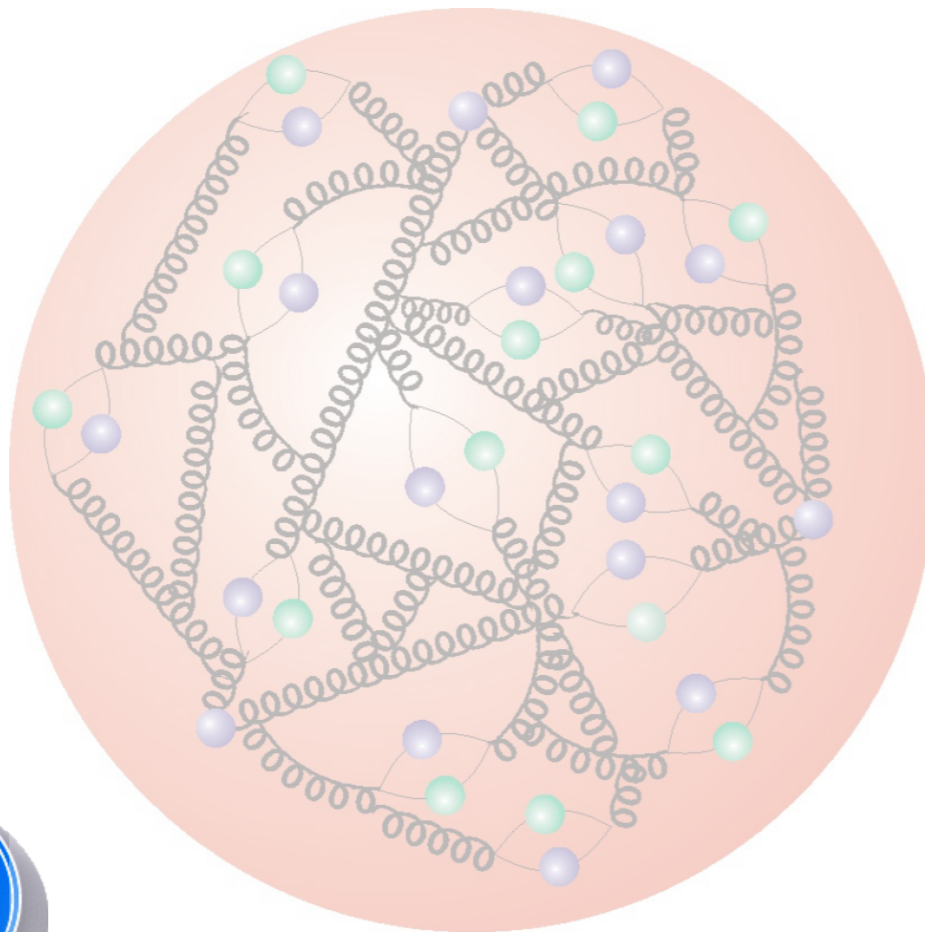


Inclusive DIS at HERA & PDF Fits



- Introduction
- HERA-II Data Sets
- Combination Procedure
- Combined Data Precision
- HERAPDF 2.0



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25th-29th August 2014



$$\frac{d\sigma_{NC}^{\pm}}{dx dQ^2} = \frac{2\pi\alpha^2}{x} \left[\frac{1}{Q^2} \right]^2 \left[Y_+ \tilde{F}_2 \mp Y_- x \tilde{F}_3 - y^2 \tilde{F}_L \right]$$

$$\frac{d\sigma_{CC}^{\pm}}{dx dQ^2} = \frac{G_F^2}{4\pi x} \left[\frac{M_W^2}{M_W^2 + Q^2} \right]^2 \left[Y_+ \tilde{W}_2^{\pm} \mp Y_- x \tilde{W}_3^{\pm} - y^2 \tilde{W}_L^{\pm} \right]$$

$$Y_{\pm} = 1 \pm (1-y)^2$$

$$\tilde{F}_2 \propto \sum (xq_i + x\bar{q}_i)$$

Dominant contribution

$$x\tilde{F}_3 \propto \sum (xq_i - x\bar{q}_i)$$

Only sensitive at high $Q^2 \sim M_Z^2$

$$\tilde{F}_L \propto \alpha_s \cdot xg(x, Q^2)$$

Only sensitive at low Q^2 and high y

The NC reduced cross section defined as:

$$\tilde{\sigma}_{NC}^{\pm} = \frac{Q^2 x}{2\alpha\pi^2} \frac{1}{Y_+} \frac{d^2\sigma^{\pm}}{dx dQ^2}$$

$$\tilde{\sigma}_{NC}^{\pm} \sim \tilde{F}_2 \mp \frac{Y_-}{Y_+} x\tilde{F}_3$$

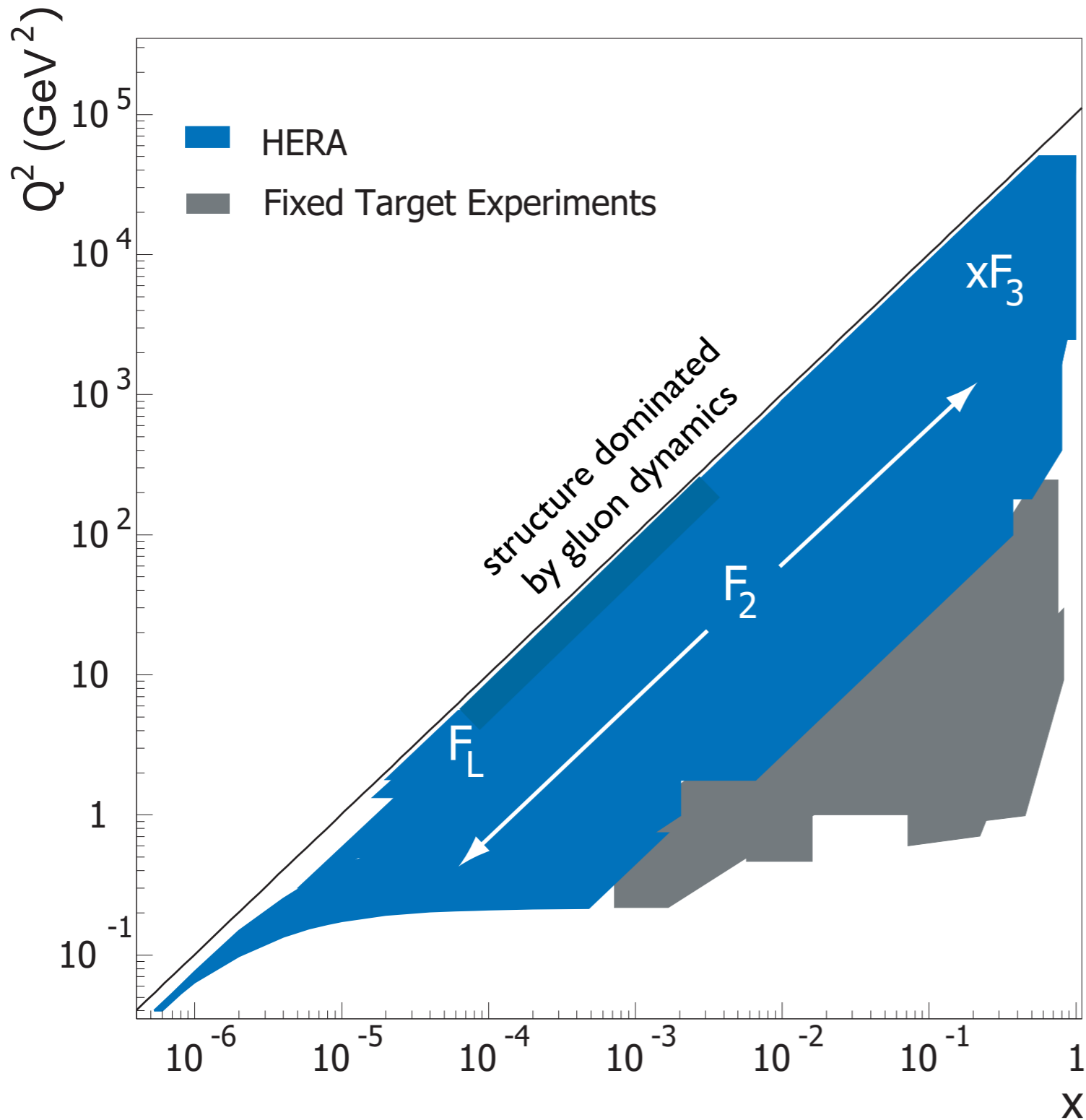
The CC reduced cross section defined as:

$$\sigma_{CC}^{\pm} = \frac{2\pi x}{G_F^2} \left[\frac{M_W^2 + Q^2}{M_W^2} \right]^2 \frac{d\sigma_{CC}^{\pm}}{dx dQ^2}$$

$$\frac{d\sigma_{CC}^{\pm}}{dx dQ^2} = \frac{1}{2} \left[Y_+ W_2^{\pm} \mp Y_- x W_3^{\pm} - y^2 W_L^{\pm} \right]$$

similarly for pure weak CC analogues:

$$W_2^{\pm}, xW_3^{\pm} \text{ and } W_L^{\pm}$$



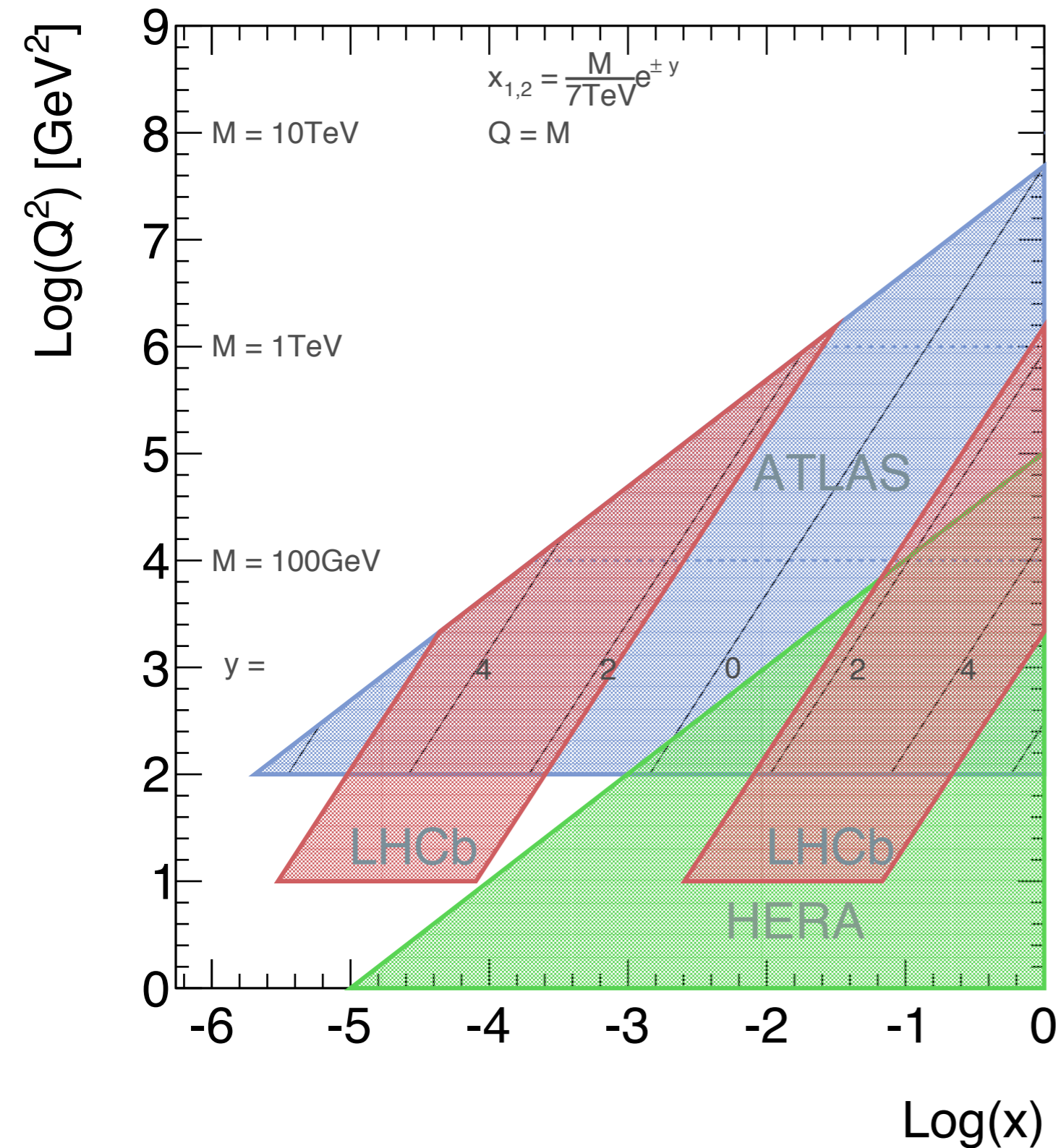
HERA data cover wide region of x, Q^2

NC Measurements

F_2 dominates most of Q^2 reach
 xF_3 contributes in EW regime
 F_L contributes only at highest y

CC Measurements

W_2 and xW_3 contribute equally
 W_L only at high y



LHC: largest mass states at large x

For central production $x=x_1=x_2$

$$M = x\sqrt{s}$$

i.e. $M > 1\text{TeV}$ probes $x > 0.1$

Searches for high mass states require precision knowledge at high x

Z' / quantum gravity / susy searches...

