



Precision tests of QCD at HERA

Nataša Raičević

University of Montenegro

on behalf of the H1 and ZEUS Collaborations

Excited QCD 2013

3-9 February 2013, Bjelašnica Mountain, Sarajevo

HERA and luminosity



HERA (DESY, Hamburg): 1992 - 2007

➤ Total lumi H1, ZEUS: 0.5 fb^{-1} each

HERA-I 1992-2000 $\sim 120 \text{ pb}^{-1}$

HERA-II 2003-2007 $\sim 380 \text{ pb}^{-1}$

$$E_{e^+/e^-} = 27.6 \text{ GeV}$$

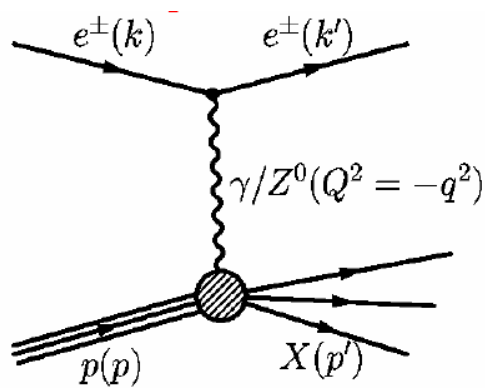
HERA-I ($E_p = 820,920 \text{ GeV}$) upgraded to HERA-II ($E_p = 920 \text{ GeV}$)

Since April 2007 until the end of June

- Low energy run - LER - ($E_p = 460 \text{ GeV}$)
 - Medium energy run - MER - ($E_p = 575 \text{ GeV}$)
- } Measurement of F_L

Inclusive Deep Inelastic Scattering (DIS)

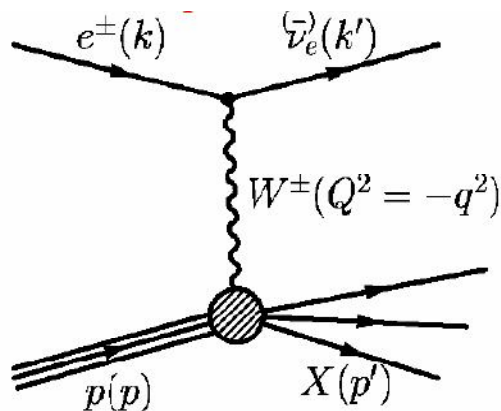
Neutral Current (NC)



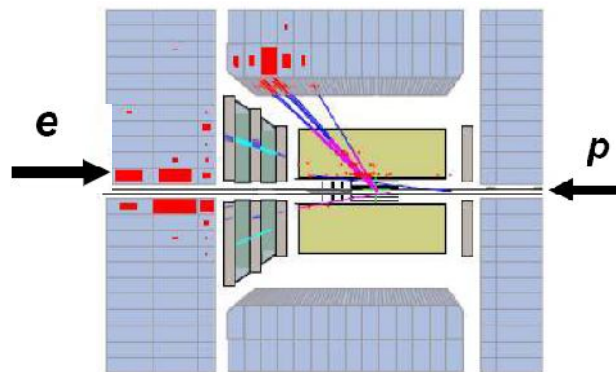
H1 NC event display



Charged Current (CC)



ZEUS CC event display



Virtuality of exchanged boson:

$$Q^2 = -q^2 = -(k - k')^2$$

Fraction of proton momentum carried by struck quark

$$x = \frac{Q^2}{2p \cdot q}$$

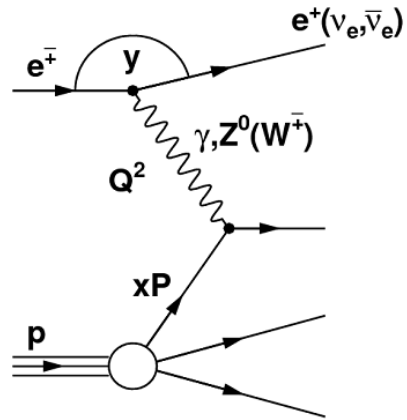
Fraction of energy transferred from incoming lepton at proton rest frame

$$y = \frac{p \cdot q}{p \cdot k}$$

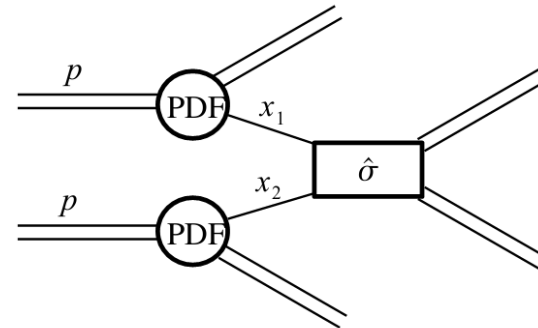
HERA Parton Density Functions (PDFs) and the LHC

HERA:

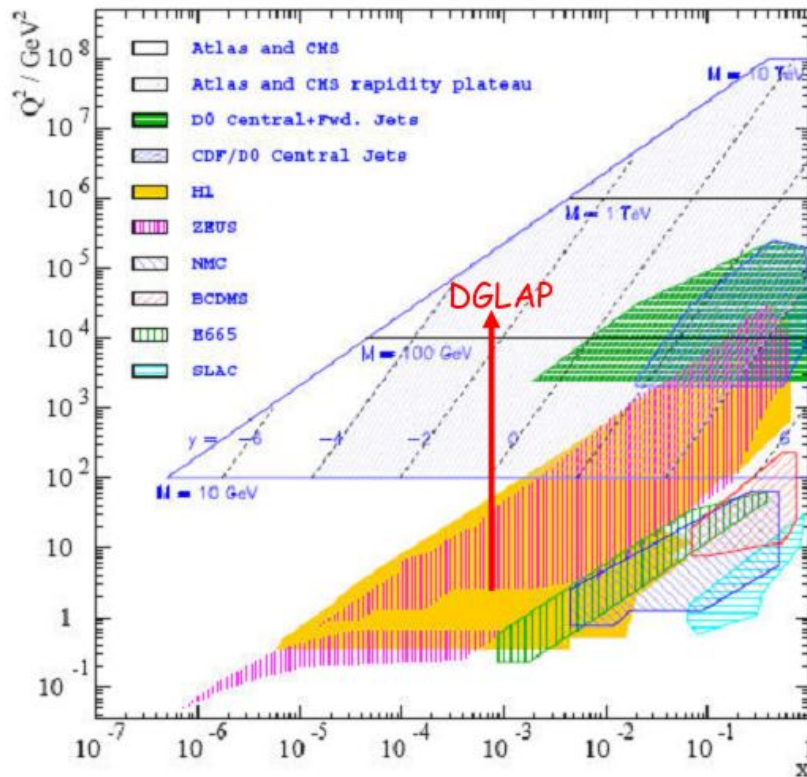
$$\sigma \propto \text{PDF}(x) \times \hat{\sigma}$$



LHC:



$$\sigma \propto \text{PDF}(x_1) \times \text{PDF}(x_2) \times \hat{\sigma}$$



cited QCD 2013

- ❑ Proton structure described by precise PDFs needed for making accurate predictions for any process involving protons.
- ❑ **DGLAP QCD** evolution provides Q^2 dependence of the PDFs, x dependence must come from data. HERA covers the most important region for the LHC.

Precision measurements of QCD at HERA

Neutral current cross section - new results from HERA

$\tilde{\sigma}_{\text{NC}}(x, Q^2)$ - NC reduced cross-section

$$\frac{d^2 \sigma_{\text{NC}}(e^\pm p)}{dx dQ^2} = \frac{2\pi \alpha^2}{x Q^4} y_\pm \left[F_2 - \frac{y_\pm^2}{Y_\pm} F_L \mp \frac{Y_\mp}{Y_\pm} x F_3 \right] \quad y_\pm = 1 \pm (1-y)^2$$

Contribution from valence and sea quarks

Directly related to gluon in pQCD
 $F_L \sim \alpha_s \cdot xg(x, Q^2)$

Contribution from valence quarks at high Q^2

Charged current cross section - new results from HERA

$$\frac{d^2 \sigma_{\text{CC}}^{e^\pm p}}{dx dQ^2} = \frac{G_F^2 M_W^4}{2\pi x (Q^2 + M_W^2)^2} \sigma_{\text{CC}}^\pm$$

$$\sigma_{\text{CC}}^{e^+p} \sim (x\bar{u} + x\bar{c}) + (1-y)^2(xd + xs)$$

$$\sigma_{\text{CC}}^{e^-p} \sim (xu + xc) + (1-y)^2(x\bar{d} + x\bar{s})$$

} Sensitivity to the flavor of the valence distributions at high x

- Direct measure of structure functions (various linear combination of PDFs)
- HERA can disentangle proton PDFs with little assumptions

