



# Combination of Inclusive $e^\pm p$ Cross-Section Measurements at HERA



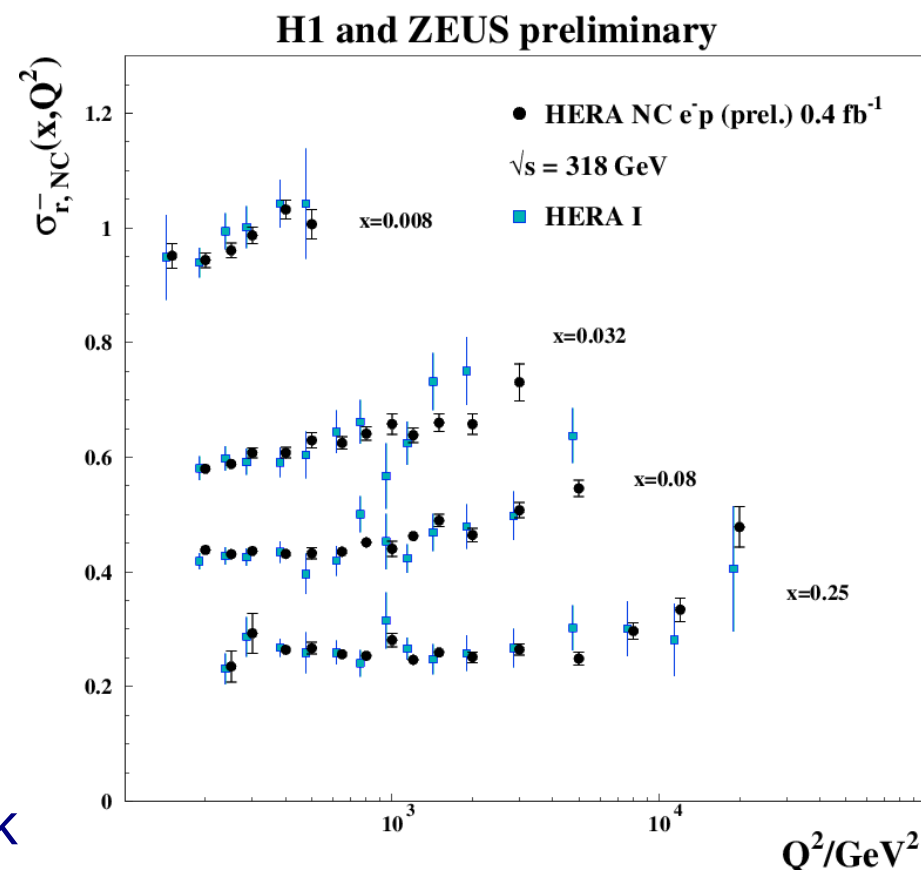
Oleksii Turkot  
DESY



On behalf of H1 and ZEUS Collaborations

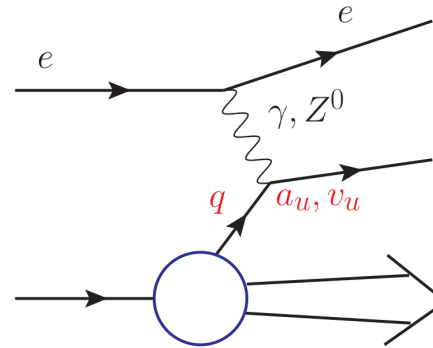
## Motivation

- ◆ HERA II data collected during 2002 — 2007 and provides approximately  $0.4 \text{ fb}^{-1}$  of luminosity for each H1 and ZEUS experiments. Great statistical improvement compare to  $0.1 \text{ fb}^{-1}$  of HERA I.
- ◆ 162 sources of correlated systematic uncertainties are taken into account.
- ◆ The combined HERA I+II cross sections are used as an input in a QCD analysis to extract new proton's PDFs.
  - see V. Radescu talk.
- ◆ HERAPDF 1.5 prel will be replaced by HERAPDF 2.0.
  - see A. Cooper-Sarkar talk



# Inclusive DIS

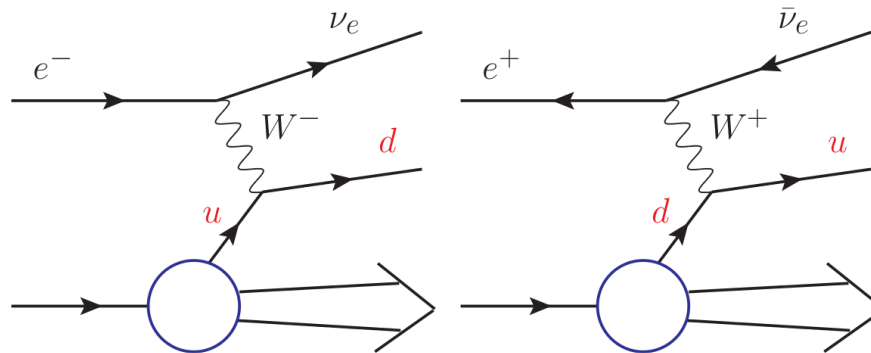
Neutral Current :



$$\frac{d^2 \sigma_{NC}^{e\bar{\nu}p}}{dx dQ^2} = \frac{2\pi\alpha^2 \cdot Y_{\pm}}{xQ^4} \cdot \left( F_2(x, Q^2) \pm \frac{Y_{-}}{Y_{+}} \cdot x \cdot F_3(x, Q^2) - \frac{y^2}{Y_{+}} \cdot F_L(x, Q^2) \right)$$

$$Y_{\pm} = 1 \pm (1-y)^2$$

Charged Current :



$$\frac{d^2 \sigma_{CC}^{e\bar{\nu}p}}{dx dQ^2} = \frac{G_F^2}{4\pi x} \cdot \kappa^2 \cdot \left( Y_{+} \cdot W_2^{\mp} \pm Y_{-} \cdot x \cdot W_3^{\mp} - y^2 \cdot W_L^{\mp} \right)$$

$$\kappa = \frac{M_W^2}{M_W^2 + Q^2}$$

## ZEUS and H1 experiments



**HERA** is worlds only  $e^\pm p$  collider :

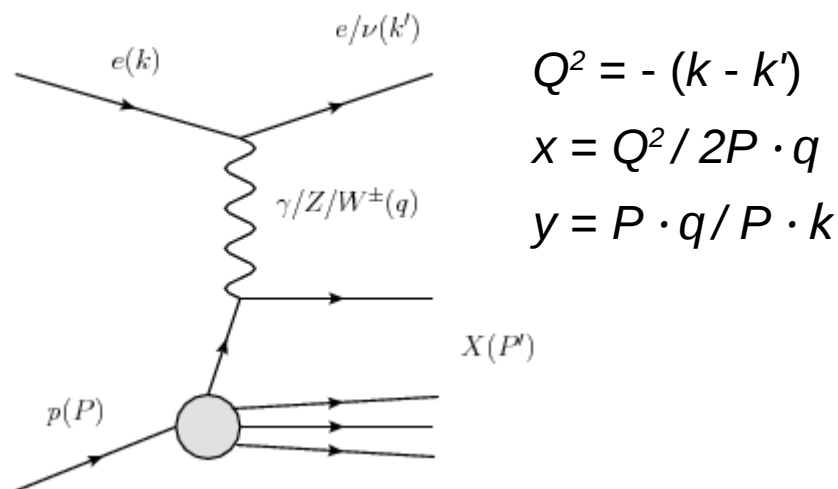
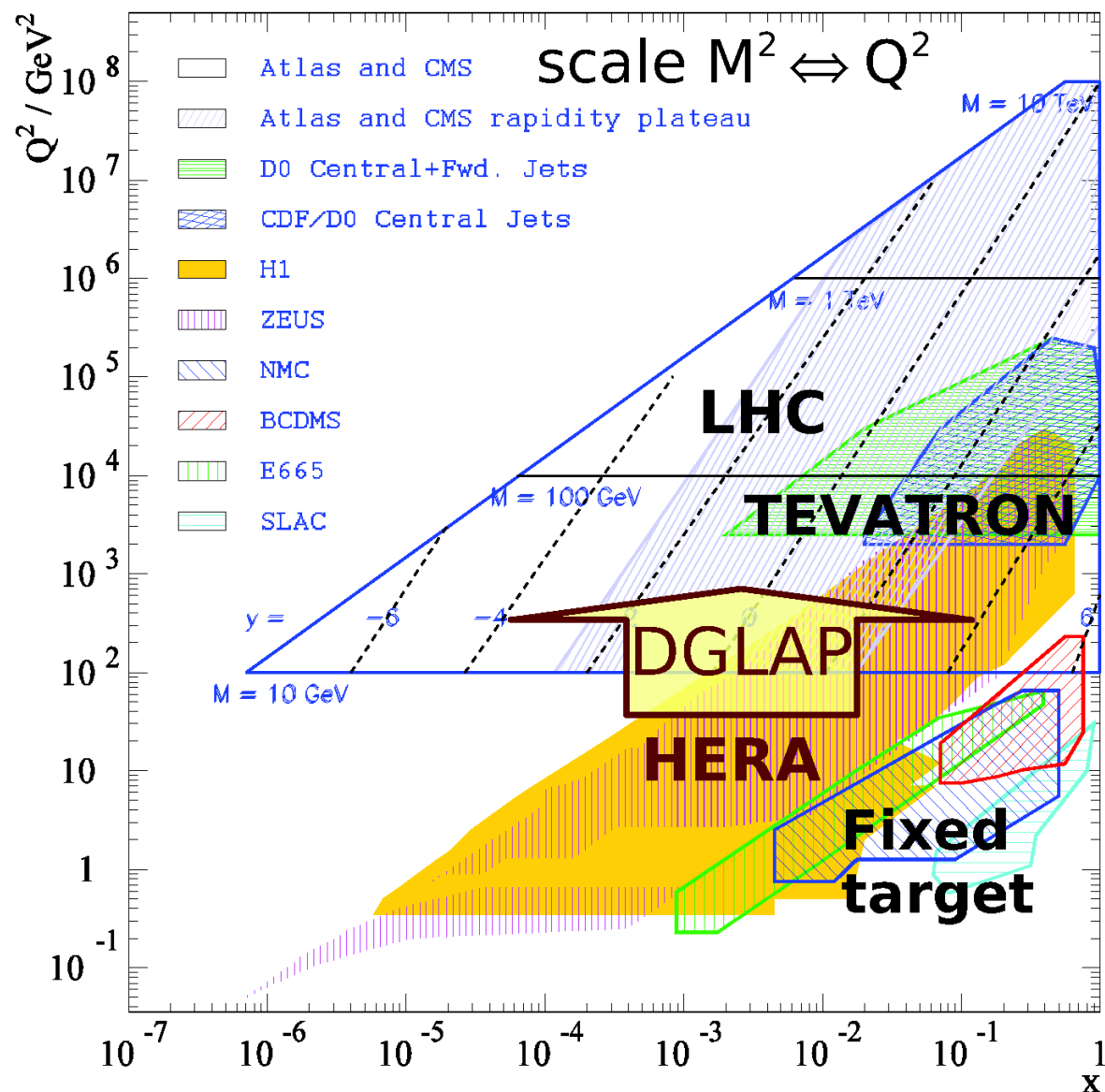
operated during 1992 — 2007;  
 $e^\pm$  energy 27.5 GeV;  
 $p$  energies 920, 820, 575 and 460 GeV.