DGLAP evolution allows predictions to be made

High x predictions rely on

- data (DIS / fixed target)
- sum rules
- behaviour of PDFs as $x \rightarrow 1$

HERA-I operation 1993-2000

$E_e = 27.6 \text{ GeV}$

$E_p = 820 / 920 \text{ GeV}$

$\int \mathcal{L} \sim 110 \text{ pb}^{-1}$ per experiment

HERA-II operation 2003-2007

$E_e = 27.6 \text{ GeV}$

$E_p = 920 \text{ GeV}$

$\int \mathcal{L} \sim 330 \text{ pb}^{-1}$ per experiment

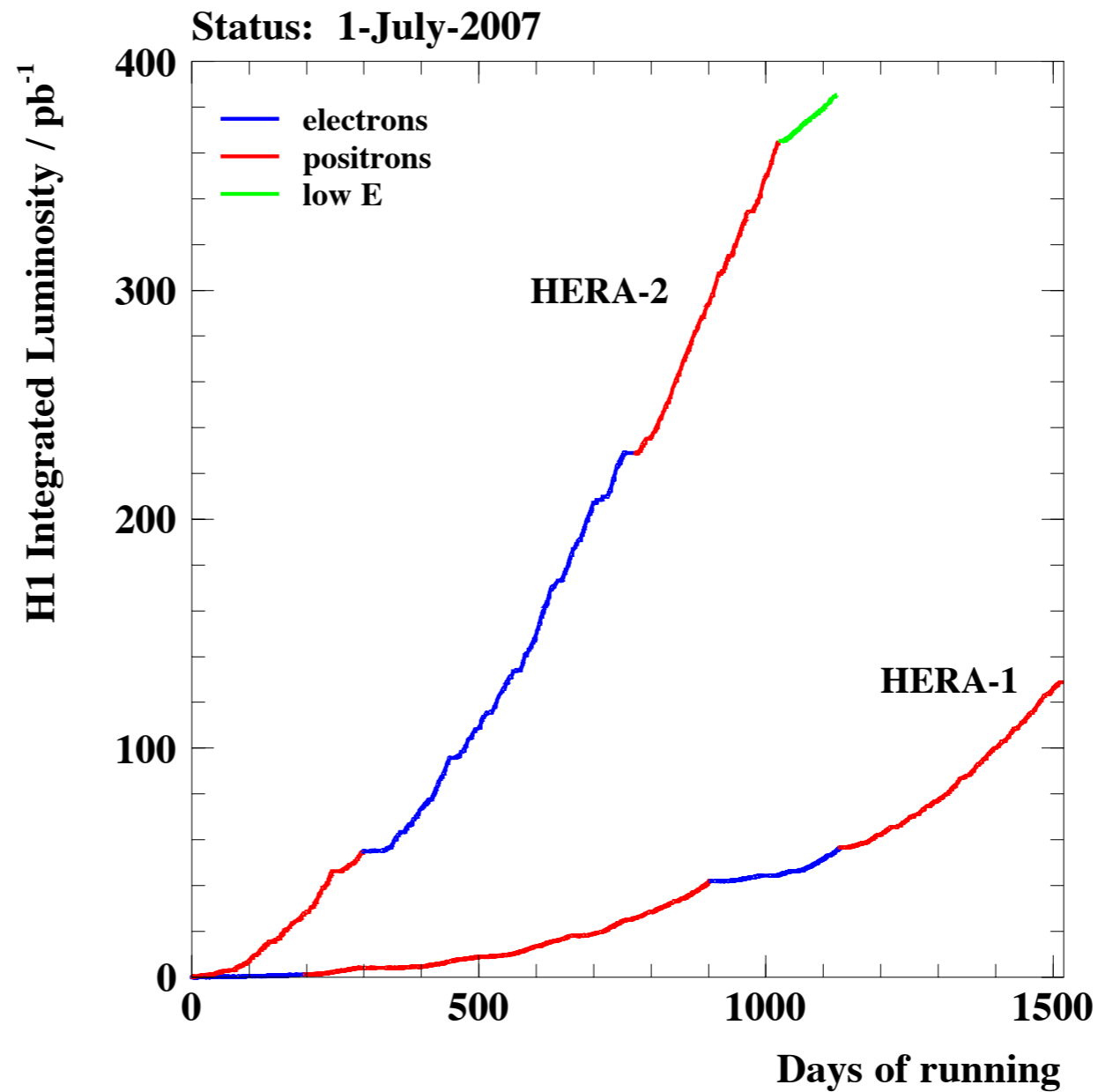
Longitudinally polarised leptons

Low Energy Run 2007

$E_e = 27.6 \text{ GeV}$

$E_p = 575 \text{ \& } 460 \text{ GeV}$

Dedicated F_L measurement





Summary of HERA-I datasets Combined in HERAPDF1.0

Available since 2009

Data Set		x Range		Q^2 Range GeV ²		\mathcal{L} pb ⁻¹	e^+/e^-	\sqrt{s} GeV
H1 svx-mb	95-00	5×10^{-6}	0.02	0.2	12	2.1	$e^+ p$	301-319
H1 low Q^2	96-00	2×10^{-4}	0.1	12	150	22	$e^+ p$	301-319
H1 NC	94-97	0.0032	0.65	150	30000	35.6	$e^+ p$	301
H1 CC	94-97	0.013	0.40	300	15000	35.6	$e^+ p$	301
H1 NC	98-99	0.0032	0.65	150	30000	16.4	$e^- p$	319
H1 CC	98-99	0.013	0.40	300	15000	16.4	$e^- p$	319
H1 NC HY	98-99	0.0013	0.01	100	800	16.4	$e^- p$	319
H1 NC	99-00	0.0013	0.65	100	30000	65.2	$e^+ p$	319
H1 CC	99-00	0.013	0.40	300	15000	65.2	$e^+ p$	319
ZEUS BPC	95	2×10^{-6}	6×10^{-5}	0.11	0.65	1.65	$e^+ p$	301
ZEUS BPT	97	6×10^{-7}	0.001	0.045	0.65	3.9	$e^+ p$	301
ZEUS SVX	95	1.2×10^{-5}	0.0019	0.6	17	0.2	$e^+ p$	301
ZEUS NC	96-97	6×10^{-5}	0.65	2.7	30000	30.0	$e^+ p$	301
ZEUS CC	94-97	0.015	0.42	280	17000	47.7	$e^+ p$	301
ZEUS NC	98-99	0.005	0.65	200	30000	15.9	$e^- p$	319
ZEUS CC	98-99	0.015	0.42	280	30000	16.4	$e^- p$	319
ZEUS NC	99-00	0.005	0.65	200	30000	63.2	$e^+ p$	319
ZEUS CC	99-00	0.008	0.42	280	17000	60.9	$e^+ p$	319

High Q^2 NC and CC data limited to
100 pb⁻¹ $e^+ p$
16 pb⁻¹ $e^- p$

HERA Structure Function Data



Data Set	x Grid		Q^2/GeV^2 Grid		\mathcal{L}	e^+/e^-	\sqrt{s}	x, Q^2 from	Ref.	
	from	to	from	to	pb^{-1}		GeV	equations		
HERA I $E_p = 820 \text{ GeV}$ and $E_p = 920 \text{ GeV}$ data sets										
H1 svx-mb	95-00	0.000005	0.02	0.2	12	2.1	e^+p	301, 319	11,15,16	[2]
H1 low Q^2	96-00	0.0002	0.1	12	150	22	e^+p	301, 319	11,15,16	[3]
H1 NC	94-97	0.0032	0.65	150	30000	35.6	e^+p	301	17	[4]
H1 CC	94-97	0.013	0.40	300	15000	35.6	e^+p	301	12	[4]
H1 NC	98-99	0.0032	0.65	150	30000	16.4	e^-p	319	17	[5]
H1 CC	98-99	0.013	0.40	300	15000	16.4	e^-p	319	12	[5]
H1 NC HY	98-99	0.0013	0.01	100	800	16.4	e^-p	319	11	[6]
H1 NC	99-00	0.0013	0.65	100	30000	65.2	e^+p	319	17	[6]
H1 CC	99-00	0.013	0.40	300	15000	65.2	e^+p	319	12	[6]
ZEUS BPC	95	0.000002	0.00006	0.11	0.65	1.65	e^+p	300	11	[10]
ZEUS BPT	97	0.0000006	0.001	0.045	0.65	3.9	e^+p	300	11, 17	[11]
ZEUS SVX	95	0.000012	0.0019	0.6	17	0.2	e^+p	300	11	[12]
ZEUS NC	96-97	0.00006	0.65	2.7	30000	30.0	e^+p	300	19	[13]
ZEUS CC	94-97	0.015	0.42	280	17000	47.7	e^+p	300	12	[14]
ZEUS NC	98-99	0.005	0.65	200	30000	15.9	e^-p	318	18	[15]
ZEUS CC	98-99	0.015	0.42	280	30000	16.4	e^-p	318	12	[16]
ZEUS NC	99-00	0.005	0.65	200	30000	63.2	e^+p	318	18	[17]
ZEUS CC	99-00	0.008	0.42	280	17000	60.9	e^+p	318	12	[18]
HERA II $E_p = 920 \text{ GeV}$ data sets										
H1 NC	03-07	0.0008	0.65	60	30000	182	e^+p	319	11, 17	[7] ¹
H1 CC	03-07	0.008	0.40	300	15000	182	e^+p	319	12	[7] ¹
H1 NC	03-07	0.0008	0.65	60	50000	151.7	e^-p	319	11, 17	[7] ¹
H1 CC	03-07	0.008	0.40	300	30000	151.7	e^-p	319	12	[7] ¹
H1 NC med Q^2 ^{*y.5}	03-07	0.0000986	0.005	8.5	90	97.6	e^+p	319	11	[9]
H1 NC low Q^2 ^{*y.5}	03-07	0.000029	0.00032	2.5	12	5.9	e^+p	319	11	[9]
ZEUS NC	06-07	0.005	0.65	200	30000	135.5	e^+p	318	11,12,18	[21]
ZEUS CC	06-07	0.0078	0.42	280	30000	132	e^+p	318	12	[22]
ZEUS NC	05-06	0.005	0.65	200	30000	169.9	e^-p	318	18	[19]
ZEUS CC	04-06	0.015	0.65	280	30000	175	e^-p	318	12	[20]
ZEUS NC nominal ^{*y}	06-07	0.000092	0.008343	7	110	44.5	e^+p	318	11	[23]
ZEUS NC satellite ^{*y}	06-07	0.000071	0.008343	5	110	44.5	e^+p	318	11	[23]
HERA II $E_p = 575 \text{ GeV}$ data sets										
H1 NC high Q^2	07	0.00065	0.65	35	800	5.4	e^+p	252	11, 17	[8]
H1 NC low Q^2	07	0.0000279	0.0148	1.5	90	5.9	e^+p	252	11	[9]
ZEUS NC nominal	07	0.000147	0.013349	7	110	7.1	e^+p	251	11	[23]
ZEUS NC satellite	07	0.000125	0.013349	5	110	7.1	e^+p	251	11	[23]
HERA II $E_p = 460 \text{ GeV}$ data sets										
H1 NC high Q^2	07	0.00081	0.65	35	800	11.8	e^+p	225	11, 17	[8]
H1 NC low Q^2	07	0.0000348	0.0148	1.5	90	12.2	e^+p	225	11	[9]
ZEUS NC nominal	07	0.000184	0.016686	7	110	13.9	e^+p	225	11	[23]
ZEUS NC satellite	07	0.000143	0.016686	5	110	13.9	e^+p	225	11	[23]

HI & ZEUS have now published all datasets

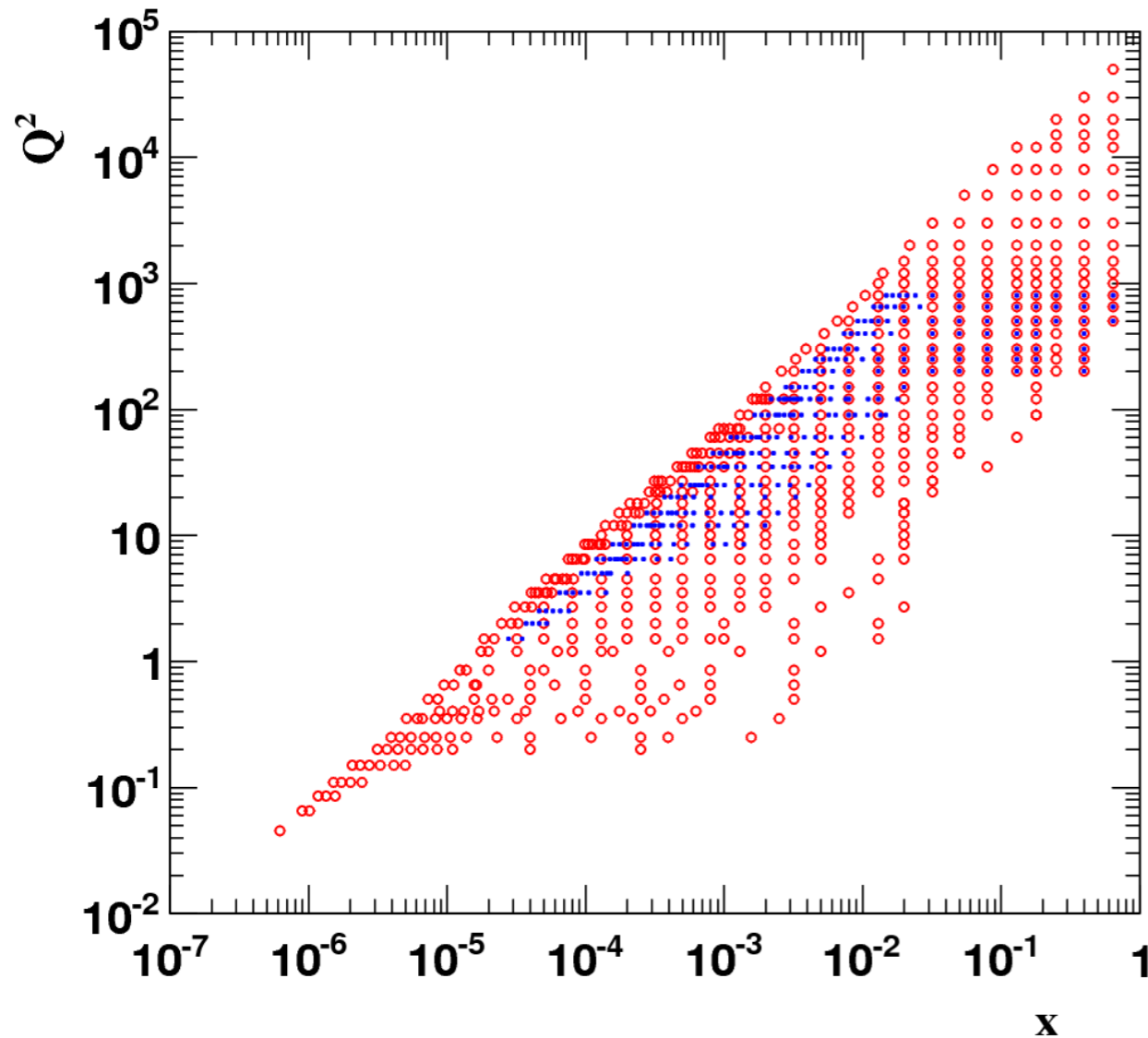
- HERA-II measurements at high $\int \mathcal{L}$
- reduced \sqrt{s} data