Precision measurements of QCD at HERA

Charm contribution to the inclusive DIS - new result from HERA

- ~ 30% contribution to the inclusive DIS cross section (sizeable part)

$$\frac{d^2 \sigma_{NC}(e^\pm p)}{dx dQ^2} = \frac{2\pi \alpha^2}{x Q^4} Y_+ [F_2^{cc} - \frac{Y_+^2}{Y_+} F_L^{cc}]$$

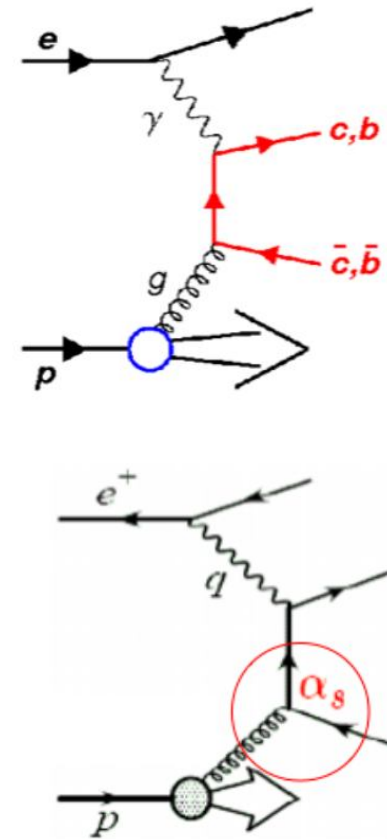
- Measurement of the structure function F_2^{cc} , probing mass effects in the QCD evolution

Jet production in DIS - new measurements from HERA

- Direct sensitivity to α_s and **gluon density**

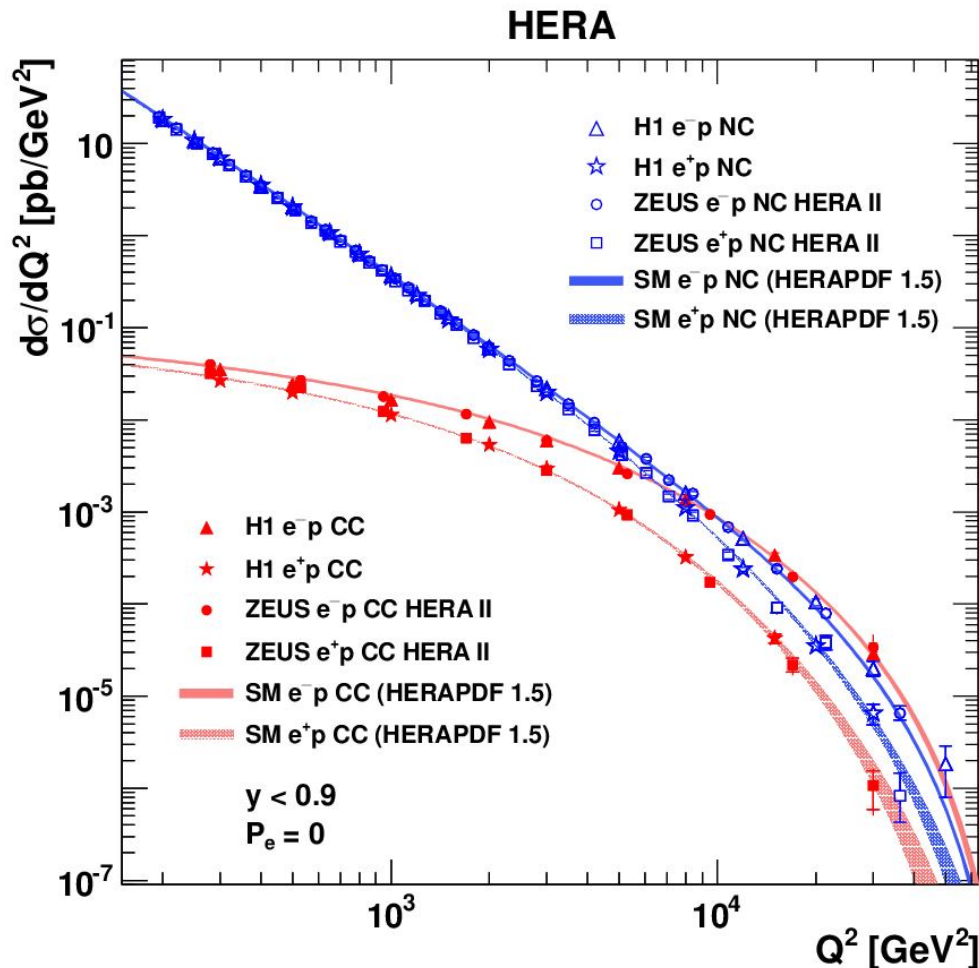
Diffraction - new measurements from HERA

- New inputs for more precise DPDFs (not covered here): EPJ C72 (2012) 2175 and EPJ C72 (2012) 2074



H1 and ZEUS HERA-II NC and CC cross sections at high Q^2

- Last pieces from H1 and ZEUS inclusive measurements (at nominal $E_p = 920 \text{ GeV}$)
- high Q^2 - FINALISED



JHEP 1209 (2012) 061 H1 NC and CC $e^{\pm}p$

arXiv:1208.6138 ZEUS NC $e^{\pm}p$

EPJ C70 (2010) 945 ZEUS CC $e^{\pm}p$

EPJ C62 (2009) 625 ZEUS NC $e^{\pm}p$

EPJ C61 (2009) 223 ZEUS CC $e^{\pm}p$

□ EW unification at the $M_{W,Z}$ scale

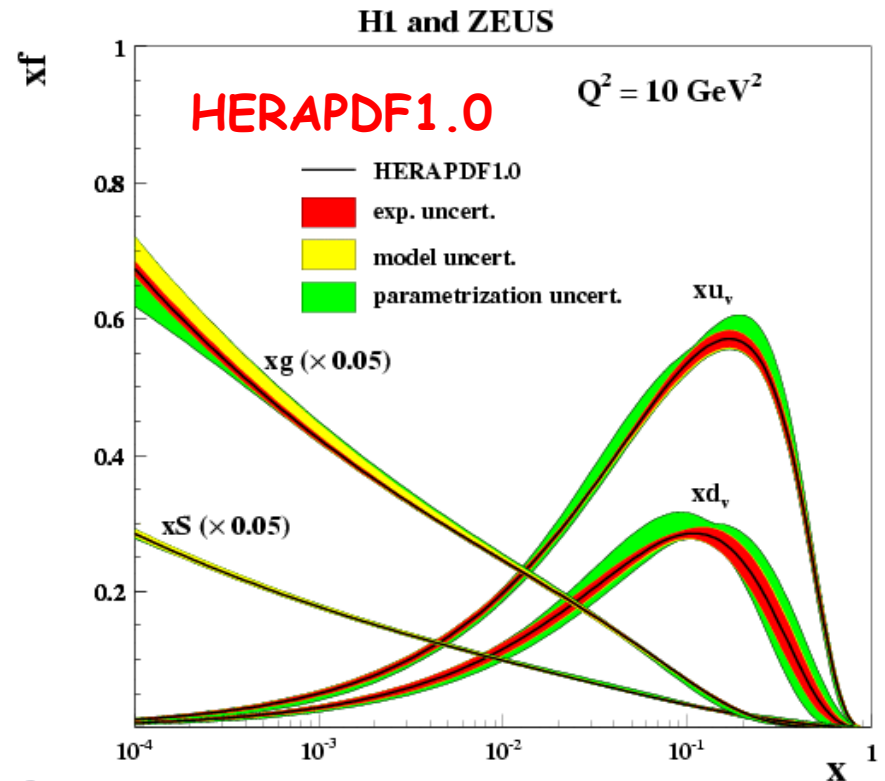
□ SM provides perfect description of data over many orders of magnitude