**H1** and **ZEUS** — two colliding experiments at HERA :

$\sim 0.5 \text{ fb}^{-1}$  of luminosity  
recorded by each experiment.

HERA data provides unique opportunity to study the structure of the proton.

# HERA data and the LHC



HERA data covers nearly the whole  $x$  range of the LHC.

Evolution in  $Q^2$  via DGLAP allows to extrapolate HERA PDFs into LHC region.

## Inclusive DIS Data Samples

Input data — 41 final data sets with HERA inclusive measurements:

- ◆ 21 HERA I data samples
- ◆ 20 HERA II data samples, including:
  - ◆ 8 inclusive HERA II  $E_p = 920$  GeV
  - ◆ 4 high  $y$  data  $E_p = 920$  GeV
  - ◆ 4 high  $y$  data  $E_p = 575$  GeV
  - ◆ 4 high  $y$  data  $E_p = 460$  GeV

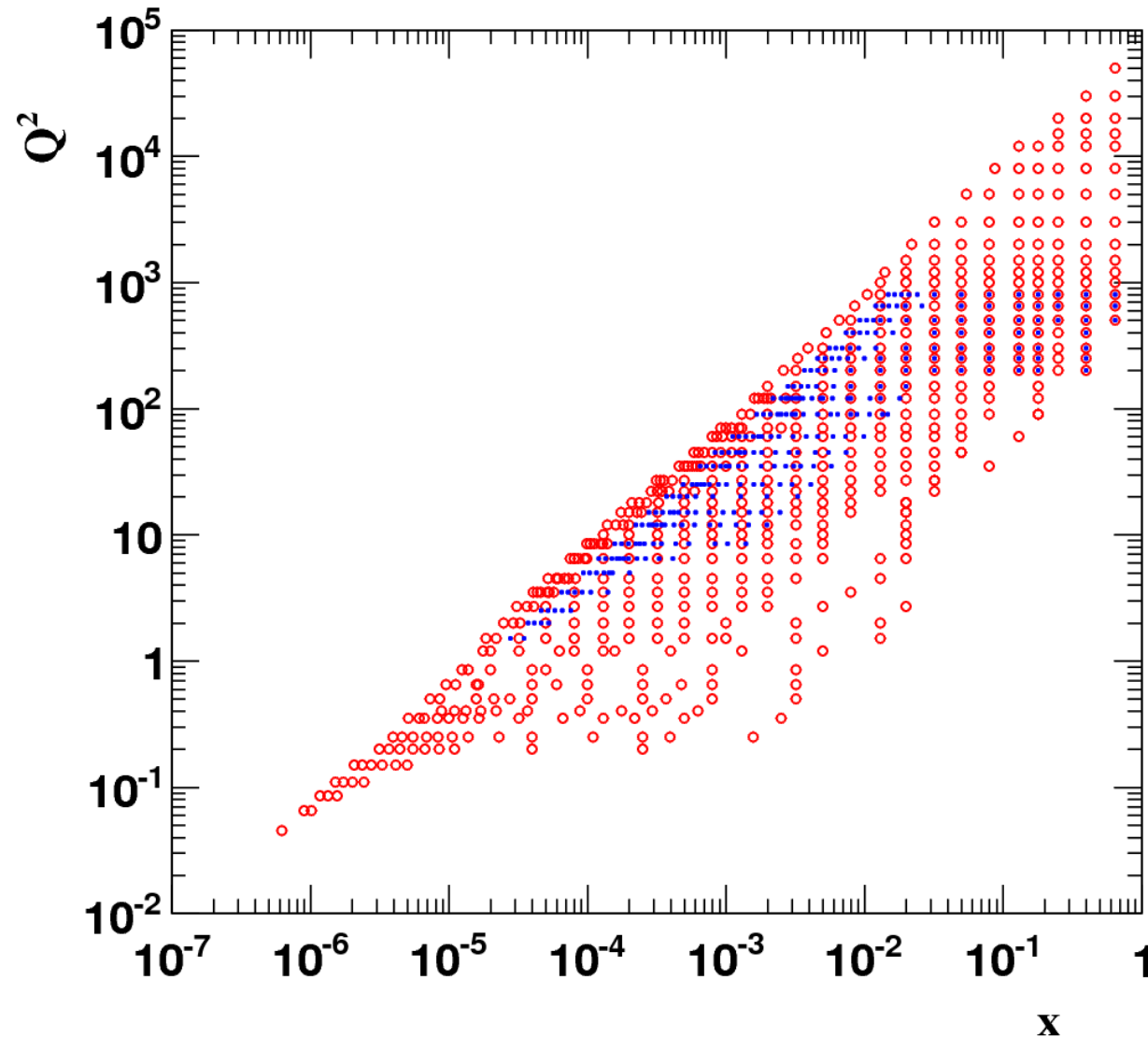
→ see J.Grebenyuk and S.Shushkevich talks.

Total of **2927** data points combined to **1307**.

## Combination procedure

- Swim all points to common  $x - Q^2$  grids and to one of common proton beam energies.
- Average cross - section values.
- Evaluate procedural uncertainties.

## x-Q<sup>2</sup> common grids



Two separate grids :

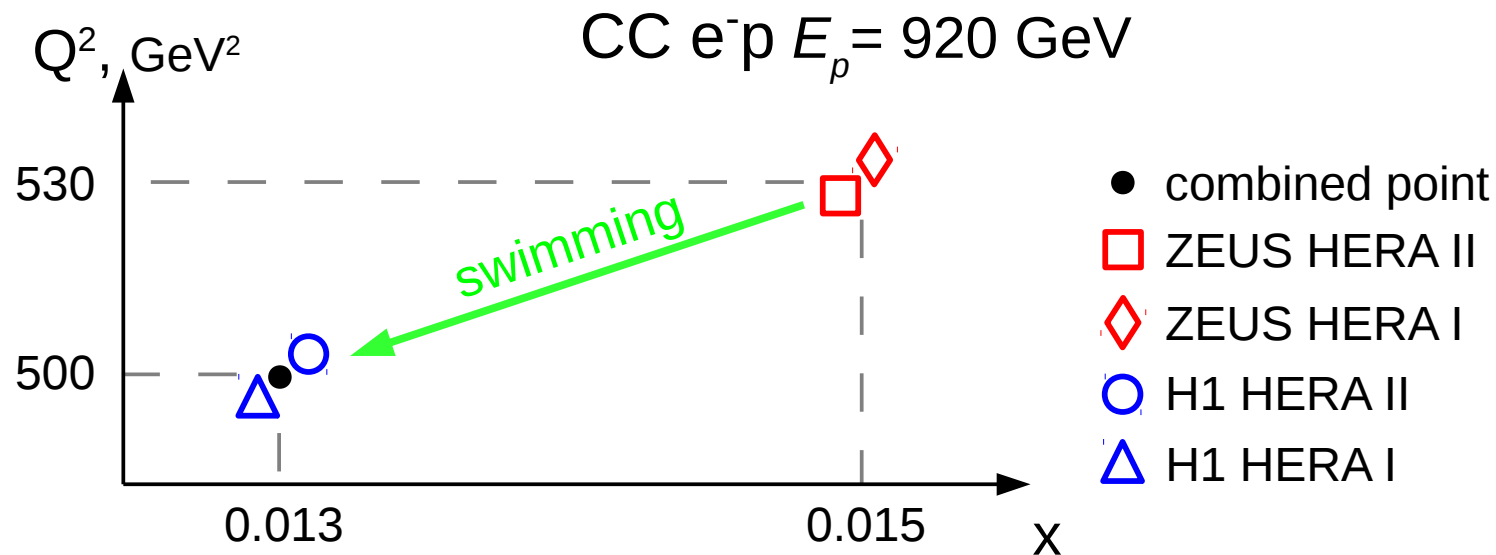
- inclusive grid, for  $E_p = 920$  GeV and  $E_p = 820$  GeV data sets;
- fine x grid, for  $E_p = 575$  GeV and  $E_p = 460$  GeV data sets.



