarks
06/2013	0.3.1	@herafitter-0.3.1.tgz	fix release includes @manual-0.3.1.pdf and decoupled @theoryfiles.tgz
03/2013	0.3.0	@herafitter-0.3.0.tgz	release includes @manual-0.3.1.pdf and decoupled @theoryfiles.tgz
07/2012	0.2.1	@herafitter-0.2.1.tgz	fix release for 0.2.0
05/2012	0.2.0	@herafitter-0.2.0.tgz	added functionality for LHC users
09/2011	0.1.0	@herafitter-0.1.0.tgz	first release

Releases  
(publicly accessible)

### Documentation

- From 0.3.0 on a manual is provided together with an example directory.
- The **README** file (accessible via the package) gives an explanation for a quick start.

### Web access to SVN

- For users with a valid DESY account, the SVN repository is accessible on the web at <https://svnsrv.desy.de/k5viewvc/h1fitter>.
- For users without DESY account, the SVN repository is accessible on the web at <https://svnsrv.desy.de/basviewvc/h1fitter/> with [herafitter-user@desy.de](mailto:herafitter-user@desy.de) account and PDFfits password.

### Doxygen Documentation

- The doxygen documentation is located [here](#)

Documentation:  
manual,  
release notes,  
README,  
DOXYGEN

### Links to external packages

External packages that could be run with HERAFitter via configuration flags can be accessed for convenience [HERE](#).

External packages

### HERAverager data combination package

Information can be accessed here <https://wiki-zeuthen.desy.de/HERAverager>.

### Subscription

We encourage users to subscribe to mailing list for news and updates related to the HERAFitter webpage. (average rate of e-mails is once a month), please contact [herafitter-help@desy.de](mailto:herafitter-help@desy.de) ( or by creating a user account to this wiki we get a notification)