→ Lepton probe behaves as expected

QCD analysis of HERA data

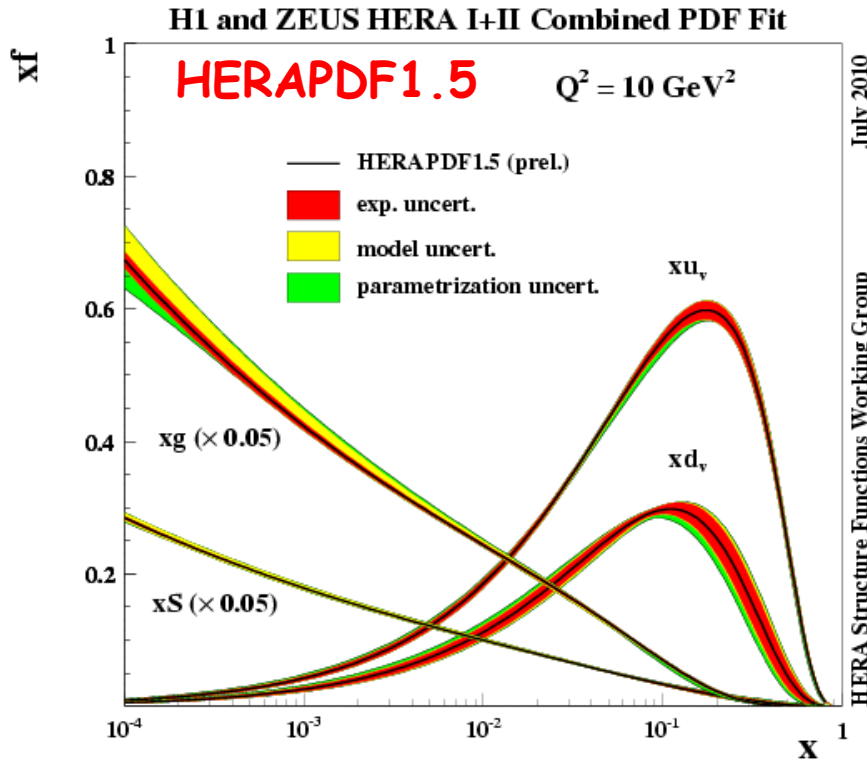
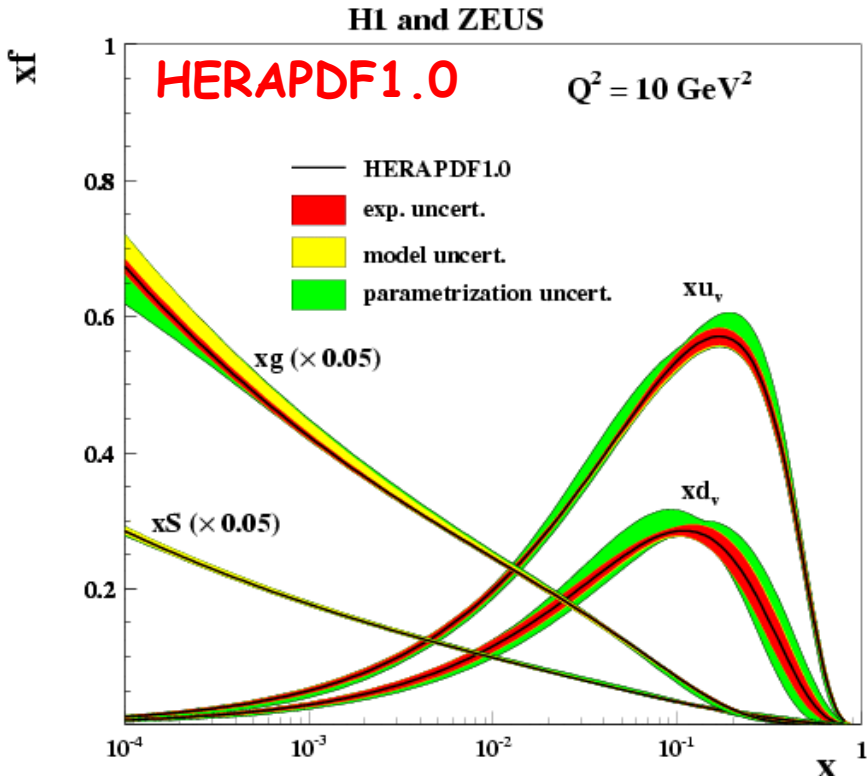
General approach for PDF determination

- ❑ At low starting scale Q_0^2 PDFs parametrised by $Ax^B(1-x)^C(1+Dx+\dots)$
- ❑ Evolve these functions using the **DGLAP equations** to higher Q^2 and calculate x-sections
- ❑ Compare the calculation to experimental data and adjust the free parameters by χ^2 minimisation
- ❑ Heavy flavours treated according to RT-VFNS
- ❑ Fixed strong coupling constant: $\alpha_s = 0.1176$
- ❑ **HERAPDF1.0** obtained from combined HERA-I data from H1 and ZEUS experiments (**JHEP 1001:109(2010)**)
- Latest DGLAP analyses use open source **HERAFitter** 'package' which gives possibility to further improve PDFs by adding measurements from other experiments (Developers: H1, ZEUS, ATLAS and CMS)



Inclusion of preliminary HERA-II high Q^2 data

H1prelim-10-142 and ZEUS-prel-10-018

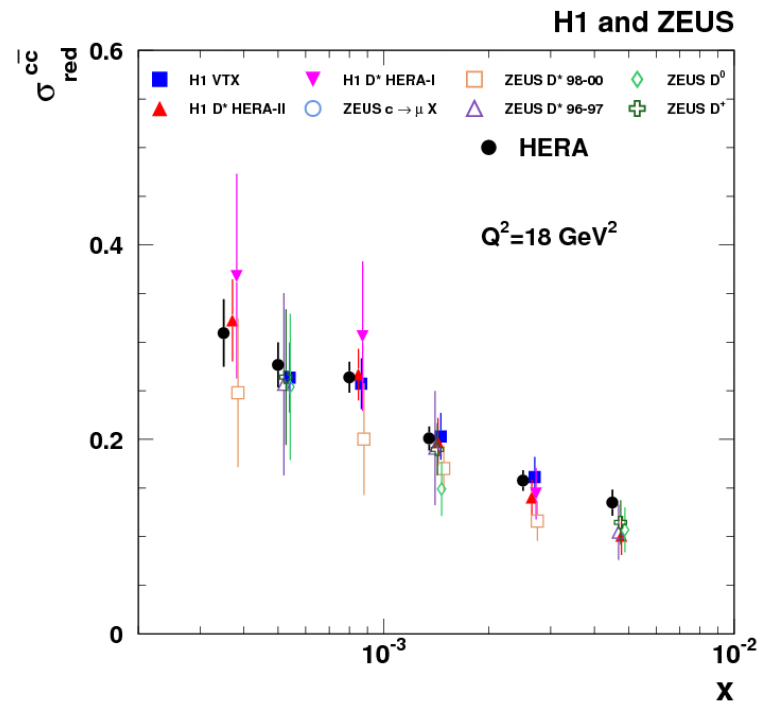
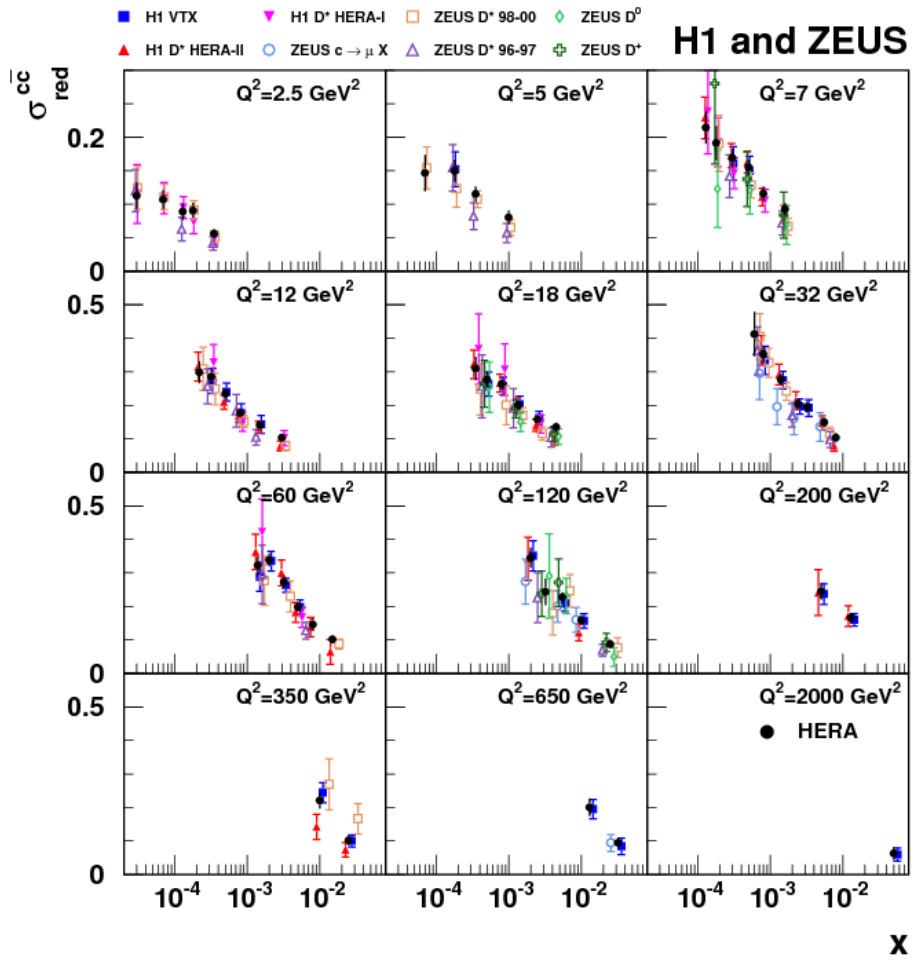