## Swimming procedure

$$\sigma_{\text{meas}}^{e\bar{\nu}p}(X_{\text{grid}}, Q_{\text{grid}}^2) = \frac{\sigma_{\text{model}}^{e\bar{\nu}p}(X_{\text{grid}}, Q_{\text{grid}}^2)}{\sigma_{\text{model}}^{e\bar{\nu}p}(X_{\text{meas}}, Q_{\text{meas}}^2)} \cdot \sigma_{\text{meas}}^{e\bar{\nu}p}(X_{\text{meas}}, Q_{\text{meas}}^2)$$

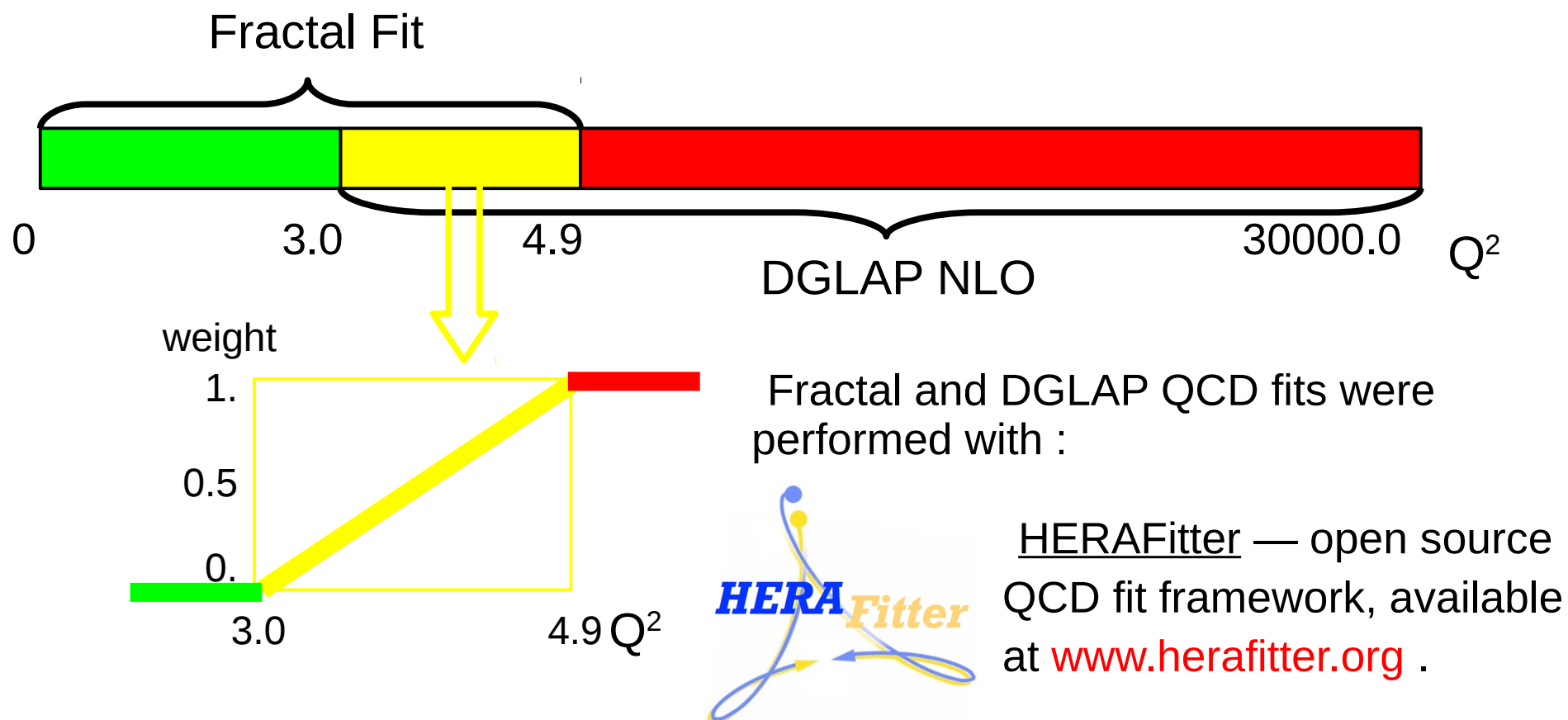
We need a model for the swimming.



Swimming factors are usually at level of few percent.

## Swimming procedure

The swimming done iteratively with our own data.



Averaging of scale factors is performed in dependence on  $Q^2$ .

## Cross Sections Averaging

The combination of the data done with HERAverager.

( available at [wiki-zeuthen.desy.de/HERAverager](http://wiki-zeuthen.desy.de/HERAverager) ).

All **162** correlated systematic sources are treated as multiplicative and the  $\chi^2$  definition:

$$\chi^2(\mathbf{m}, \mathbf{b}) = \sum_i \frac{[m^i - \sum_j \gamma_j^i m^i b_j - \mu^i]^2}{\delta_{i,stat}^2 \mu^i (m^i - \sum_j \gamma_j^i m^i b_j) + (\delta_{i,uncorr} m^i)^2} + \sum_j b_j^2$$

Procedural errors are calculated:

- ◆ multiplicative vs additive;
- ◆ possible correlations between data sets :
  - ◆ photoproduction background;
  - ◆ hadronic energy scale.

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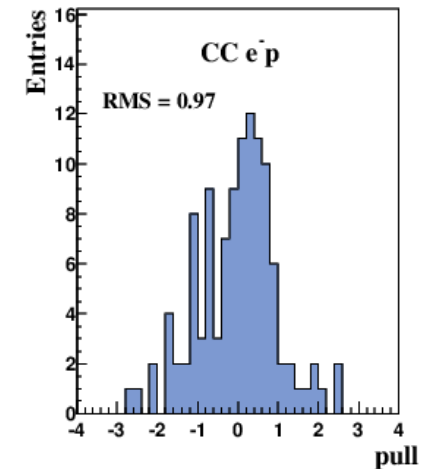
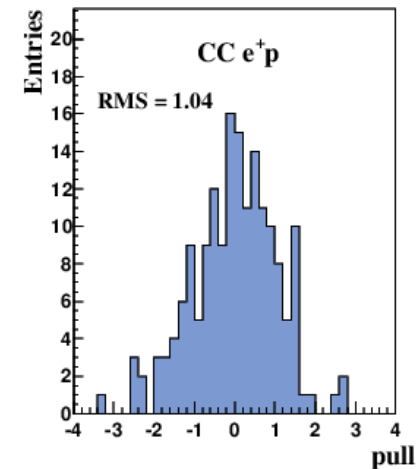
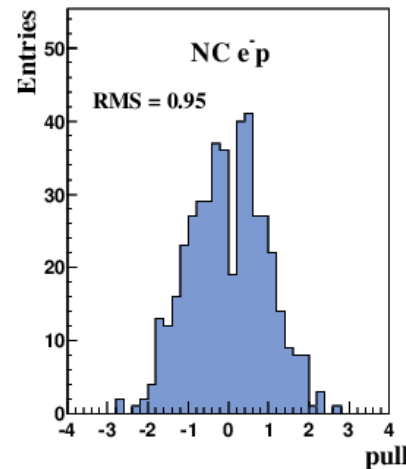
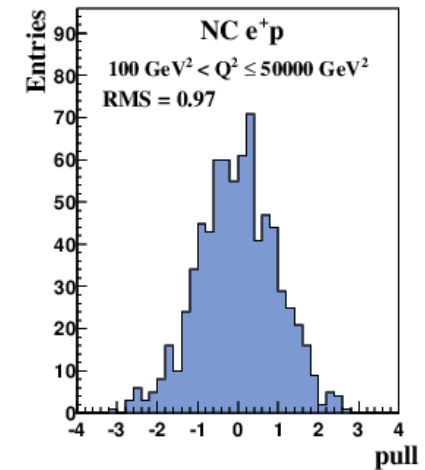
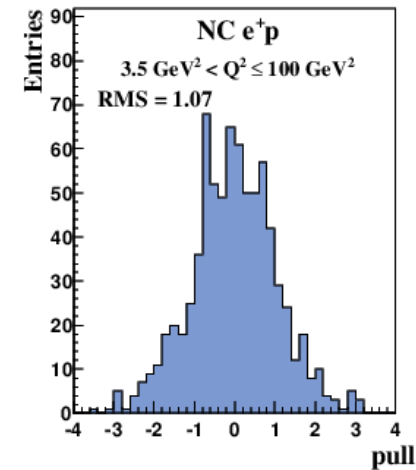
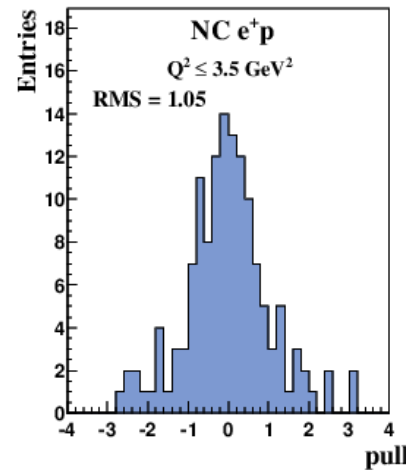
# Fit results