41 data sets to be combined:

- NC & CC cross sections
- e^+p and e^-p scattering
- 4 different \sqrt{s} values

2927 data points in total

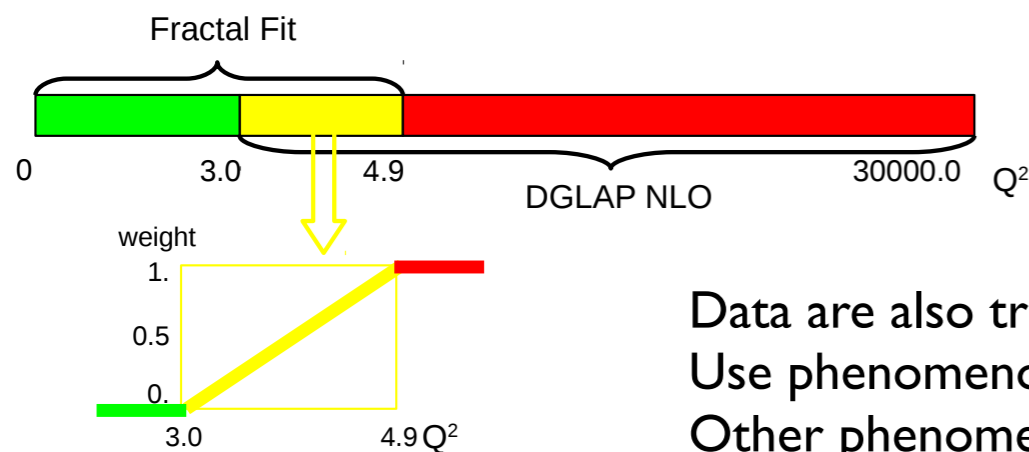
In some cases 6 measurements combined



Data are combined onto a common x, Q^2 grid
 Two grids used:
 inclusive measurements $\sqrt{s}=301$ & 319 GeV
 fine x grid for $\sqrt{s}=575$ & 460 GeV

2927 data points \rightarrow 1307 combined measurements

Data are translated to nearest x, Q^2 grid point
 Iterative process using NLO QCD fit to data
 Use uncombined data in first iteration
 Then combined data in later iterations
 No changes after 3 iterations



$$\sigma(x_{grid}, Q_{grid}^2) = \frac{\sigma_{model}(x_{grid}, Q_{grid}^2)}{\sigma_{model}(x_{meas}, Q_{meas}^2)} \cdot \sigma_{meas}(x_{meas}, Q_{meas}^2)$$

Data are also translated outside of region of DGLAP fit validity $Q^2 < 3.0$ GeV²
 Use phenomenological “fractal” model and interpolate to DGLAP region
 Other phenomenological fits tested \rightarrow negligible differences

i data points
 j systematic error sources

Correlated uncertainties treated multiplicative: size proportional to central averaged value
 True for normalisation uncertainties
 Perhaps not true for other uncertainties

$$\chi_{tot}^2(\mathbf{m}, \mathbf{b}) = \sum_i \frac{[\mu^i - m^i(1 - \sum_j \gamma_j^i b_j)]^2}{\delta_{i,stat}^2 \mu^i m^i (1 - \sum_j \gamma_j^i b_j) + (\delta_{i,unc} m^i)^2} + \sum_j b_j^2$$

μ^i = measurement

m^i = averaged value

γ_j^i = correlated relative (%) sys uncertainty on point i from error source j

b_j = systematic error source strength

nuisance parameter left free in fit but constrained
 no extra degrees of freedom due to additional constraint

For HERAPDF2.0 number of correlated error sources $j = 162$

These include:

- b/g uncertainty
- luminosity uncertainty
- EM calibration scale
- had calibration scale
- etc....

Extra procedural uncertainty included:
 difference between using
 additive vs multiplicative
 correlated uncertainties (except normalisation)
 ⇒ extra ~0.5% uncertainty

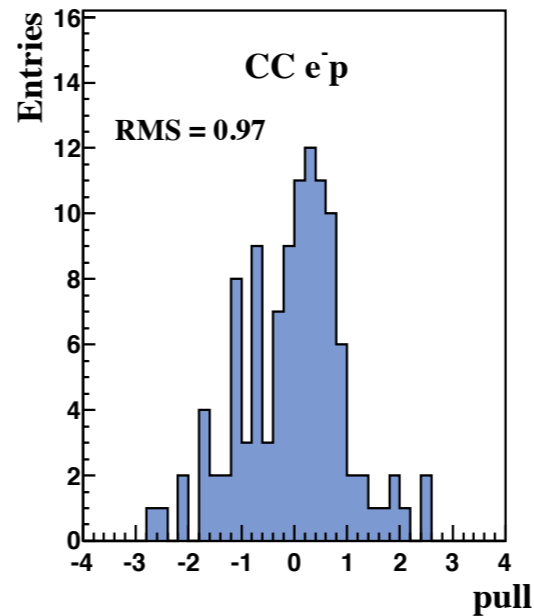
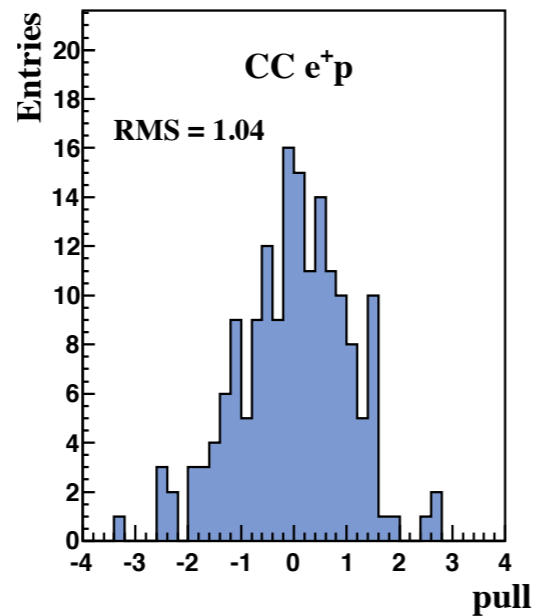
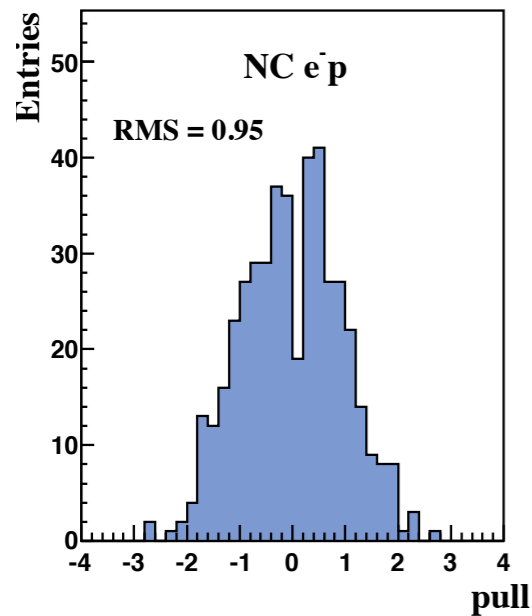
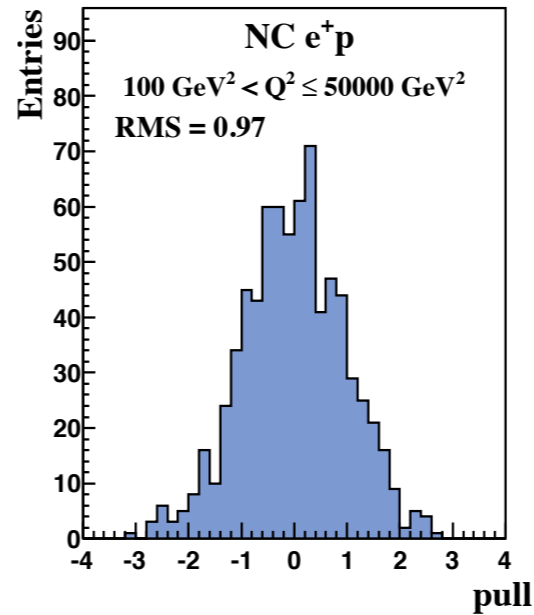
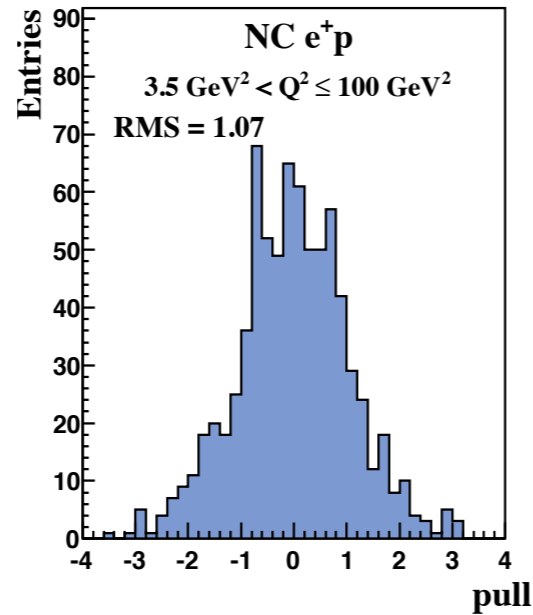
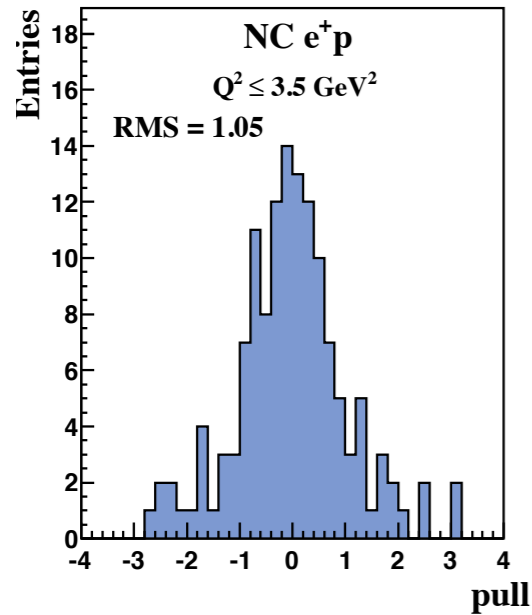
Are correlated point-to-point within a single measurement

Reported in detail in individual publications from experiments

May also be correlated across measurements

May also be correlated between H1 & ZEUS (e.g. had scale & photoproduction b/g)