July 2010
HERA Structure Functions Working Group

- Inclusion of the HERA-II high Q^2 data improves uncertainties of PDFs in the high x region especially visible for the valence quark distributions

Inclusion of charm data

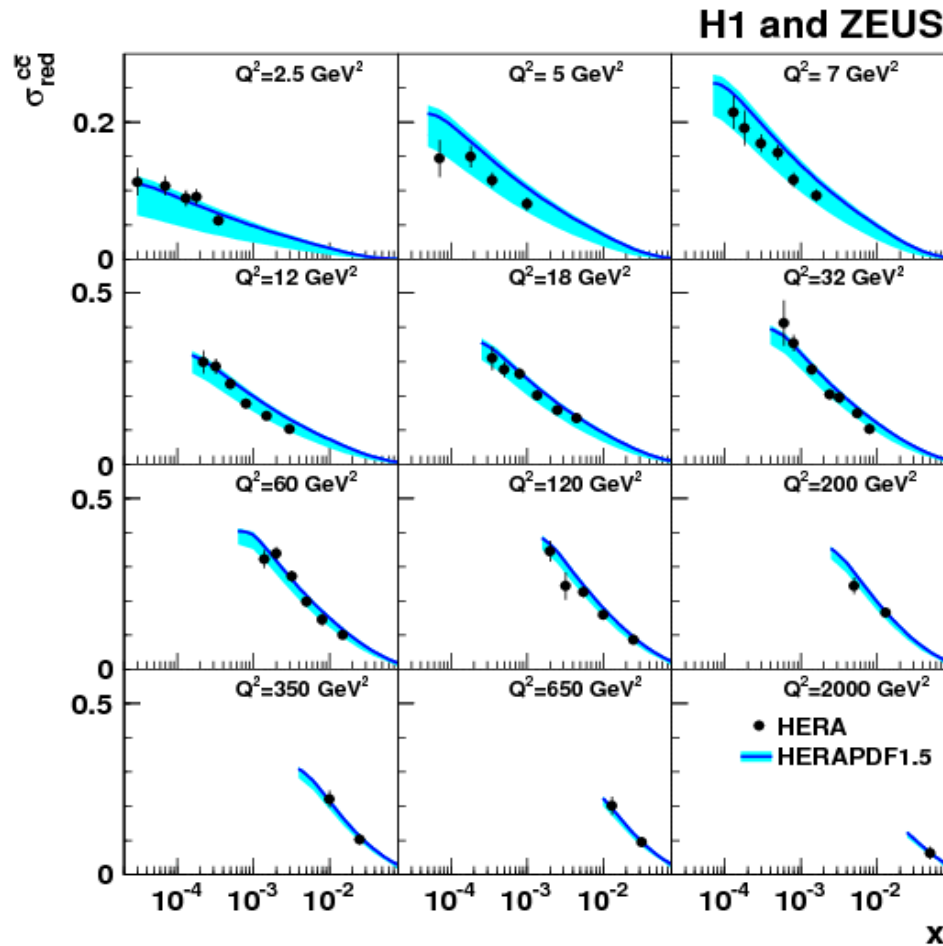
arXiv:1211.1182



➤ Significant improvement in precision obtained by combining H1 and ZEUS data

Inclusion of charm data

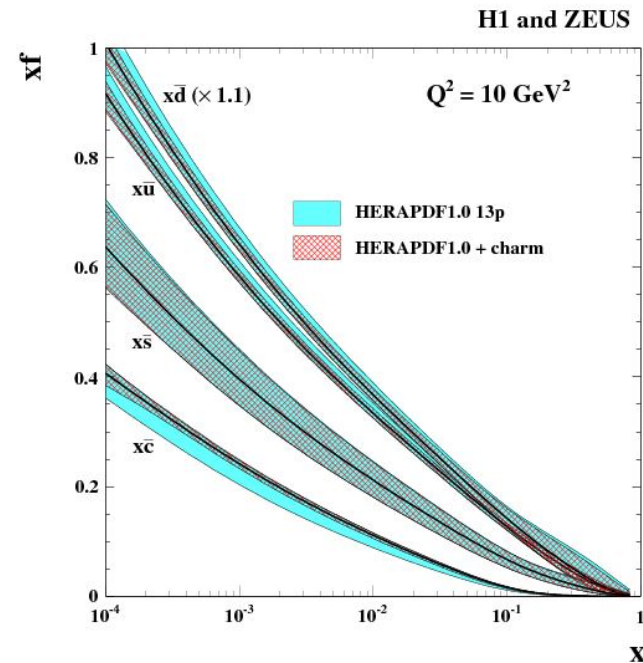
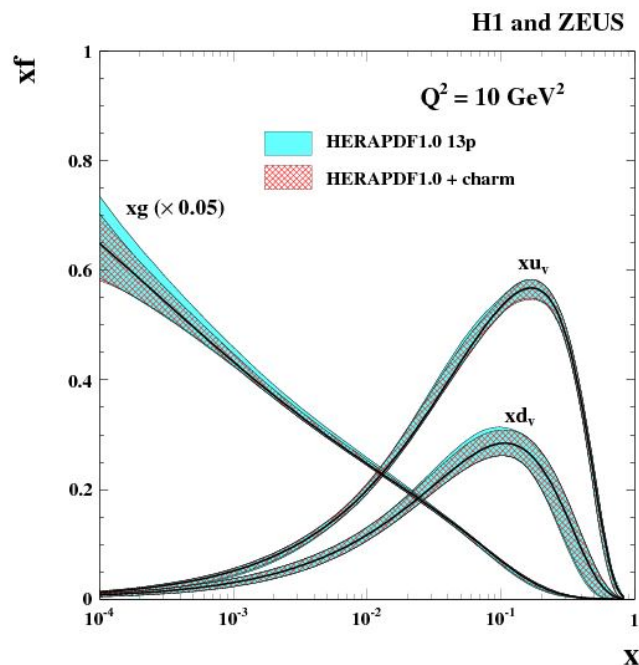
arXiv:1211.1182



- Reasonable agreement with HERAPDF1.5 when taking into account uncertainty on m_c ($1.35 < m_c < 1.65 \text{ GeV}$)

Inclusion of charm data

arXiv:1211.1182



- ❑ The uncertainties of the valence quark distribution functions unaffected
- ❑ The uncertainty on the gluon distribution function reduced (due to the constraints that the charm data put on the gluon through the $\gamma g \rightarrow c\bar{c}$)
- ❑ The uncertainty on the $x\bar{c}$ distribution function is considerably reduced due to the constrained range of m_c