Good consistency of data sets:  $\chi^2 / \text{ndf} = 1685 / 1620$

H1 and ZEUS preliminary

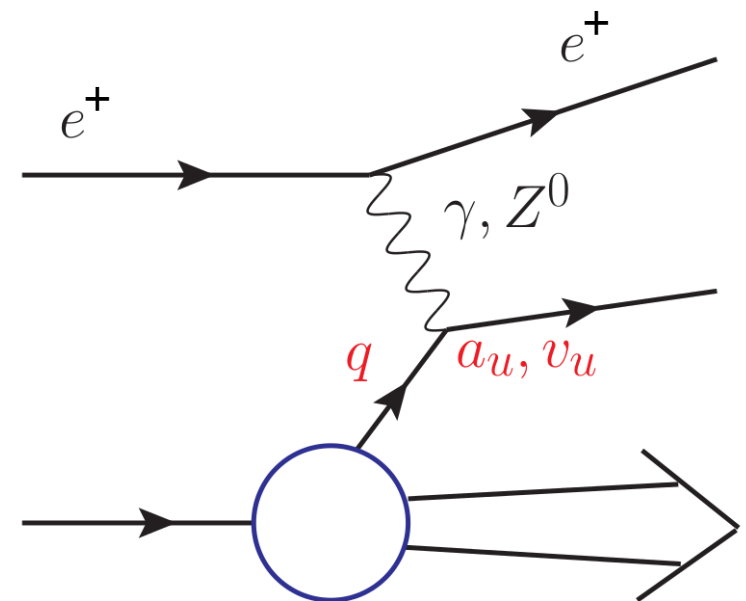
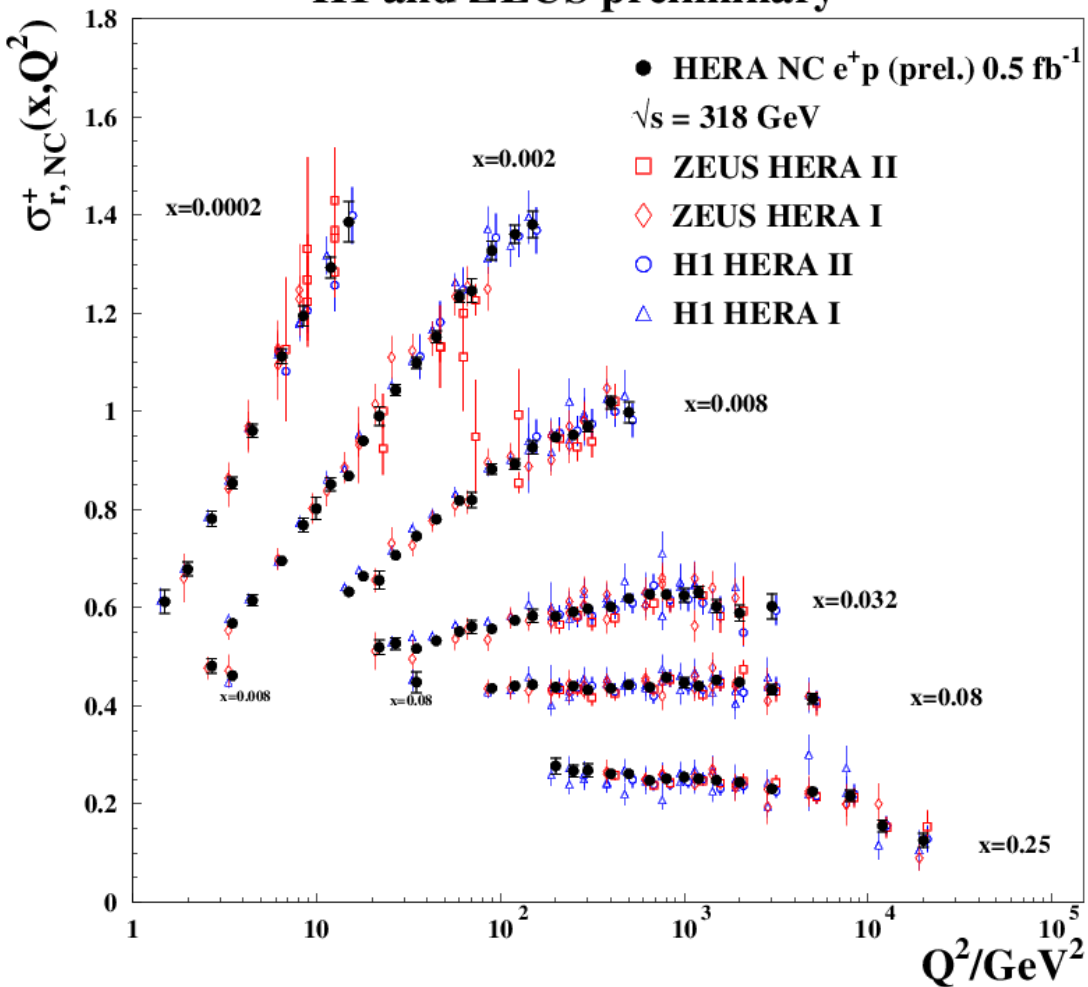
The pulls are defined as:

$$\text{pull}^{i,k} = \frac{\mu^{i,k} - m^i}{\sqrt{\Delta_{i,k}^2 - \Delta_{i,\text{ave}}^2}}$$



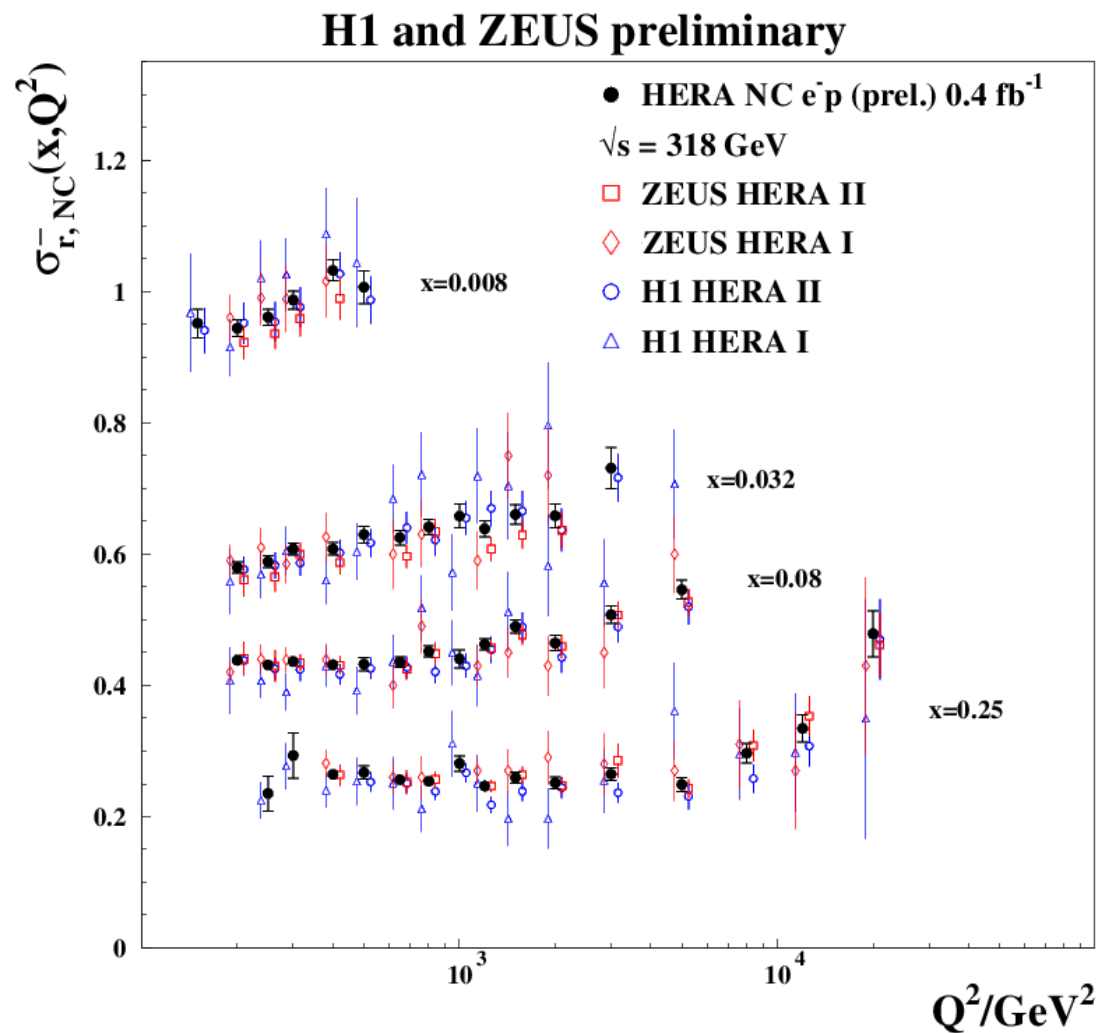
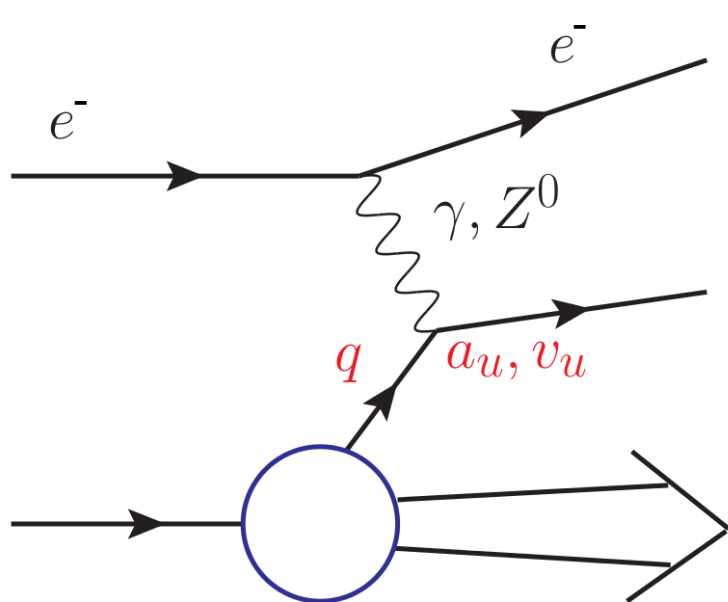
# Averaged Cross Sections : NC $e^+p$