H1 and ZEUS preliminary



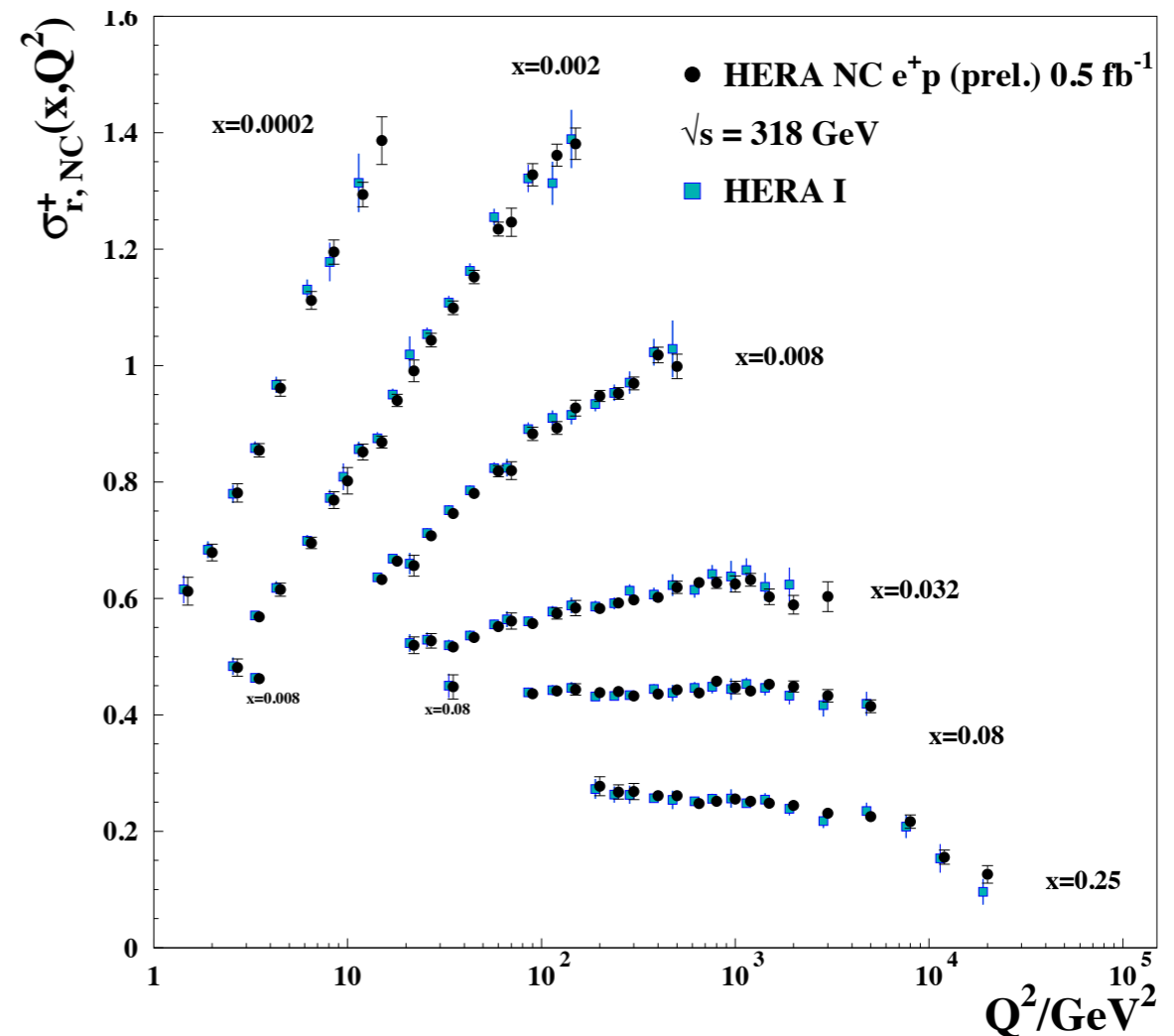
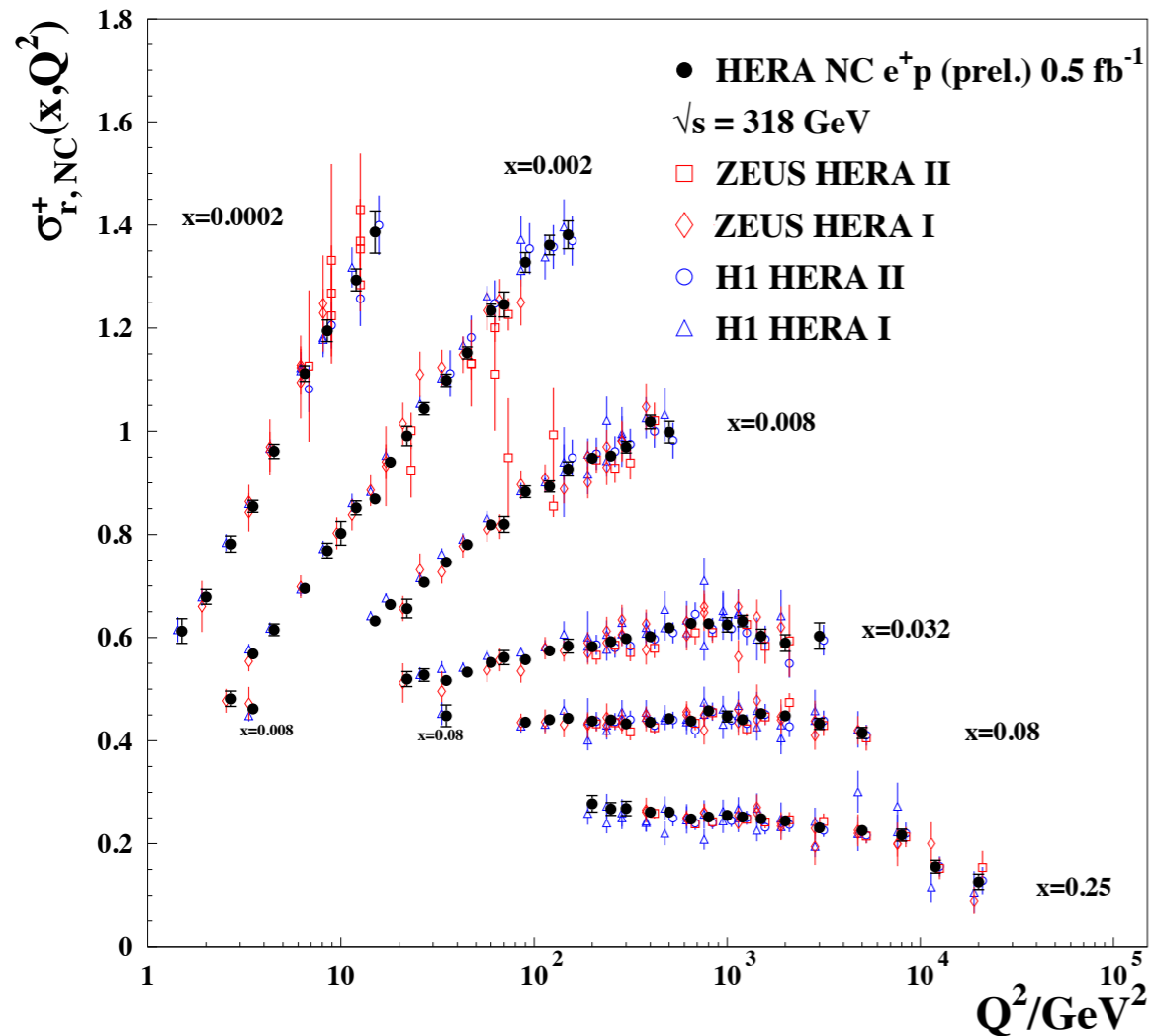
Overall $\chi^2/\text{ndf} = 1685 / 1620 = 1.04$

Pulls defined for each measurement difference between measured & average values after applying sys shifts b_j in units of uncorrelated uncertainty

Pulls of the data points should be distributed as a unit Gaussian

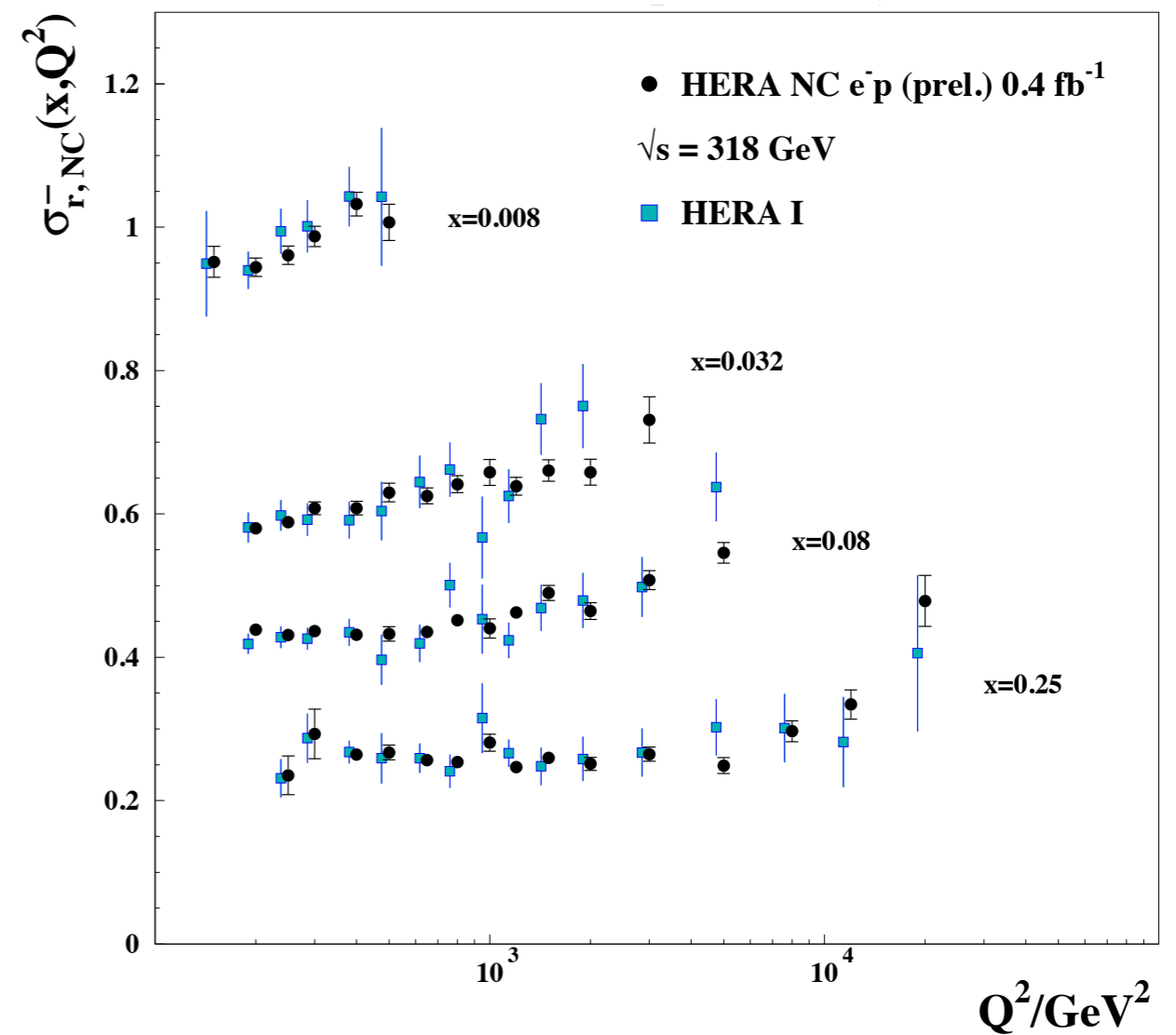
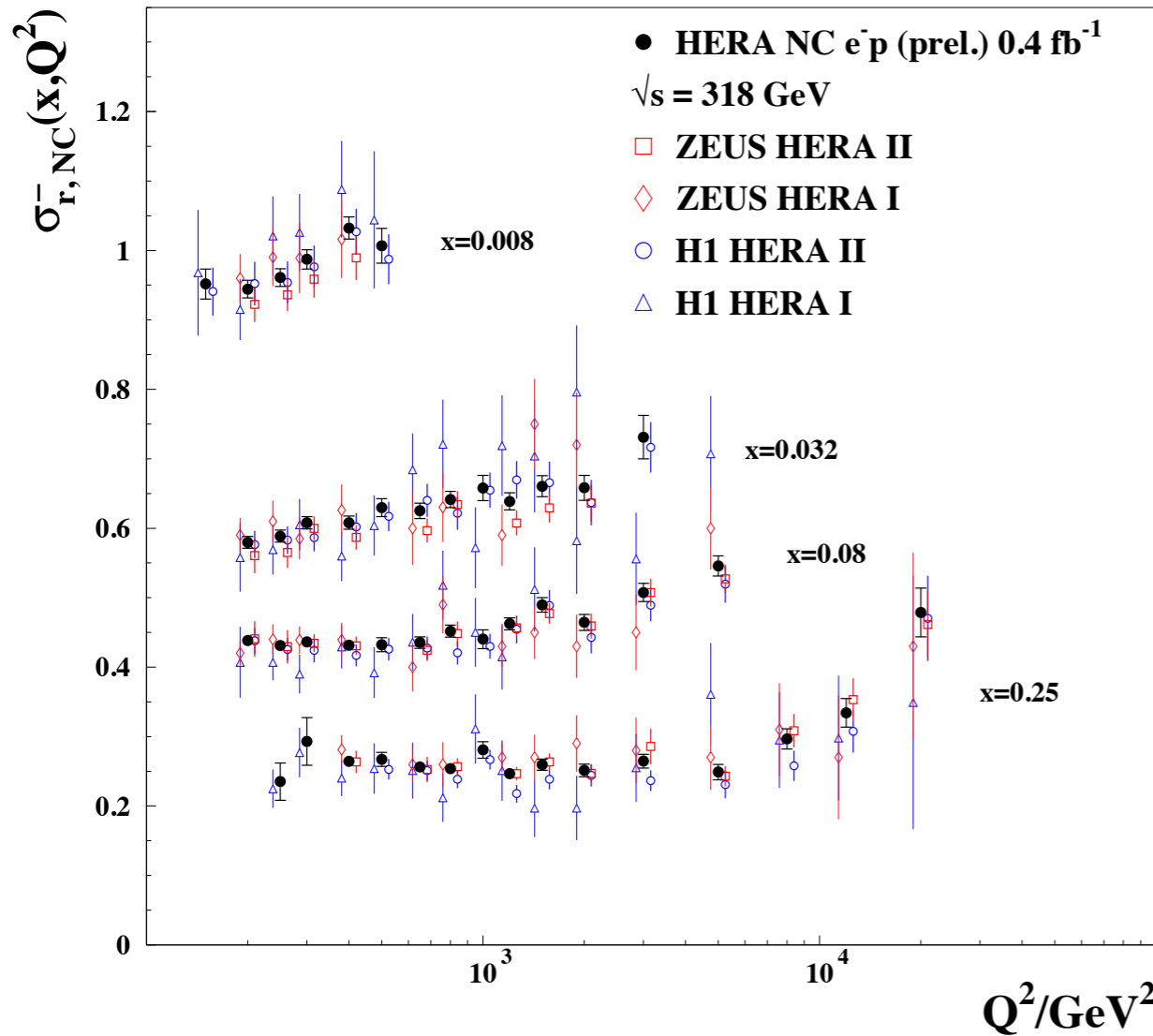
Each measurement channel shows pull centred on zero & unit width