Inclusion of charm data

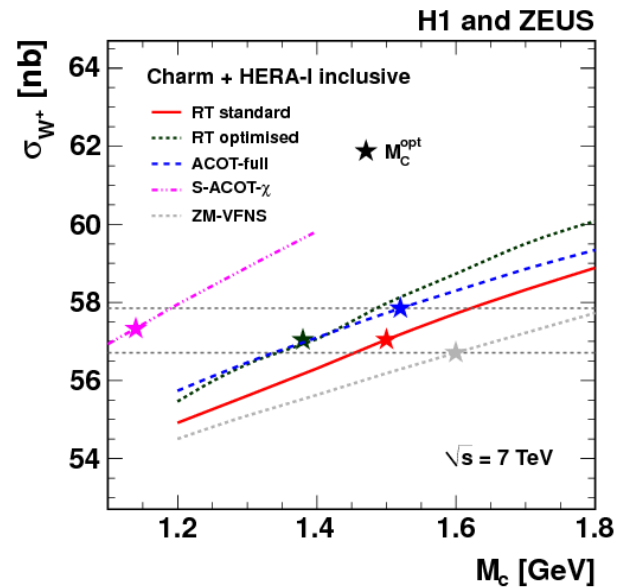
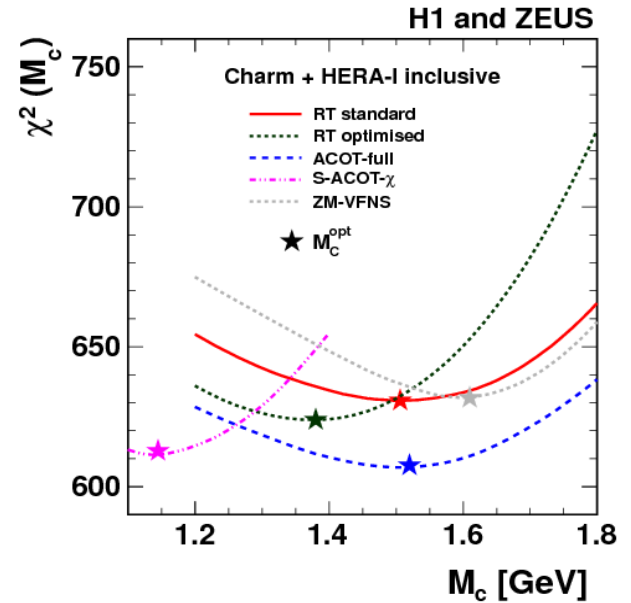
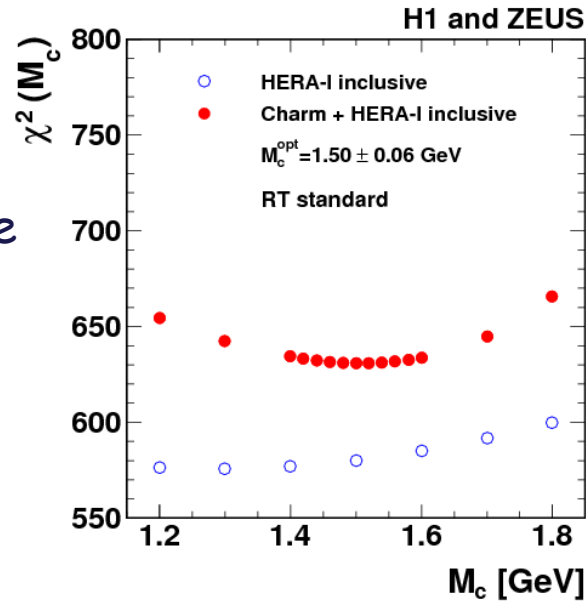
- ❑ Increased sensitivity to charm mass
- ❑ The σ^{cc} allows to determine the optimal charm mass parameter (M_c^{opt}) for the various VFNS schemes

arXiv:1211.1182

- ❑ For all implementations of VFNS a similar monotonic dependence of the W^\pm (and Z) production cross sections at the LHC on M_c is observed \rightarrow significant spread of about 6% between the predictions
- ❑ When using the M_c^{opt} for each scheme the spread of predictions is significantly reduced

N. Raicevic

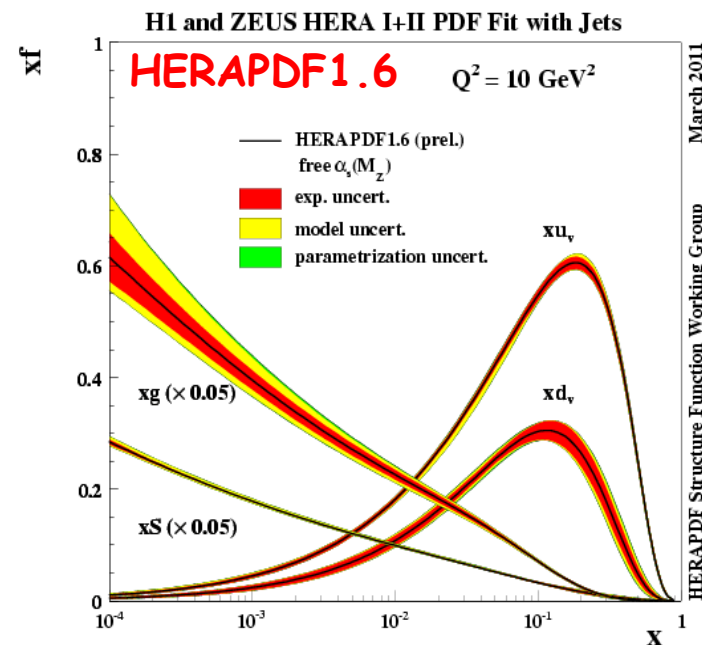
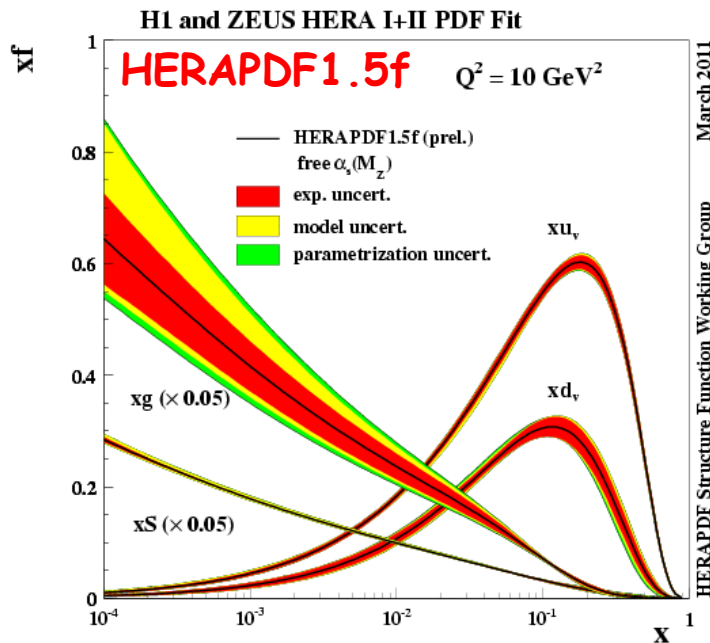
Excited QCD 2013



Inclusion of JETS

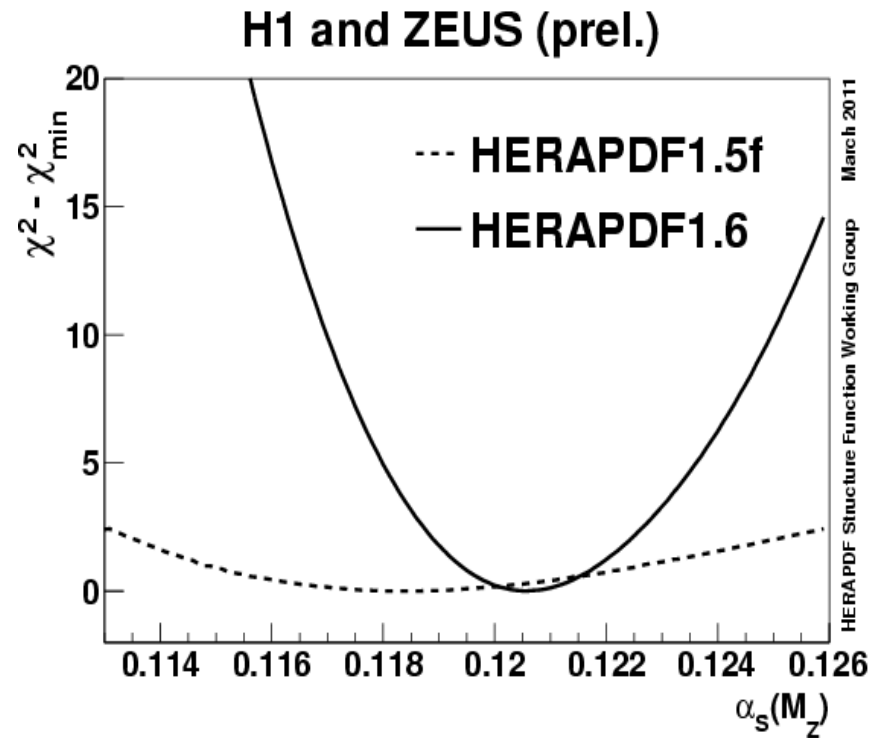
H1prelim-11-034 and ZEUS-prel-11-001

- ❑ **HERAPDF1.6**: the same input as for HERAPDF1.5 + 4 inclusive jet measurements from H1 and ZEUS
- ❑ HERAPDF1.6 to be compared to **HERAPDF1.5f** - the same input as HERAPDF1.5 but treating $\alpha_s(M_Z)$ as a **free parameter** as in HERAPDF1.6



- ❑ The jet data significantly reduce the correlation between the gluon PDF and α_s → improved precision of the gluon PDF and an unbiased determination of $\alpha_s(M_Z)$