H1 and ZEUS preliminary



Many points are combined into one data point

# Averaged Cross Sections : NC e<sup>-</sup>p

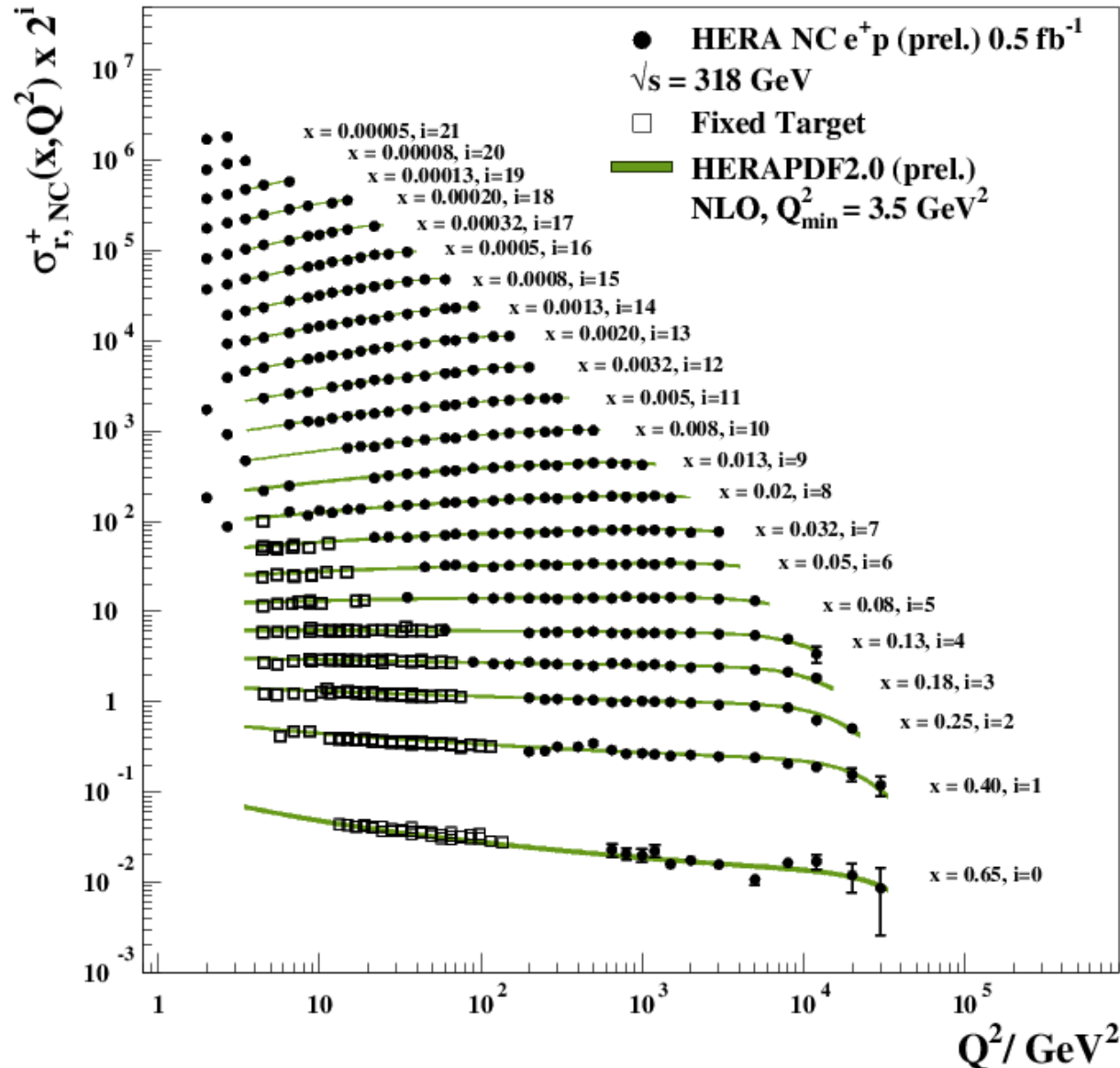


Many points are combined into one data point



# Averaged Cross Sections : NC $e^+p$

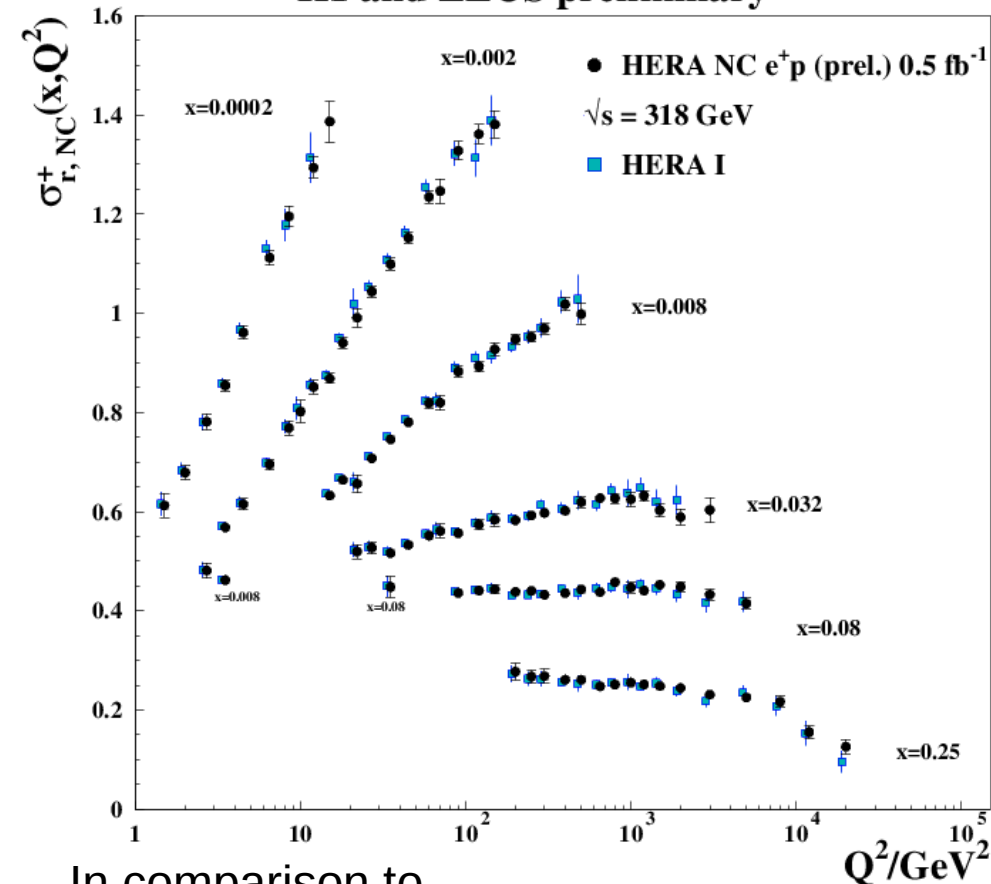
H1 and ZEUS preliminary



# Averaged Cross Sections : NC ep

## NC $e^+p$

H1 and ZEUS preliminary

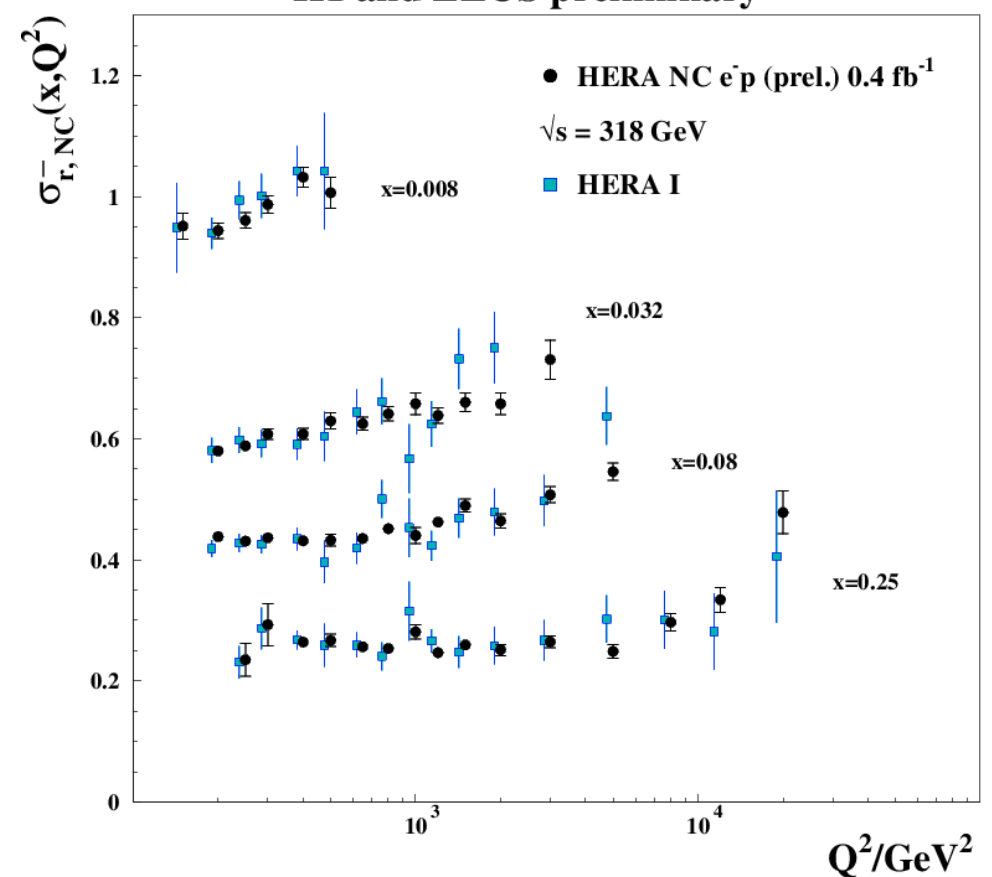


In comparison to  
HERA I luminosity :