NC e^+p inclusive cross sections



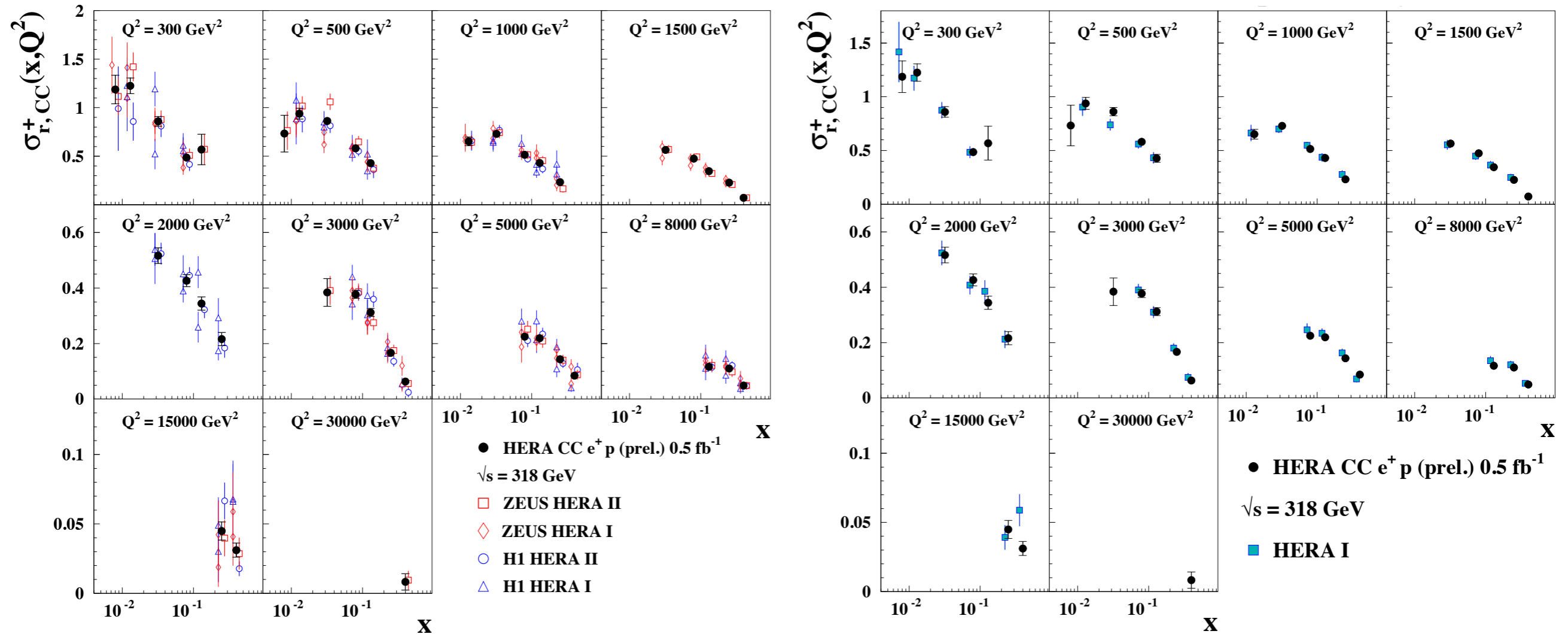
Significant improvement in NC uncertainties for $Q^2 > 100 \text{ GeV}^2$ for $\sqrt{s}=318 \text{ GeV}$
 Compared to HERA I combination: factor 3 increase in statistical precision
 stat error $< 0.9\%$ for Q^2 up to 400 GeV^2
 total error $< 1.3\%$ for Q^2 up to 400 GeV^2

NC e^-p inclusive cross sections



Significant improvement in NC uncertainties for $Q^2 > 100 \text{ GeV}^2$ for $\sqrt{s}=318 \text{ GeV}$
 Compared to HERA I combination: factor 10 increase in statistical precision
 stat error $< 0.9\%$ for Q^2 up to 400 GeV^2
 total error $< 1.6\%$ for Q^2 up to 400 GeV^2

CC e^+p inclusive cross sections



At high x the CC e^+p cross sections provide direct clean access to the xd density

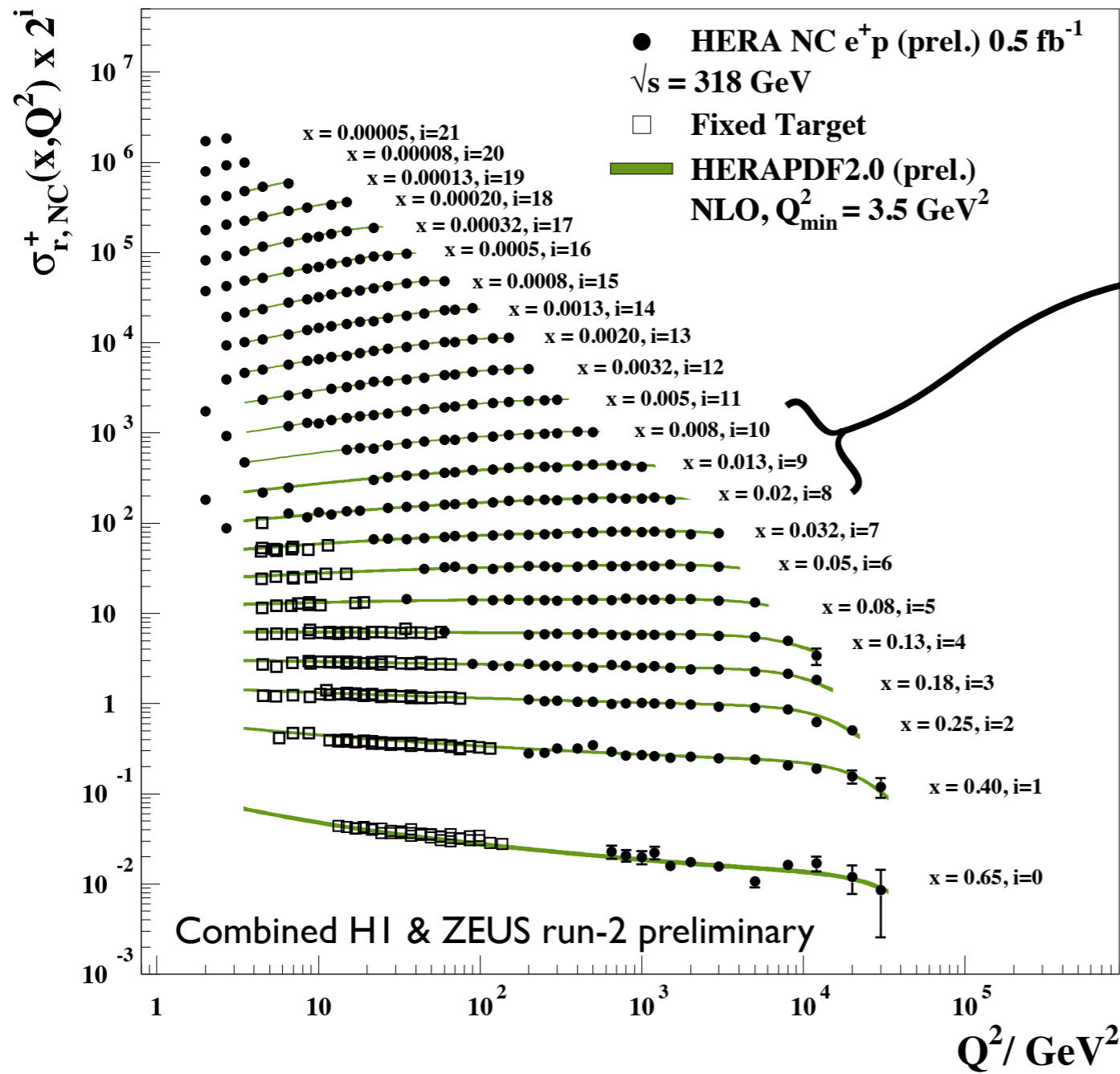
Compared to HERA I combination: factor 3 increase in statistical precision

HERAPDF1.0 combination total error $\sim 10\text{-}20\%$

HERAPDF2.0 combination total error $\sim 5\text{-}10\%$

up to $x \sim 0.25$

Dominated by statistical precision



$x \sim 10^{-2}$ is a sweet-spot
 high precision with long Q^2 lever arm
 relevant for LHC Higgs production

Precision:
 1.2% $Q^2 < 60 \text{ GeV}^2$
 1.3% $Q^2 < 400 \text{ GeV}^2$
 2% $Q^2 < 1200 \text{ GeV}^2$



HERAPDF1.0

Combine NC and CC HERA-I data from H1 & ZEUS
Complete MSbar NLO fit
NLO: standard parameterisation with 10 parameters
 $\alpha_s = 0.1176$ (fixed in fit)

HERAPDF1.5

Include additional NC and CC HERA-II data
Complete MSbar NLO and NNLO fit
NLO: standard parameterisation with 10 parameters

HERAPDF1.5f

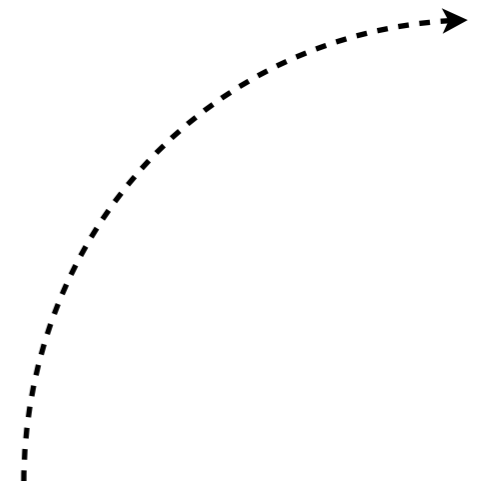
NNLO: extended fit with 14 parameters

HERAPDF1.6

Include additional NC inclusive jet data $5 < Q^2 < 15000$
Complete MSbar NLO fit
NLO: standard parameterisation with 14 parameters
 $\alpha_s = 0.1202 \pm 0.0013$ (exp) ± 0.004 (scales) free in fit

HERAPDF1.7

Include 41 additional F_2^{cc} data $4 < Q^2 < 1000$
Include 224 combined cross section points $E_p=575/460$ GeV
Complete MSbar NLO fit
NLO: standard parameterisation with 14 parameters



HERAPDF2.0

Include final:

HERA-I low/medium Q^2 precision F_2

HERA-II high Q^2 NC/CC data

HERA-II low/medium energy NC data

NLO & NNLO fits

Final structure function measurements from H1 / ZEUS now published

Combination of the data is underway

New combination will include:

HERA-I published data

HERA-II published data

low/medium energy $E_p=575/460$ GeV run data

Table 3. Comparison between the recent QCD analyses of several groups. The upper part of the table indicates which experimental data are included in the fit. The main ingredients of the theoretical framework used in these analyses are given in the lower part of the table. Updated and expanded from [239].

	CTEQ6.6, CT10	MSTW08	NNPDF2.1, 2.3	ABKM09, ABM11	HERAPDF1.0, 1.5	GJR08, JR09
HERA DIS	+	+	+	+	+	+
Fixed target DIS	+	+	+	+	–	+
Fixed target Drell–Yan	+	+	+	+	–	+
Tevatron jets	+	+	+	+	–	+
				(NLO ABM11)		(GJR08)
Tevatron W, Z	+	+	+	–	–	–
LHC	–	–	+	–	–	–
			(2.3: see section 4.3.3)			
GM-VFNS	+	+	+	–	+	–
	(ACOT)	(Thorne–Roberts)	(FONLL)	(FFNS)	(Thorne–Roberts)	(FFNS)
Q_0^2 (GeV ²)	1.69	1	2	9	1.9	0.5
$\alpha_s(M_Z)$	Fixed	Fitted	Fixed	Fitted	Fixed	Fitted
PDF parameters	26	28	259 (NNs)	24	10 (for 1.0) 14 (for 1.5)	20
Strangeness	$s = \bar{s}$	Some flexibility	Maximal flexibility	$s = \bar{s}$	Assumptions (inc. $s = \bar{s}$)	$s = \bar{s}$
Errors	Hessian	Hessian	Monte Carlo	Hessian	Hessian	Hessian
Tolerance T ($\Delta\chi^2 = T^2$)	~ 6.1	Dynamical from ~ 1 to ~ 6	*	1	1	~ 4.7
NNLO	–	+	+	+	+	+
					(1.5, preliminary)	(JR09)

HERAPDF1.0 & 1.5

Combine NC and CC HERA-I data from H1 & ZEUS
 Complete MSbar NLO fit
 NLO: standard parameterisation with 10 parameters
 NNLO HERAPDF 1.5 with 14p

HERAPDF2.0

Include additional NC and CC HERA-II combined data
 Complete MSbar NLO and NNLO fit
 NLO & NNLO fits require 15 parameters

H1-14-042 / ZEUS-prel-14-007

$$xf(x, Q_0^2) = A \cdot x^B \cdot (1-x)^C \cdot (1 + Dx + Ex^2)$$

xg	xg	$xg(x) = A_g x^{B_g} (1-x)^{C_g}$	$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g}$
xu_v	$xU = xu + xc$	$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2)$	$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + D_{u_v} x + E_{u_v} x^2)$
xd_v	$xD = xd + xs$	$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}}$	$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}}$
$x\bar{U}$	$x\bar{U} = x\bar{u} + x\bar{c}$	$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}}$	$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x)$
$x\bar{D}$	$x\bar{D} = x\bar{d} + x\bar{s}$	$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}$	$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}$

HERAPDF1.0 & NLO HERAPDF1.5

HERAPDF2.0

$x\bar{s} = f_s x\bar{D}$ strange sea is a fixed fraction f_s of \bar{D} at Q_0^2

Apply momentum/counting sum rules:

$$\int_0^1 dx \cdot (xu_v + xd_v + x\bar{U} + x\bar{D} + xg) = 1$$

$$\int_0^1 dx \cdot u_v = 2 \quad \int_0^1 dx \cdot d_v = 1$$

$$B_{\bar{U}} = B_{\bar{D}}$$

$$Sea = 2(\bar{U} + \bar{D})$$

$$A_{\bar{U}} = A_{\bar{D}}(1 - f_s)$$

ensures $x\bar{u} \rightarrow x\bar{d}$ as $x \rightarrow 0$

$B_{u_v} = B_{d_v}$ constraint removed since HERAPDF1.5

$$Q_0^2 = 1.9$$

$$Q_{\min}^2 = 3.5 \text{ or } 10 \text{ GeV}^2$$

$$\alpha_s(M_z^2) = 0.118$$

$$2 \cdot 10^{-4} \leq x \leq 0.65$$

$$\begin{aligned}
 xg(x) &= A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g}, \\
 xu_v(x) &= A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + D_{u_v} x + E_{u_v} x^2), \\
 xd_v(x) &= A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}}, \\
 x\bar{U}(x) &= A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x), \\
 x\bar{D}(x) &= A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.
 \end{aligned}$$