α_s from HERAPDF1.6



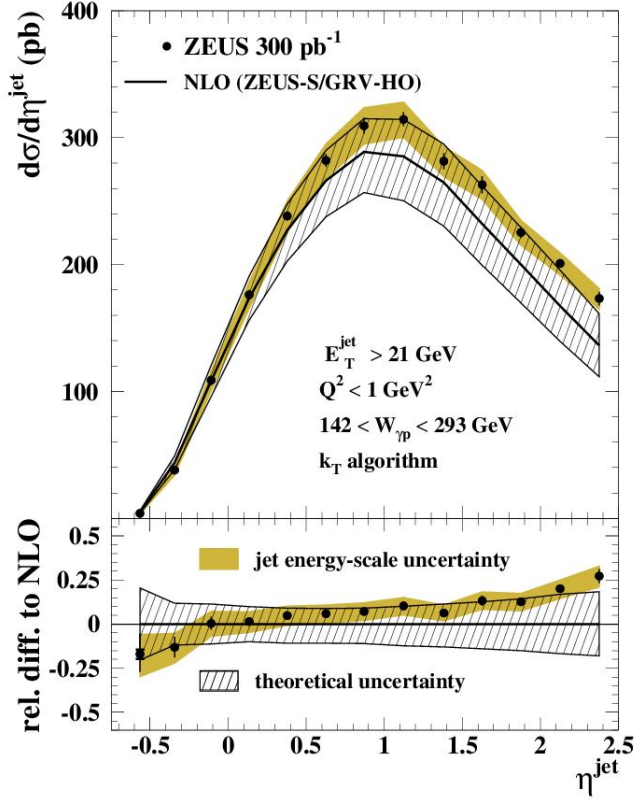
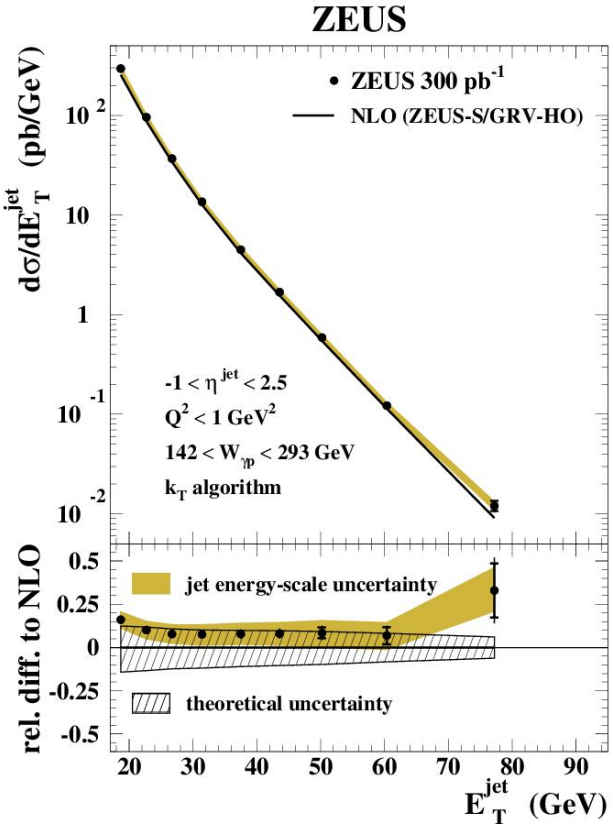
- Local minimum in $\Delta\chi^2(\alpha_s)$ pronounced only after including jet data

$$\alpha_s(M_Z) = 0.1202 \pm 0.0013(\text{exp.}) \pm 0.0007(\text{mod/param.}) \pm 0.0012(\text{had}) \begin{matrix} +0.0045 \\ -0.0036 \end{matrix}(\text{th})$$

Inclusive jets in photoproduction

Nucl. Phys. B864 (2012), 1

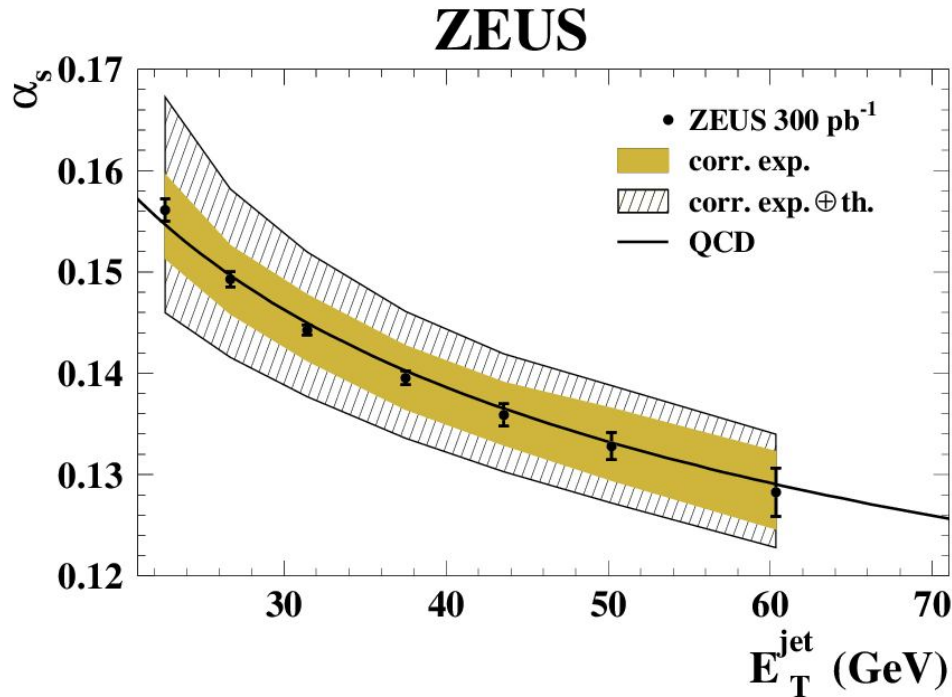
- Kinematic selection: $Q^2 < 1 \text{ GeV}^2$, $0.2 < \gamma < 0.85$, $142 < W_{\gamma p} < 293 \text{ GeV}$
 k_T algorithm, $-1 < \eta^{\text{jet}} < 2.5$



- Reasonable description of data with NLO pQCD calculations for $E_T^{\text{jet}} > 21 \text{ GeV}$

Inclusive jets in photoproduction

Nucl. Phys. B864 (2012), 1



- The α_s values determined in each E_T^{jet} value from the analysis of the measured $d\sigma/dE_T^{\text{jet}}$ via NLO QCD fit ($21 < E_T^{\text{jet}} < 71 \text{ GeV}$)
- Data are compared with QCD prediction of α_s at two loops

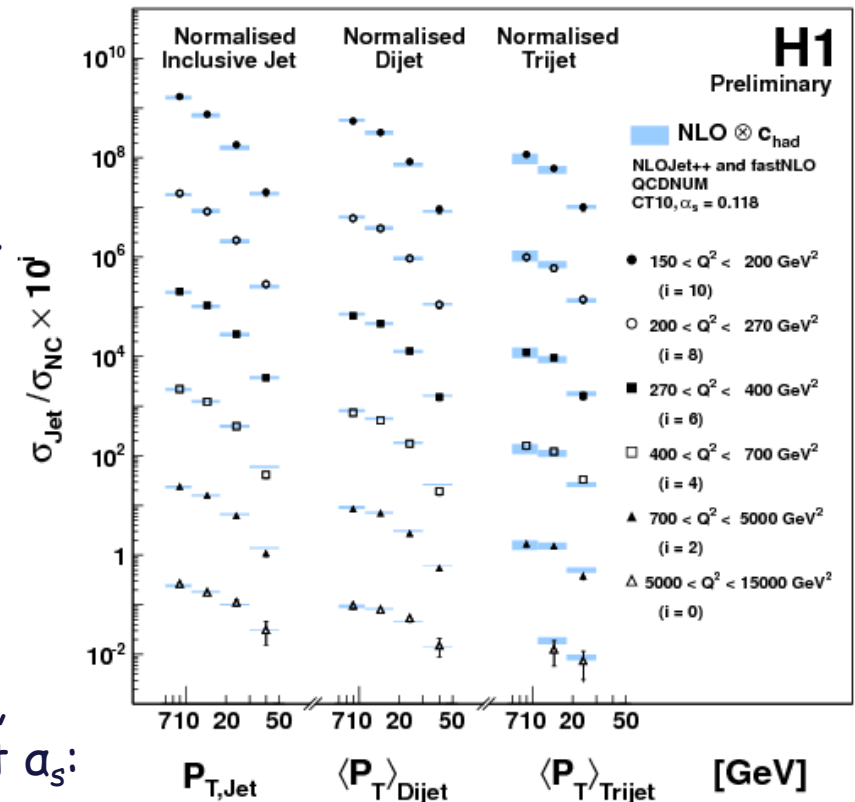
$$\alpha_s(M_Z) = 0.1206^{+0.0023}_{-0.0022} (\text{exp})^{+0.0042}_{-0.0035} (\text{th})$$