x 3

## NC $e^-p$

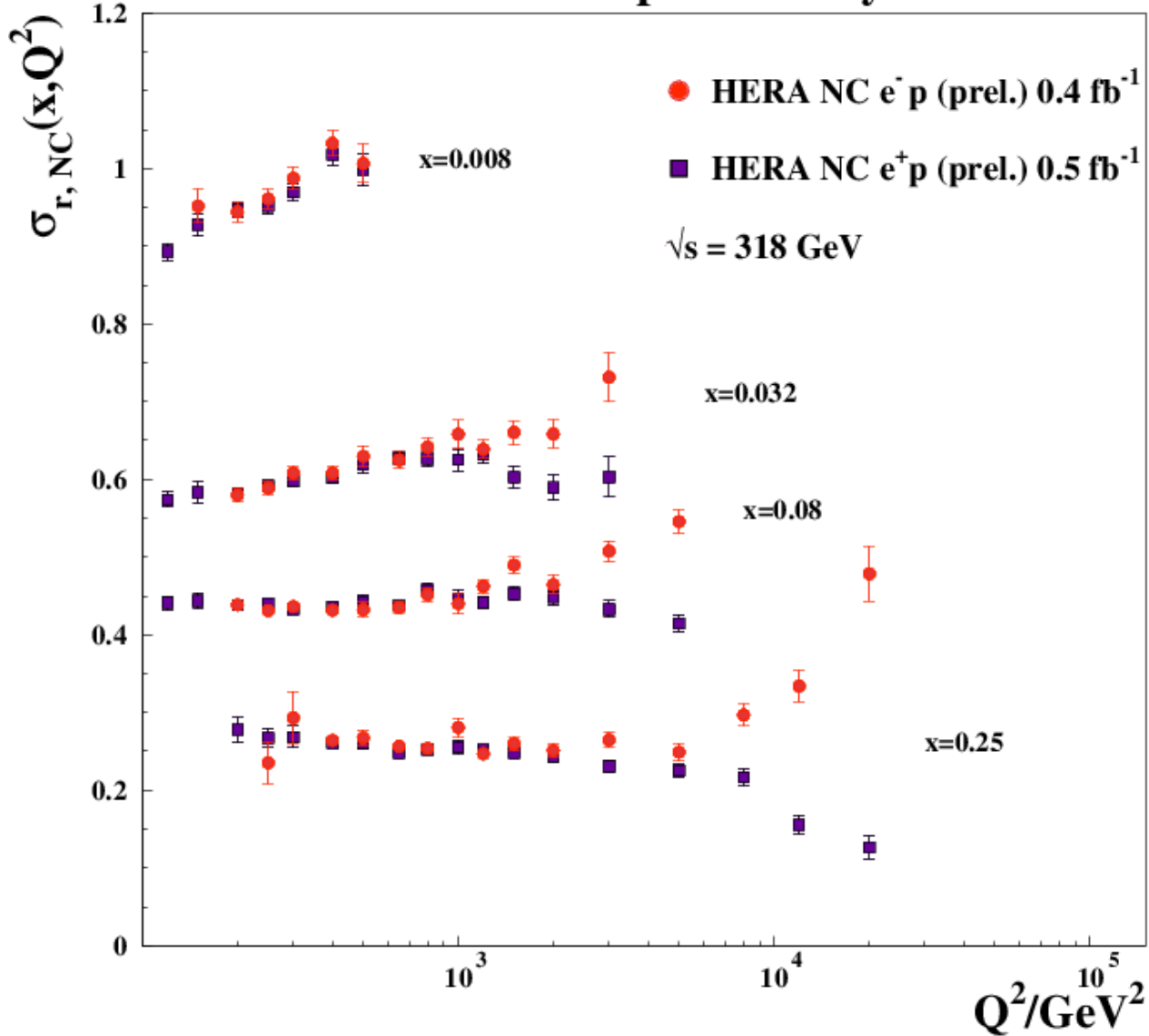
H1 and ZEUS preliminary



x 10

Big improvement in precision in comparison to HERA I, especially at high  $Q^2$

## H1 and ZEUS preliminary

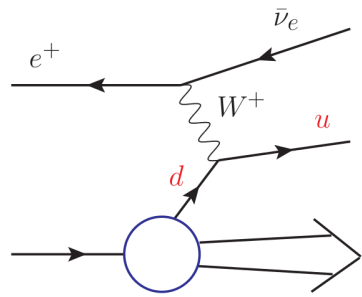


Difference in NC  $e^+ p$  and  $e^- p$  at high  $Q^2$  :

◆  $Q^2 \sim M_Z^2$  !  $\gamma Z^0$  interference clearly seen :

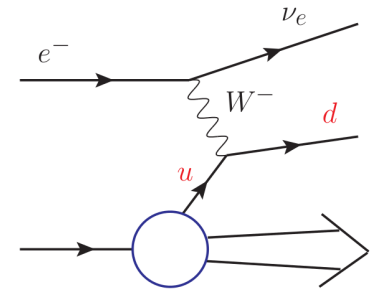
- ◆ In NC  $e^+ p$  negative  $\gamma Z^0$  interference
- ◆ In NC  $e^- p$  positive  $\gamma Z^0$  interference