NC structure functions

$$\begin{aligned}
 F_2 &= \frac{4}{9} (xU + x\bar{U}) + \frac{1}{9} (xD + x\bar{D}) \\
 xF_3 &\sim xu_v + xd_v
 \end{aligned}$$

CC structure functions

$$\begin{aligned}
 W_2^- &= x(U + \bar{D}), & W_2^+ &= x(\bar{U} + D) \\
 xW_3^- &= x(U - \bar{D}), & xW_3^+ &= x(D - \bar{U})
 \end{aligned}$$

■ fixed or constrained by sum-rules

■ parameters set equal but free

Additional parameters:

heavy quark masses M_c and M_b are optimised

$f_s = 0.4 \Rightarrow$ compromise value between unsuppressed ($f_s = 0.5$) and 'default' strange sea from dimuon data

$$\chi_{tot}^2(\mathbf{m}, \mathbf{b}) = \sum_i \frac{[\mu^i - m^i(1 - \sum_j \gamma_j^i b_j)]^2}{\delta_{i,stat}^2 \mu^i m^i (1 - \sum_j \gamma_j^i b_j) + (\delta_{i,unc} m^i)^2} + \sum_j b_j^2 + \sum_i \ln \frac{\delta_{i,unc}^2 m_i^2 + \delta_{i,stat}^2 \mu^i m^i}{\delta_{i,unc}^2 \mu_i^2 + \delta_{i,stat}^2 \mu_i^2}$$

modified χ^2 definition includes \ln term to account for likelihood transition to χ^2 after error scaling

Uncertainties of three types considered

- experimental
- model
- parametrisation

Experimental sources:

Hessian method used

Better control of systematics and correlations

Use traditional error definition $\Delta\chi^2 = 1$ to define error bands

Model Uncertainties:

We consider variations of all assumed input parameters in the fit

Deviations from central value fit quadratically summed

Variation	Standard Value	Lower Limit	Upper Limit
f_s	0.4	0.3	0.5
M_c^{opt} (NLO) [GeV]	1.47	1.41	1.53
M_c^{opt} (NNLO) [GeV]	1.44	1.38	1.50
M_b [GeV]	4.75	4.5	5.0
Q_{min}^2 [GeV ²]	10.0	7.5	12.5
Q_{min}^2 [GeV ²]	3.5	2.5	5.0
Q_0^2 [GeV ²]	1.9	1.6	2.2

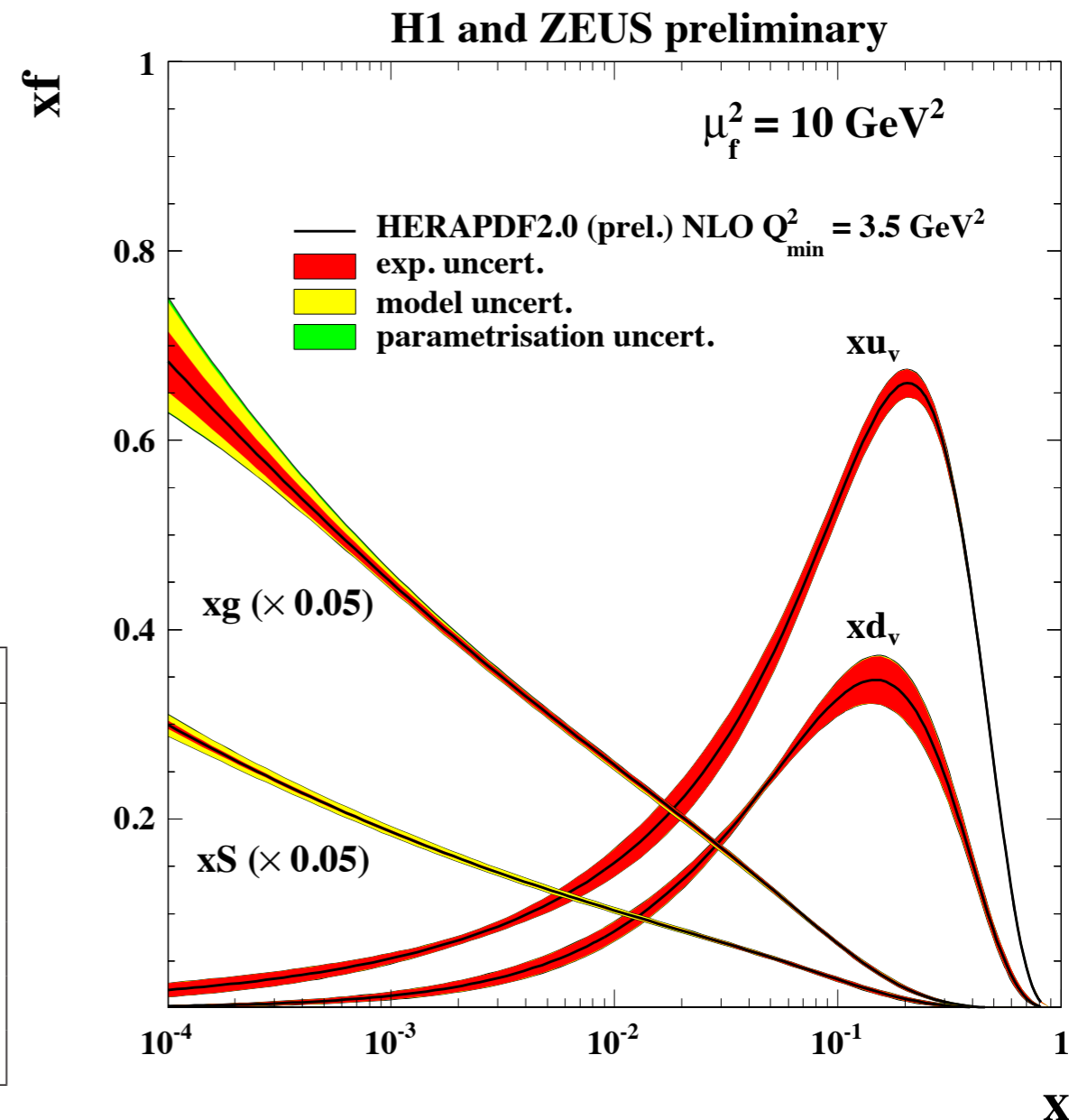
Parametrisation Uncertainty:

Take envelope of variations which include

variation of the arbitrary starting scale Q_0^2

all additional 16p fits with non-zero D or E parameters

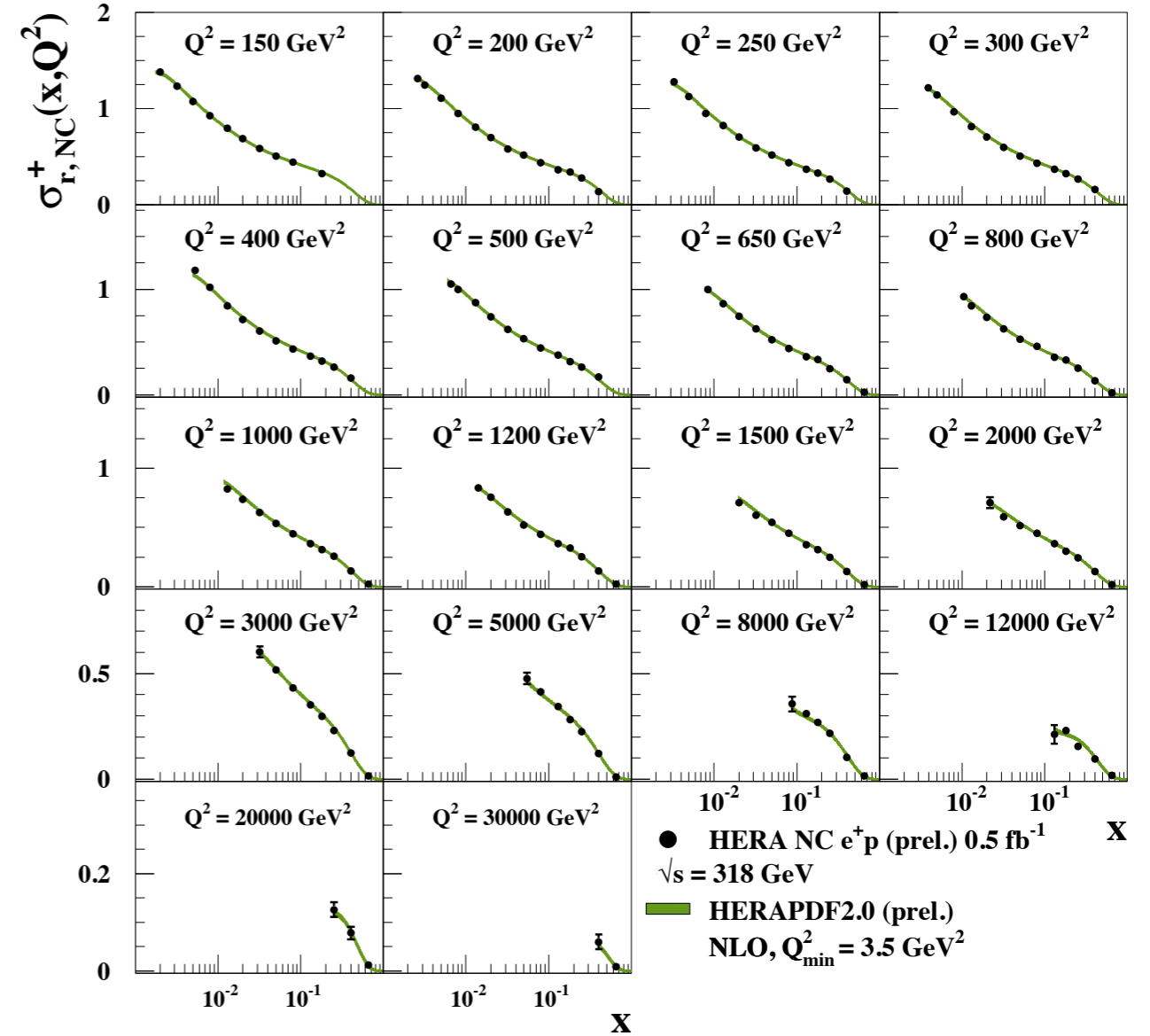
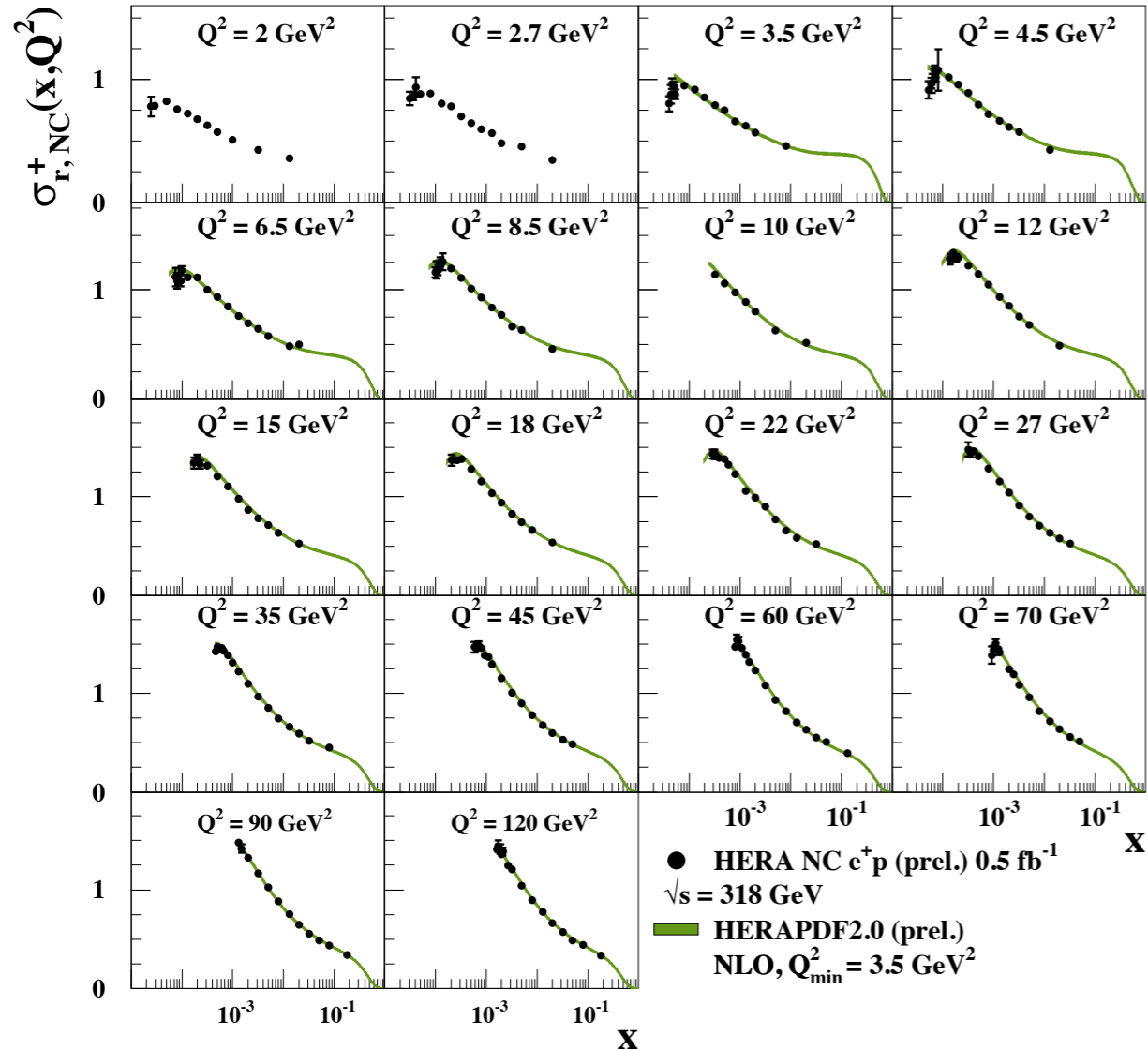
Only significant effect is from Q_0^2 variation