- The dominant uncertainties due to missing higher orders and due to photon PDFs at high η^{jet}

Normalised multijet cross sections at high Q^2 in DIS

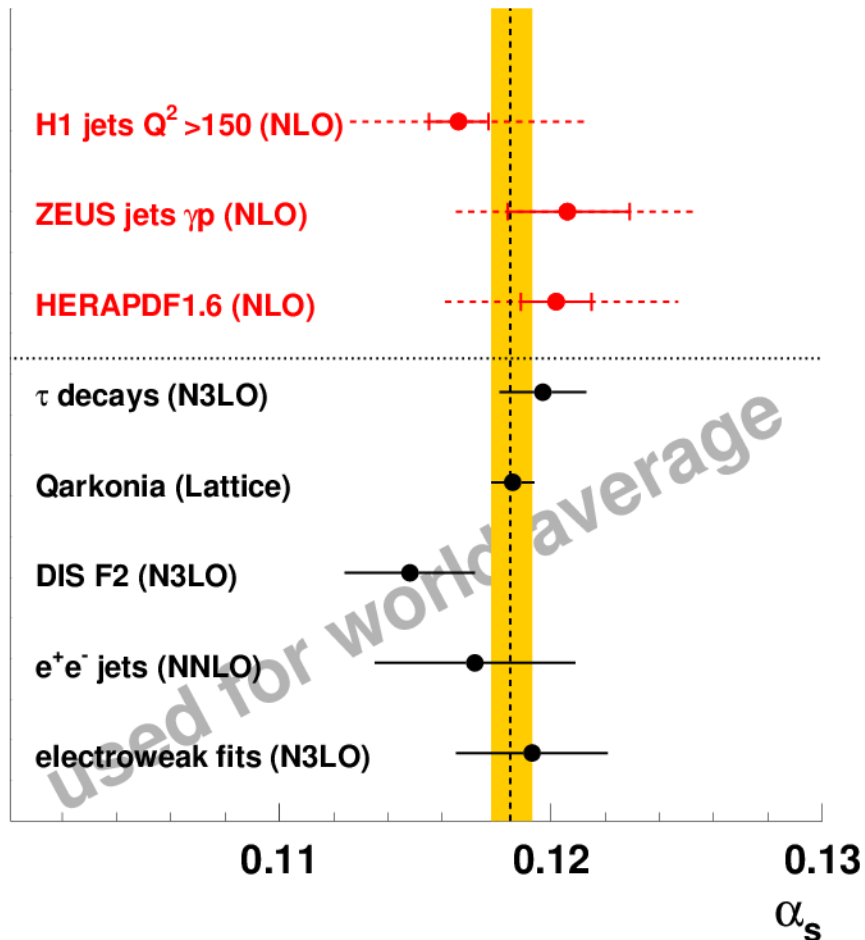
H1prelim-12-031

- ❑ Kinematic selection: $150 < Q^2 < 1500 \text{ GeV}^2$, $0.2 < y < 0.7$, $7 < P_T < 50 \text{ GeV}$
 $5 < P_{T,i} < 50 \text{ GeV}$, $M_{1,2} > 16 \text{ GeV}$ (HERA-II)
- ❑ Compared to a previously published result on multijet cross sections:
 - an extended range in jet pseudorapidity
 - an improved hadronic energy scale uncert. of 1%
- ❑ Measured cross sections described well with NLO QCD predictions
- ❑ Theoretical uncertainties dominated by missing higher orders in pQCD
- ❑ Combined NLO fit to normalised inclusive, dijet and trijet cross sections to extract α_s :



$$\alpha_s(M_Z) = 0.1163 \pm 0.0008 (\text{exp.}) \pm 0.0011 (\text{had}) \pm 0.0014 (\text{pdf}) \begin{matrix} +0.0044 \\ -0.0035 \end{matrix} (\text{th})$$

Summary on recent α_s measurements at HERA



- ❑ HERA measurements of α_s consistent with world average
- ❑ Due to the uncertainty coming from the terms beyond NLO, α_s measurements from HERA have sizable theoretical uncertainties
- ❑ HERA measurements are statistically as precise as the measurements included in the world average

Summary

- ❑ New measurements on NC and CC from HERA-II at high Q^2 from both experiments → improvement for the valence quark distributions
- ❑ New combined measurement of charm production cross section at HERA → used as input for a detailed NLO QCD analysis
- ❑ Jet measurements from HERA improve the gluon PDF and provide simultaneous determination of PDFs and α_s
- ❑ New jet measurements from both experiments → new and more precise α_s from HERA
- HERA experiments are providing unprecedented knowledge about proton structure
- HERA results are important inputs for LHC predictions

Backup

Averaging procedure

- ❑ Swim all points to a common x-Q² grid
- ❑ Moved 820 GeV data to 920 GeV p-beam energy
- ❑ Calculate average values and uncertainties
 χ^2 minimization in which the parameters are the true values of the cross section and the correlated systematic error parameters ([arXiv:0904.0929](https://arxiv.org/abs/0904.0929))

- ❑ Evaluate "procedural uncertainties"

$$\chi_{\text{exp}}^2(\mathbf{m}, \mathbf{b}) = \sum_i \frac{[m^i - \sum_j \Gamma_j^i b_j - \mu^i]^2}{\Delta_i^2} + \sum_j b_j^2$$

- Exploit differences between H1 and ZEUS in detectors, methods and systematics to "cross-calibrate" and to reduce the systematic uncertainties.

- ❑ For multiplicative error sources small biases to lower cross section values may occur. This can be avoided modifying the χ^2 definition as:

$$\chi_{\text{exp}}^2(\mathbf{m}, \mathbf{b}) = \sum_i \frac{[m^i - \sum_j \gamma_j^i m^i b_j - \mu^i]^2}{\delta_{i,\text{stat}}^2 (m^i - \sum_j \gamma_j^i m^i b_j) + (\delta_{i,\text{uncor}} m^i)^2} + \sum_j b_j^2$$

$$\gamma_j^i = \Gamma_j^i / \mu^i \quad \delta_{i,\text{stat}} = \Delta_{i,\text{stat}} / \mu^i \quad \delta_{i,\text{uncor}} = \Delta_{i,\text{uncor}} / \mu^i$$

QCD analysis

- DGLAP analysis based only on the HERA data:
 - no need for heavy target corrections
 - no strong isospin assumptions
- Some parameters in parametrisation functions constrained by the number and momentum sum rules

$$\Sigma \text{mom.} = 1 \quad \int u_v dx = 2 \quad \int d_v dx = 1$$

Fitted PDFs: $xg, xu_v, xd_v, x\bar{U} = x\bar{u} + (x\bar{c}), x\bar{D} = x\bar{d} + x\bar{s} + (x\bar{b})$

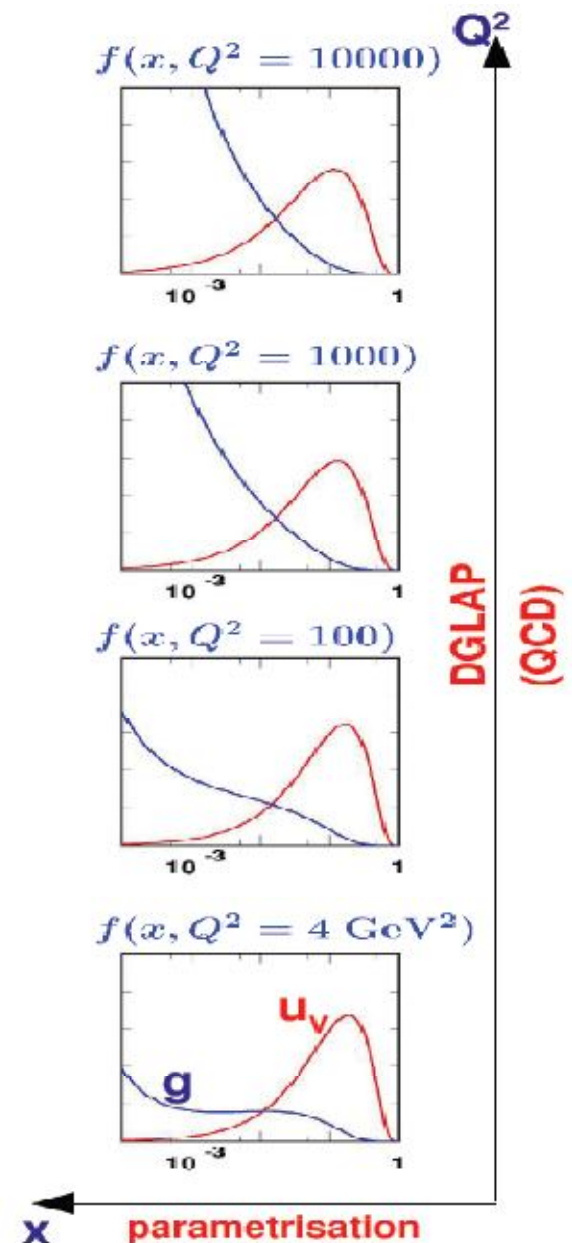
Uncertainties

- Experimental - using $\Delta\chi^2 = 1$ criterion
- Model - from variation of theory parameters:

Variation	Standard Value	Lower Limit	Upper Limit
f_s	0.31	0.23	0.38
m_c [GeV]	1.4	1.35 ^(a)	1.65
m_b [GeV]	4.75	4.3	5.0
Q_{min}^2 [GeV ²]	3.5	2.5	5.0
Q_0^2 [GeV ²]	1.9	1.5 ^(b)	2.5 ^(c,d)

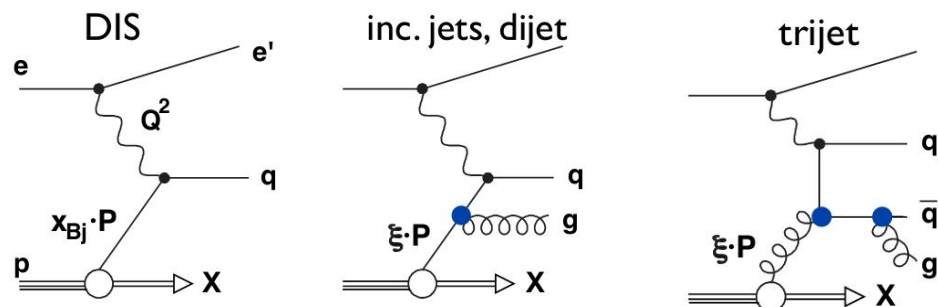
- Parameterisation - from extra D, E, ... terms in parameterisation

N. Raicevic

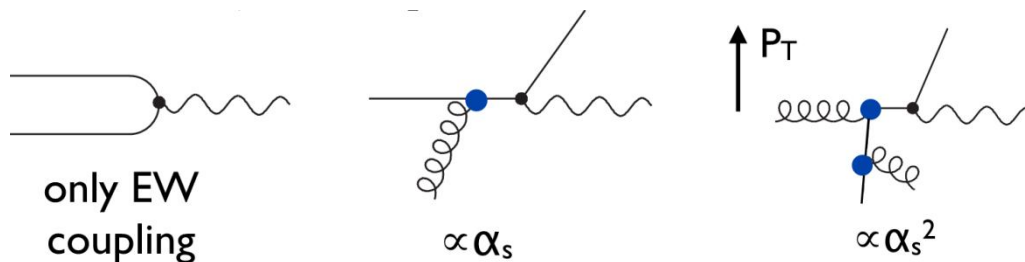


Excited QCD 2013

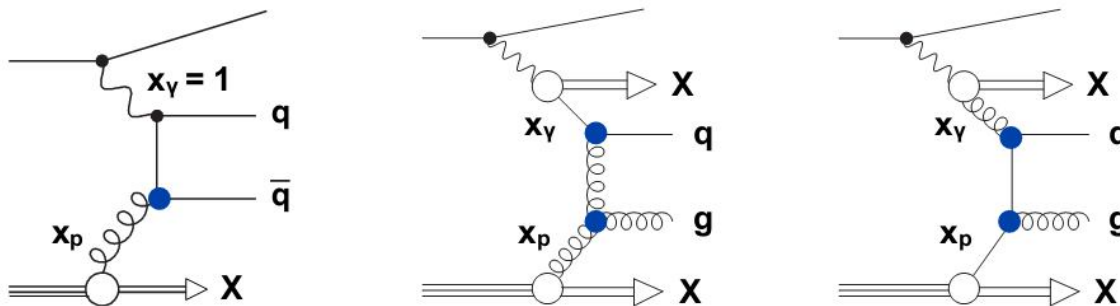
Jet production in DIS



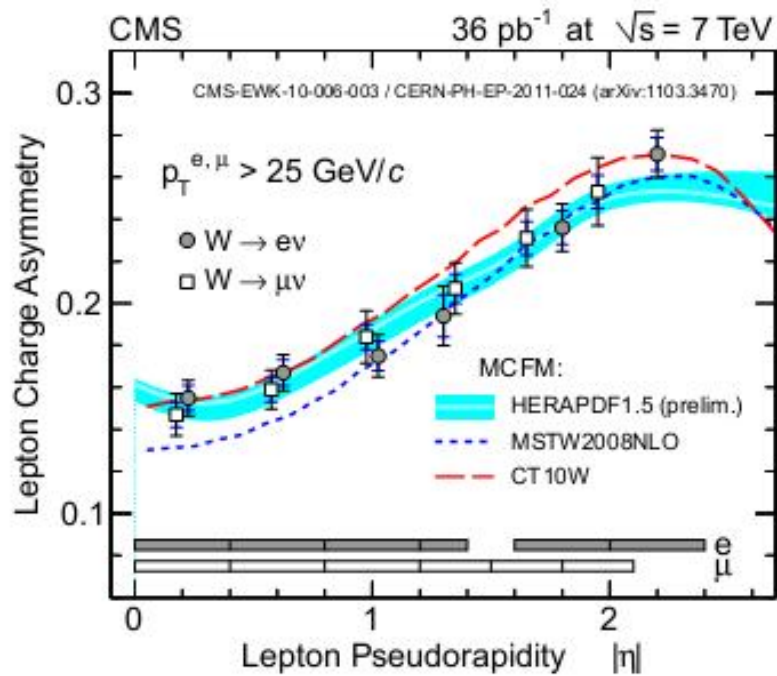
Boost to Breit frame, $2xP + q = 0$



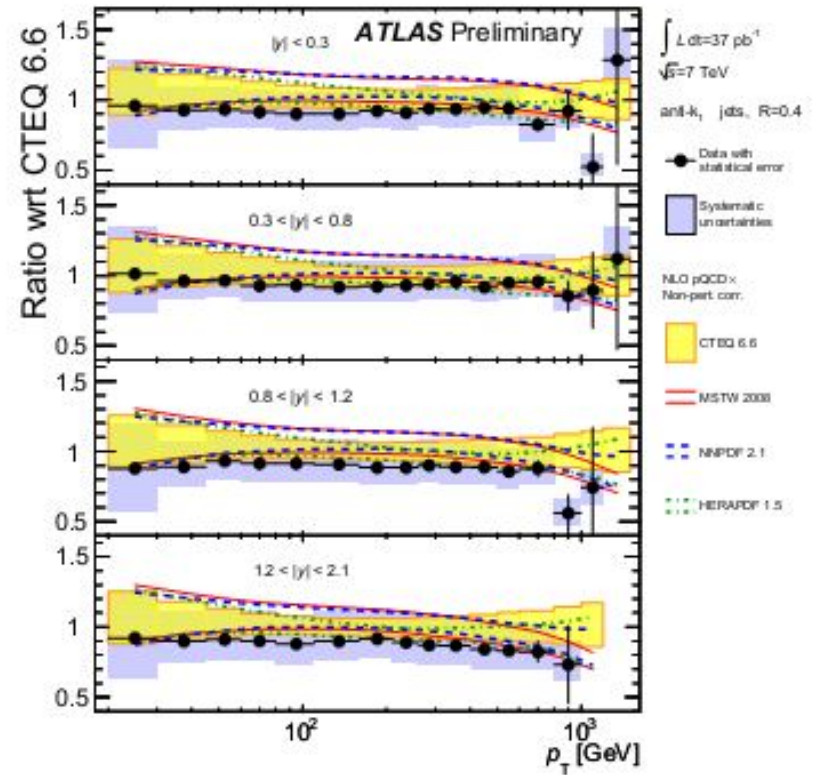
Jet production in photoproduction



HERAPDF predictions for LHC



➤ W decay lepton asymmetry data from CMS



□ ATLAS jet data in the central region in ratio to the predictions of CTEQ6.6