Electroweak effects clearly seen



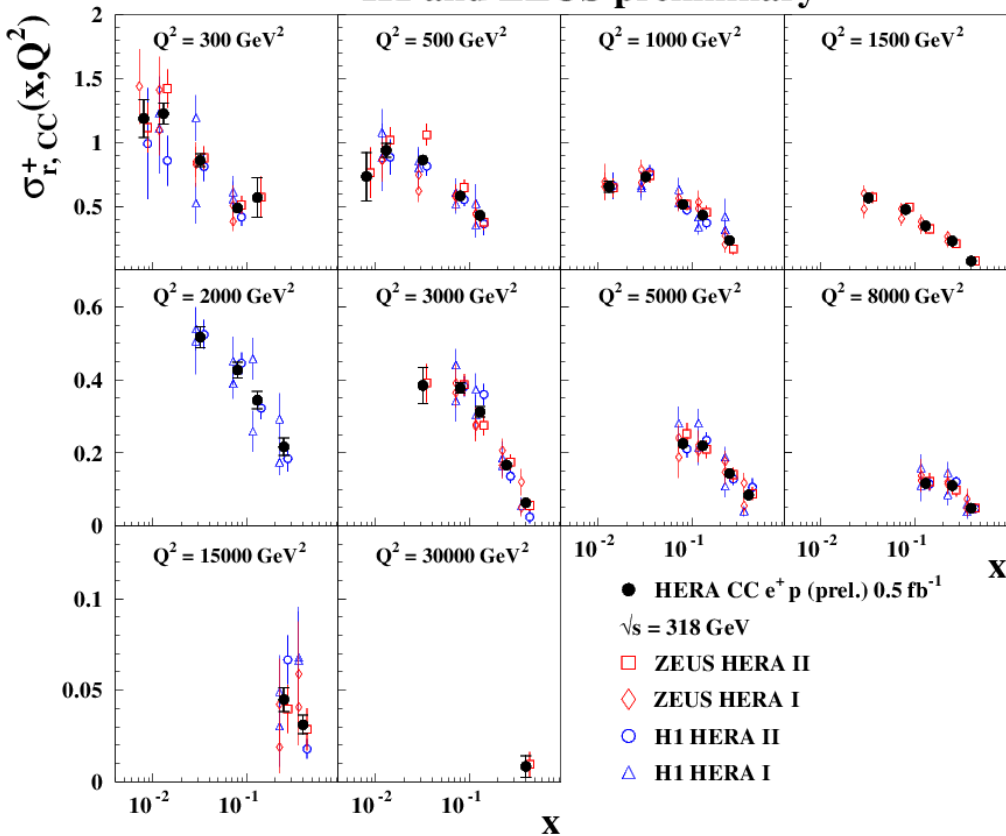
# Averaged Cross Sections : CC ep

CC e<sup>+</sup>p

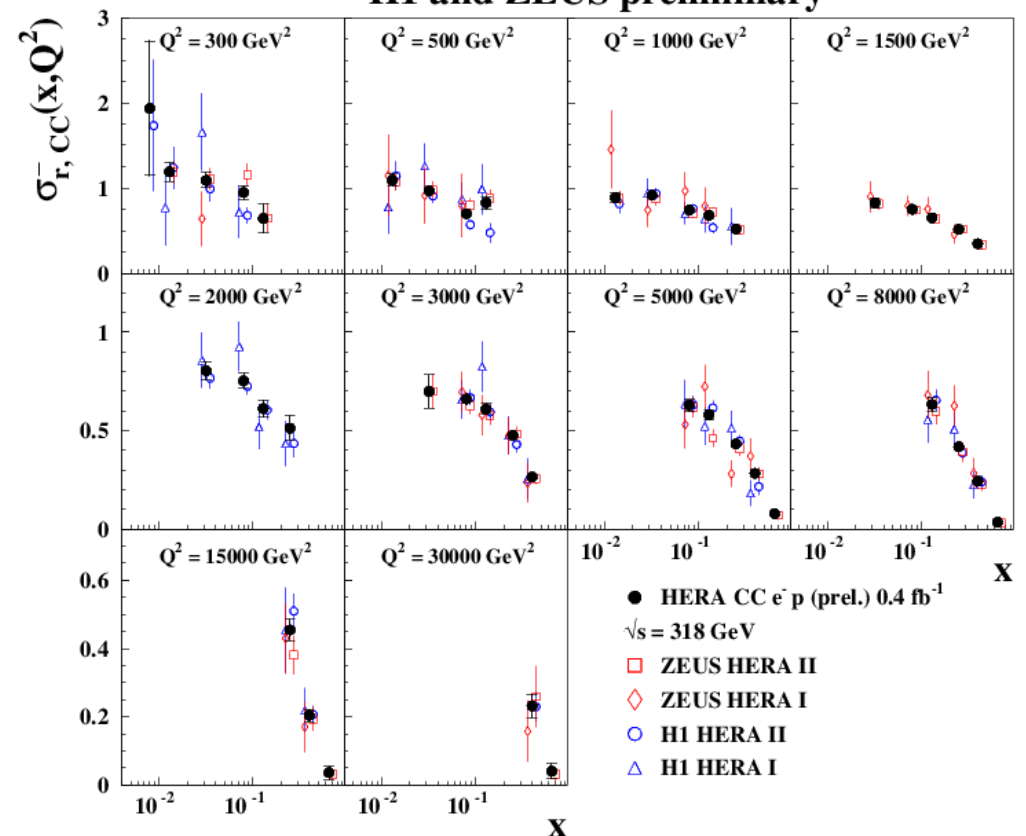


CC e<sup>-</sup>p

H1 and ZEUS preliminary



H1 and ZEUS preliminary



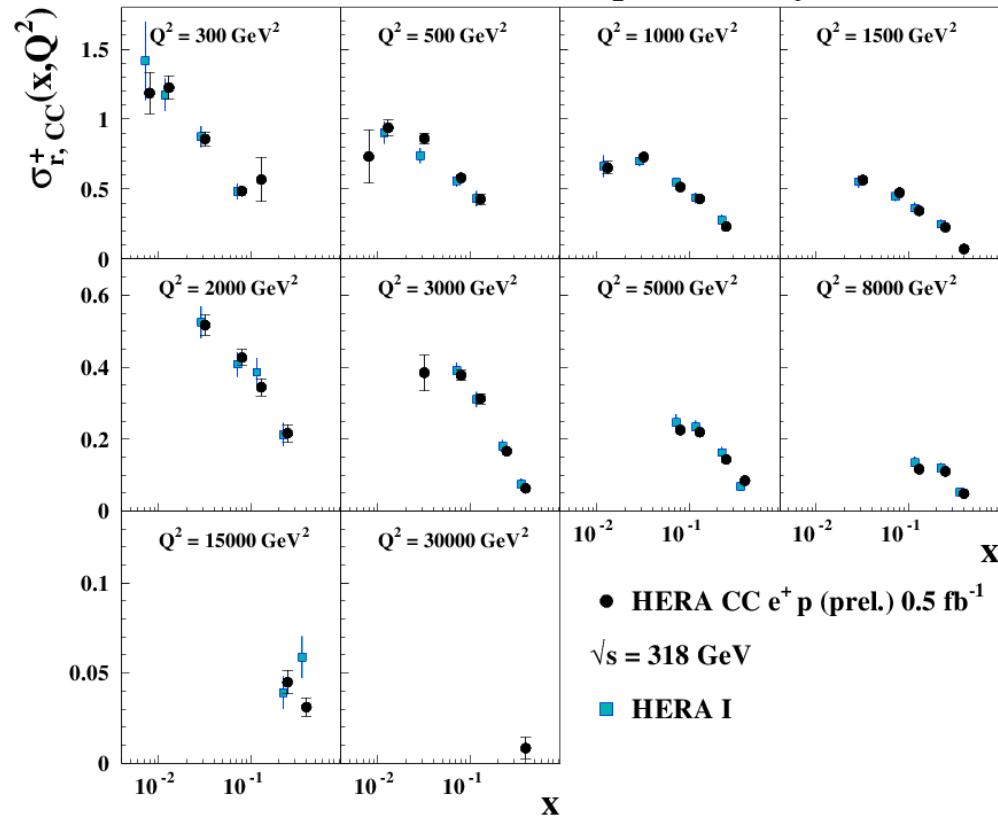
Many points are combined into one data point

# Averaged Cross Sections : CC ep

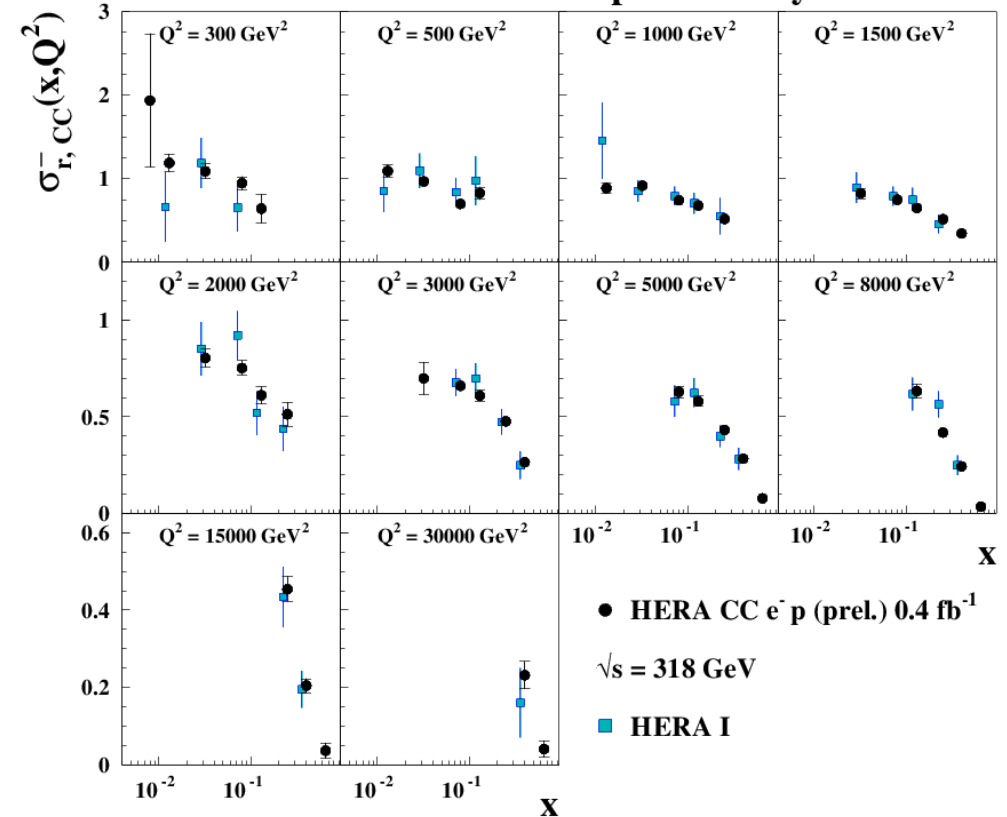
## CC e<sup>+</sup>p

## CC e<sup>-</sup>p

H1 and ZEUS preliminary



H1 and ZEUS preliminary



In comparison to  
HERA I luminosity :