NC e^+p reduced cross section

$3.5 \leq Q^2 \leq 120 \text{ GeV}^2$

$150 \leq Q^2 \leq 30000 \text{ GeV}^2$

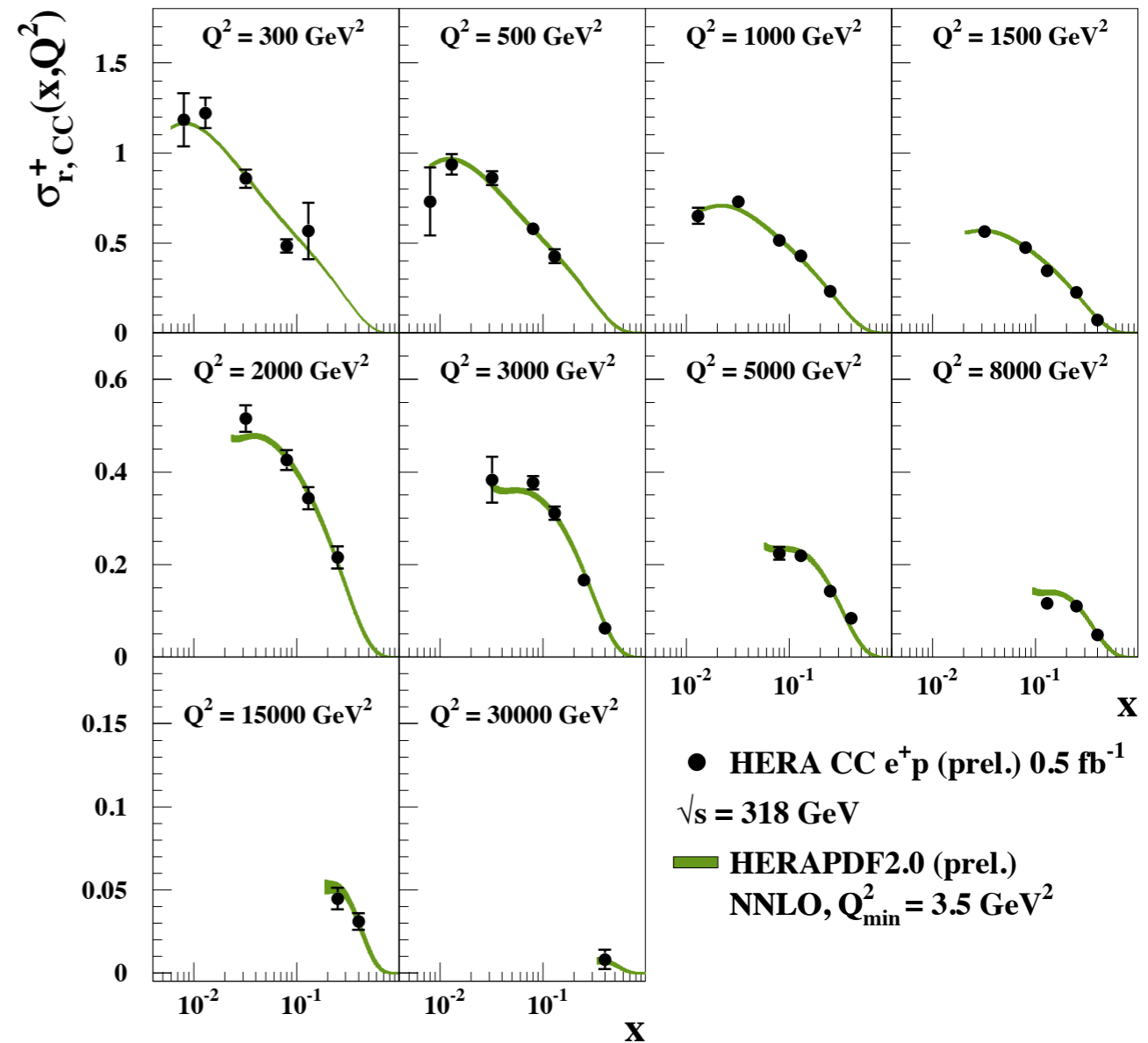
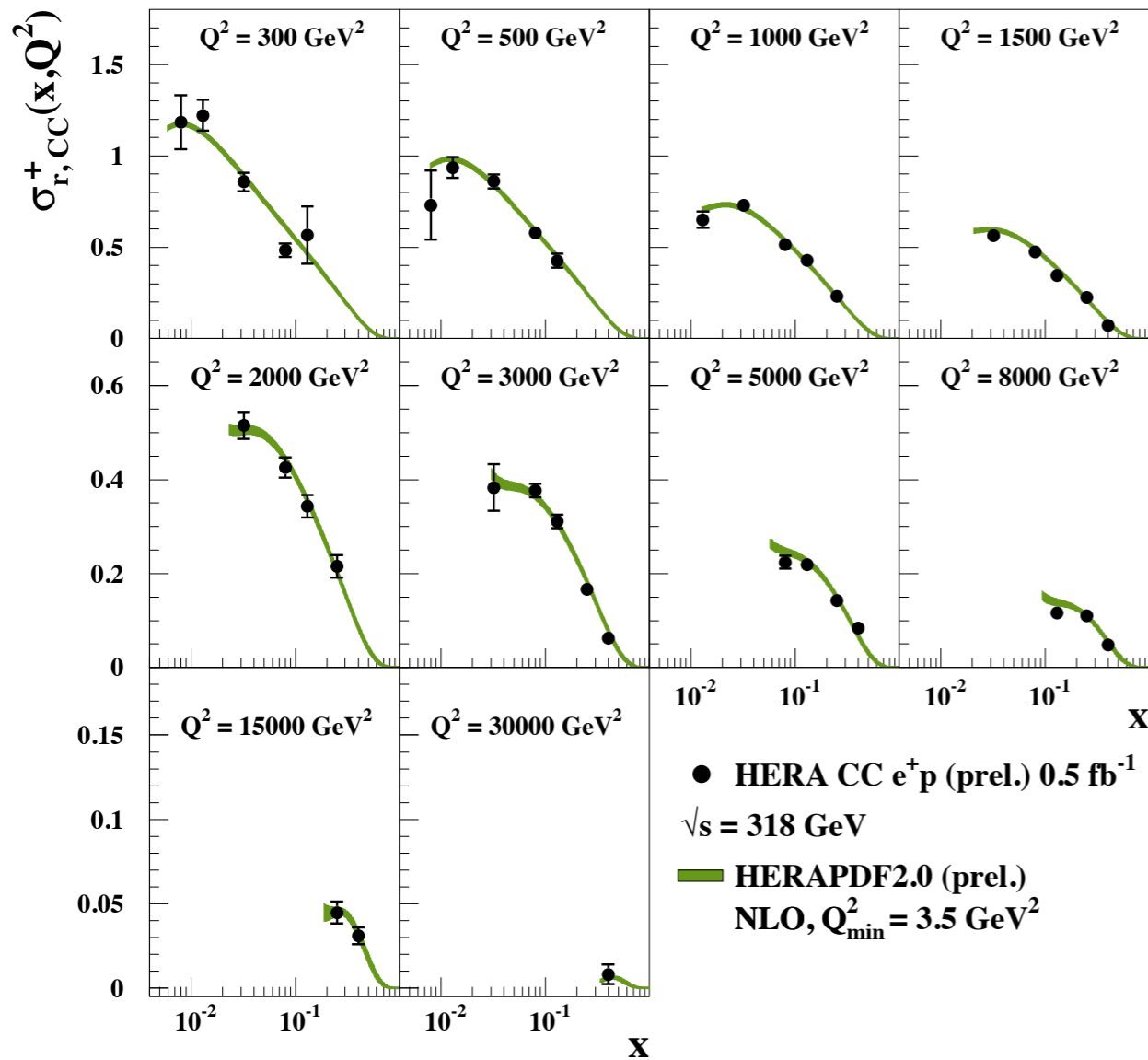


Good description of the data over \sim full Q^2 range
 Shown here for NLO
 Similar for NNLO

CC e^+p reduced cross section

$300 \leq Q^2 \leq 30000 \text{ GeV}^2$

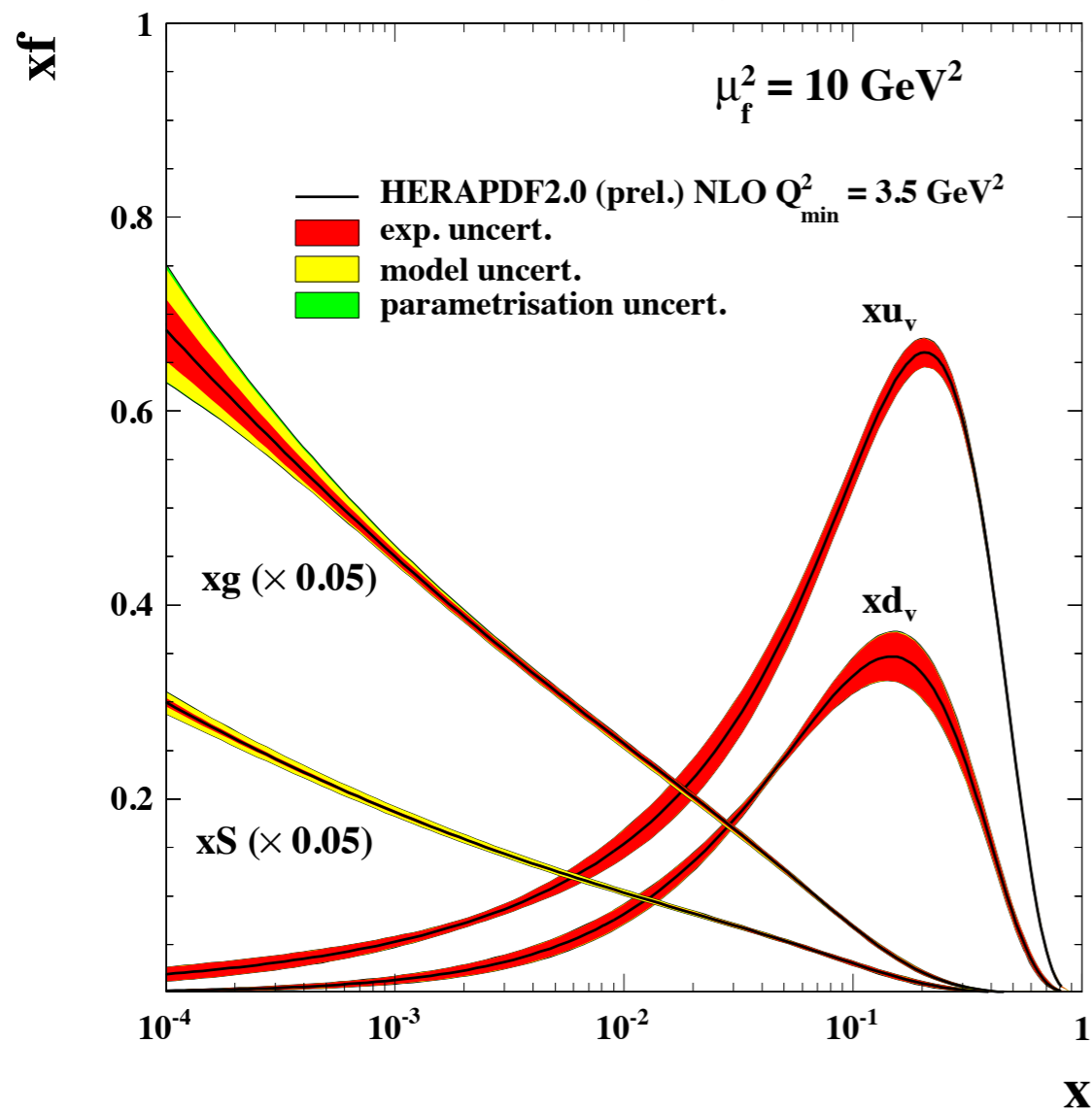
$150 \leq Q^2 \leq 30000 \text{ GeV}^2$



Good description of the CC data over full Q^2 range
 Shown here for NLO & NNLO
 Similar for e^-p data