x 3

x 10

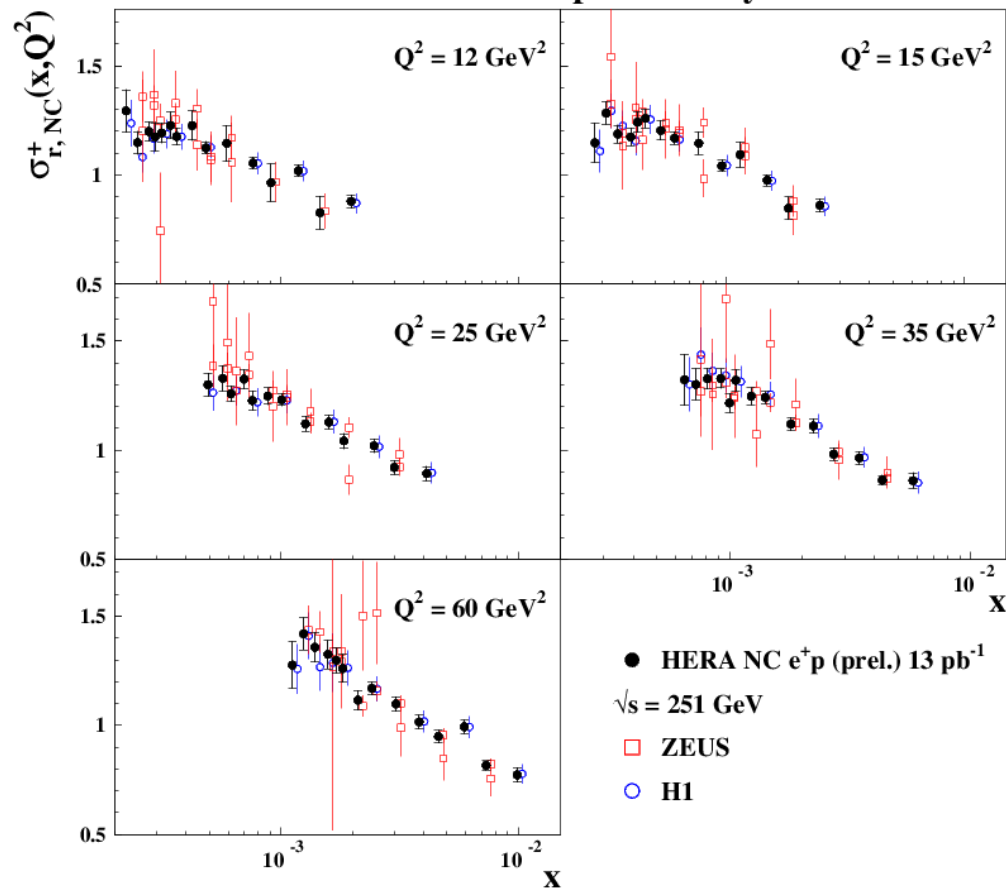
New data points, especially at high x

# Averaged Cross Sections : NC $e^+p$

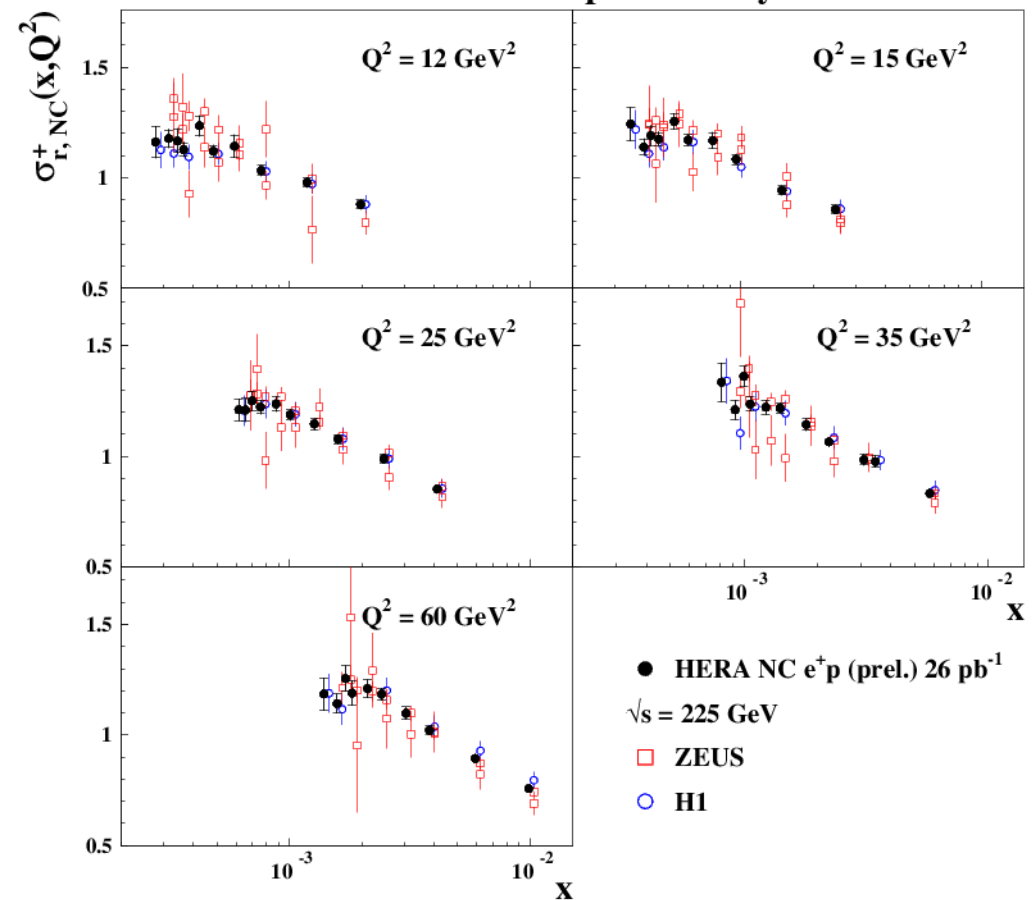
$$E_p = 575 \text{ GeV}$$

$$E_p = 460 \text{ GeV}$$

H1 and ZEUS preliminary



H1 and ZEUS preliminary

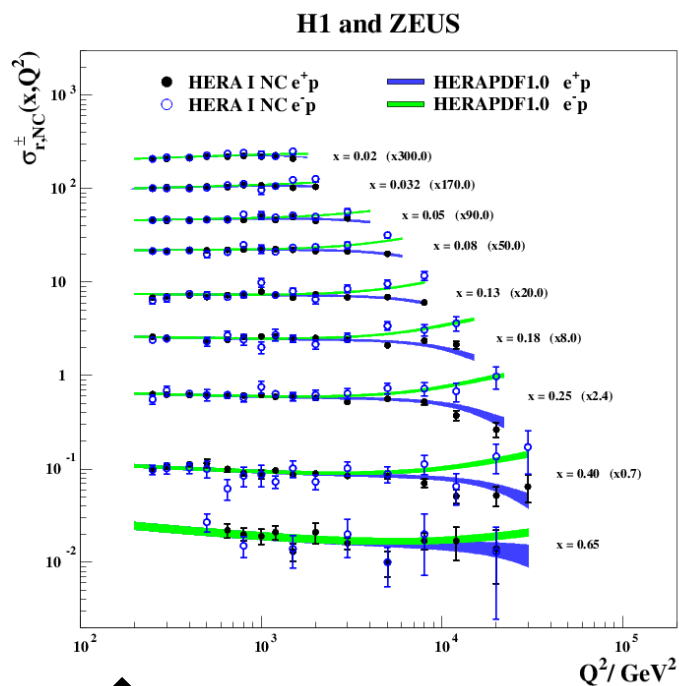


New proton beam energies data samples included

# Summary

- ◆ Combination of all final inclusive deep inelastic cross sections measured by the H1 and ZEUS collaborations have been calculated.
- ◆ The total luminosity of about  $1 \text{ fb}^{-1}$  collected by two separate experiments provides us with cross sections of very high precision.
- ◆ Combined HERA I+II data used as an input in QCD analysis

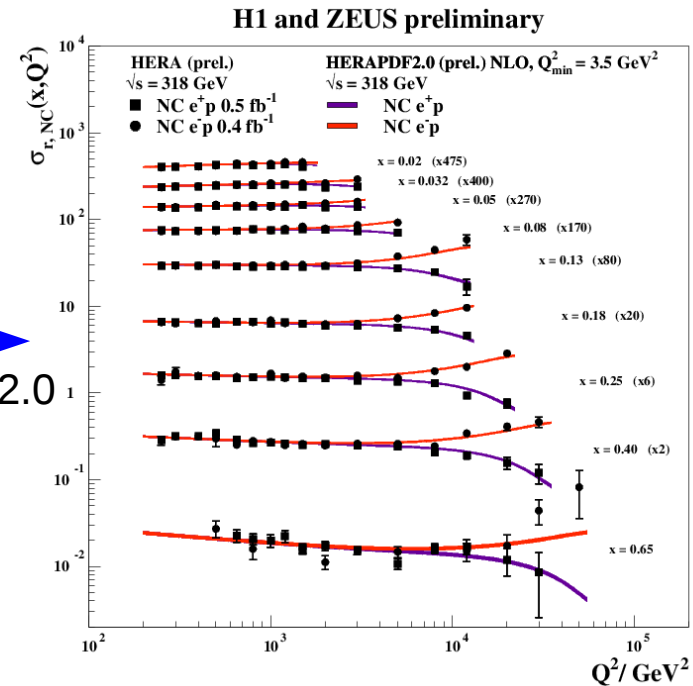
➔ see V. Radescu talk.



HERAPDF 1.0

➔

HERAPDF 2.0



# Data Samples

H1

ZEUS

Data set		$\mathcal{L}$ [pb <sup>-1</sup> ]	e <sup>+</sup> / e <sup>-</sup>	$\sqrt{s}$ [GeV]	Data set		$\mathcal{L}$ [pb <sup>-1</sup> ]	e <sup>+</sup> / e <sup>-</sup>	$\sqrt{s}$ [GeV]
HERA I $E_p = 820$ GeV and $E_p = 920$ GeV data sets									
H1 svx-mb	95-00	2.1	e <sup>+</sup> p	301, 319	ZEUS BPC	95	1.65	e <sup>+</sup> p	300
H1 low Q <sup>2</sup>	96-00	22	e <sup>+</sup> p	301,319	ZEUS BPT	97	3.9	e <sup>+</sup> p	300
H1 NC	94-97	35.6	e <sup>+</sup> p	301	ZEUS SVX	95	0.2	e <sup>+</sup> p	300
H1 CC	94-97	35.6	e <sup>+</sup> p	301	ZEUS NC	96-97	30.0	e <sup>+</sup> p	300
H1 NC	98-99	16.4	e <sup>-</sup> p	319	ZEUS CC	94-97	47.7	e <sup>+</sup> p	300
H1 CC	98-99	16.4	e <sup>-</sup> p	319	ZEUS NC	98-99	15.9	e <sup>-</sup> p	318
H1 NC HY	98-99	16.4	e <sup>-</sup> p	319	ZEUS CC	98-99	16.4	e <sup>-</sup> p	318
H1 NC	99-00	65.2	e <sup>+</sup> p	319	ZEUS NC	99-00	63.2	e <sup>+</sup> p	318
H1 CC	99-00	65.2	e <sup>+</sup> p	319	ZEUS CC	99-00	60.9	e <sup>+</sup> p	318
HERA II $E_p = 920$ GeV data sets									
H1 NC	03-07	182.0	e <sup>+</sup> p	319	ZEUS NC	06-07	135.5	e <sup>+</sup> p	318
H1 CC	03-07	182.0	e <sup>+</sup> p	319	ZEUS CC	06-07	132.0	e <sup>+</sup> p	318
H1 NC	03-07	151.7	e <sup>-</sup> p	319	ZEUS NC	05-06	169.9	e <sup>-</sup> p	318
H1 CC	03-07	151.7	e <sup>-</sup> p	319	ZEUS CC	04-06	175.0	e <sup>-</sup> p	318
H1 NC med Q <sup>2</sup>	03-07	97.6	e <sup>+</sup> p	319	ZEUS NC nominal	06-07	44.5	e <sup>+</sup> p	318
H1 NC low Q <sup>2</sup>	03-07	5.9	e <sup>+</sup> p	319	ZEUS NC satellite	06-07	44.5	e <sup>+</sup> p	318
HERA II $E_p = 575$ GeV data sets									
H1 NC high Q <sup>2</sup>	07	5.4	e <sup>+</sup> p	252	ZEUS NC nominal	07	7.1	e <sup>+</sup> p	251
H1 NC low Q <sup>2</sup>	07	5.9	e <sup>+</sup> p	252	ZEUS NC satellite	07	7.1	e <sup>+</sup> p	251
HERA II $E_p = 460$ GeV data sets									
H1 NC high Q <sup>2</sup>	07	11.8	e <sup>+</sup> p	225	ZEUS NC nominal	07	13.9	e <sup>+</sup> p	225
H1 NC low Q <sup>2</sup>	07	12.2	e <sup>+</sup> p	225	ZEUS NC satellite	07	13.9	e <sup>+</sup> p	225