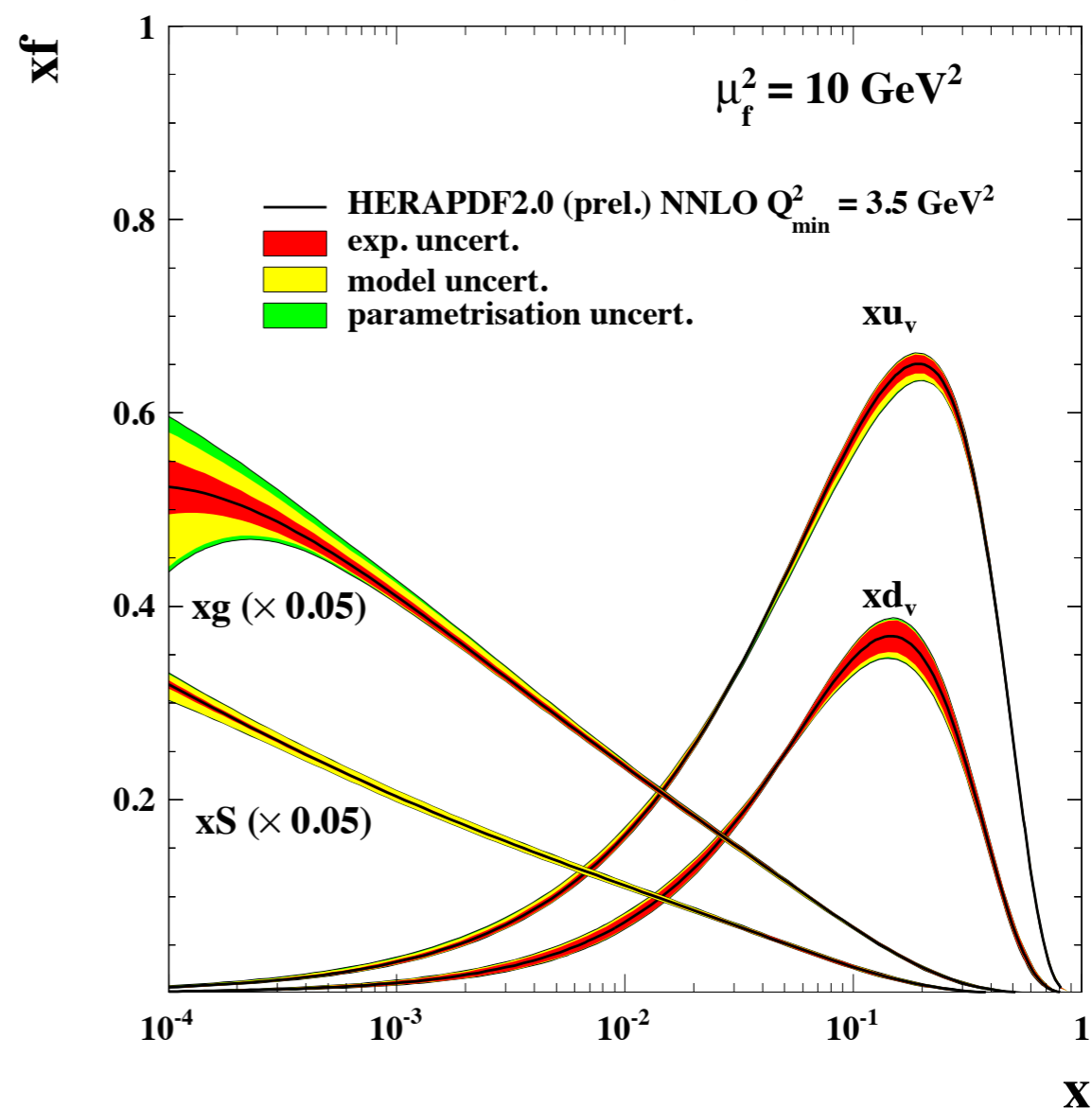
$$Q_{\min}^2 = 3.5 \text{ GeV}^2$$

NLO fit



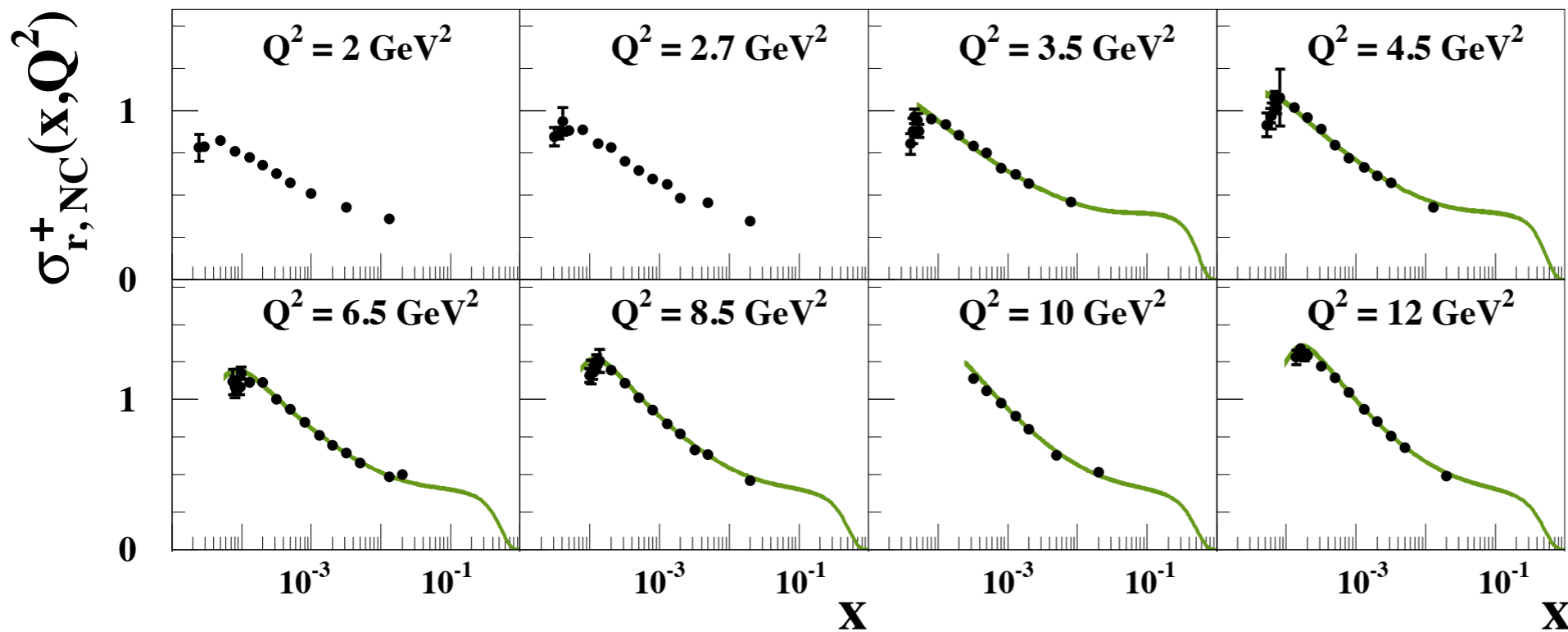
$$\chi^2/\text{ndf} = 1385/1130$$

NNLO fit



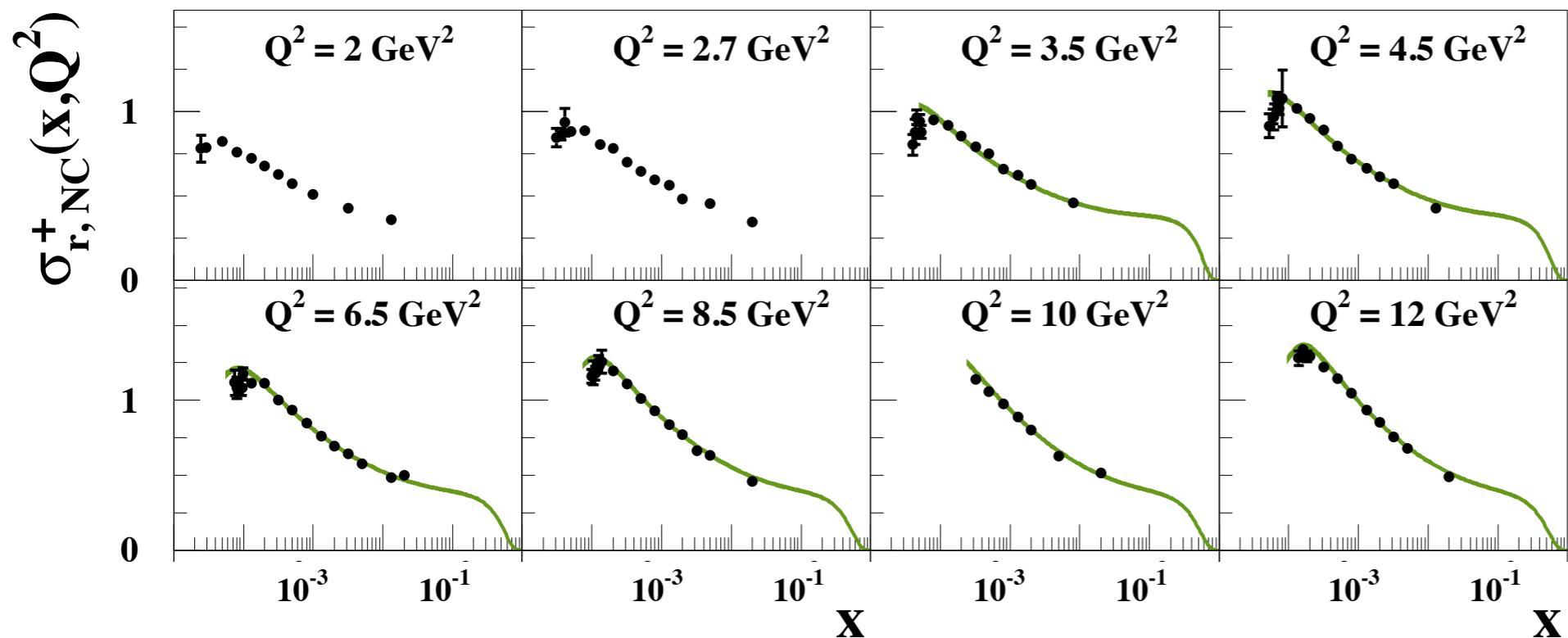
$$\chi^2/\text{ndf} = 1414/1130$$

NLO & NNLO fits similar
 Largest differences in xg and xS at low x



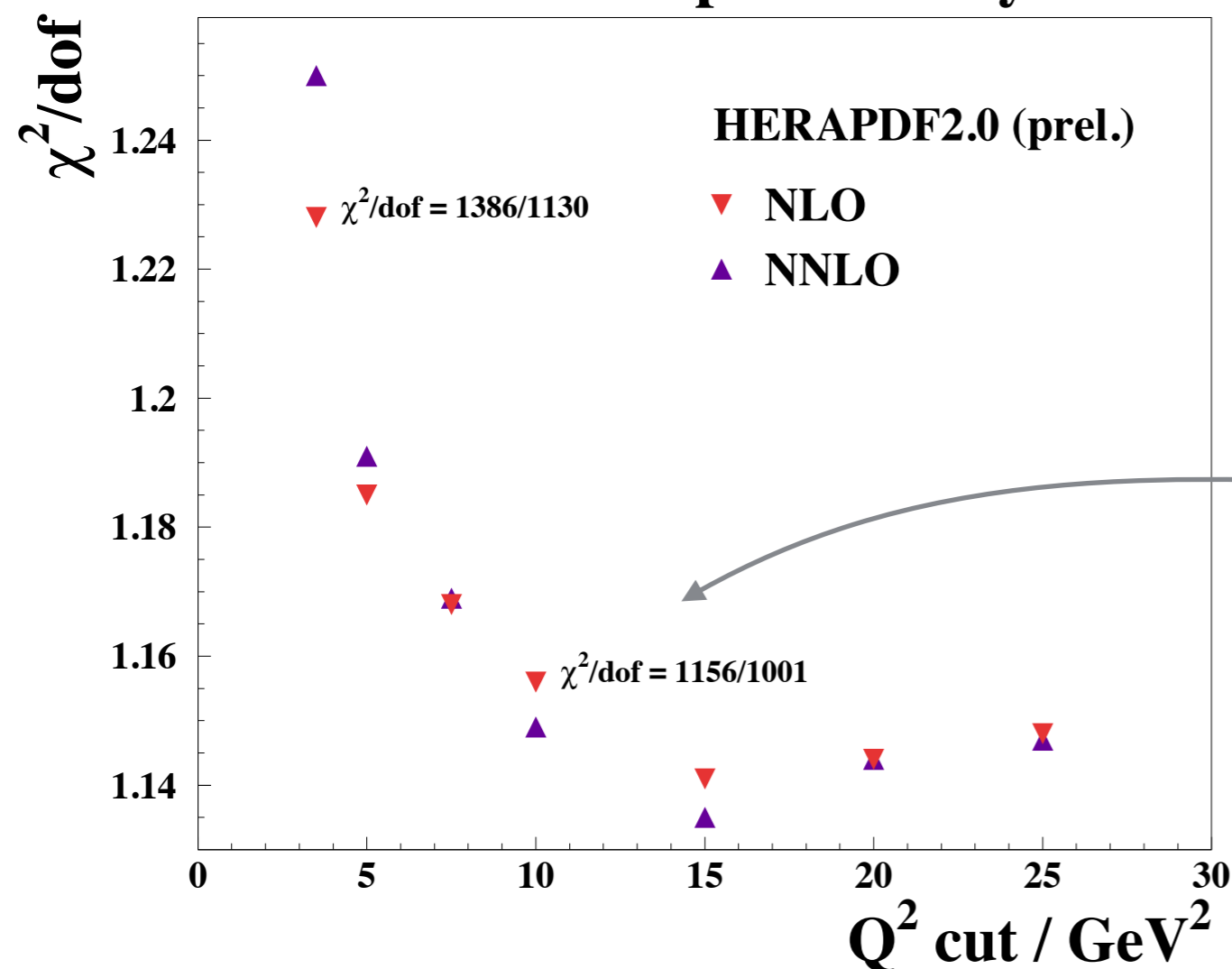
● HERA NC e^+p (prel.) 0.5 fb^{-1}
 $\sqrt{s} = 318 \text{ GeV}$
 — HERAPDF2.0 (prel.)
NLO, $Q_{\text{min}}^2 = 3.5 \text{ GeV}^2$

Some tension at low x
 NLO & NNLO same trends



● HERA NC e^+p (prel.) 0.5 fb^{-1}
 $\sqrt{s} = 318 \text{ GeV}$
 — HERAPDF2.0 (prel.)
NNLO, $Q_{\text{min}}^2 = 3.5 \text{ GeV}^2$

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Adjust minimum Q^2 cut on data entering fit
 Already included in uncertainty
 Look at larger range and effect on χ^2/ndf

For $Q^2_{\text{min}} = 3.5 \text{ GeV}^2$
 $\chi^2/\text{ndf} = 1385 / 1130$ at NLO
 $\chi^2/\text{ndf} = 1414 / 1130$ at NNLO

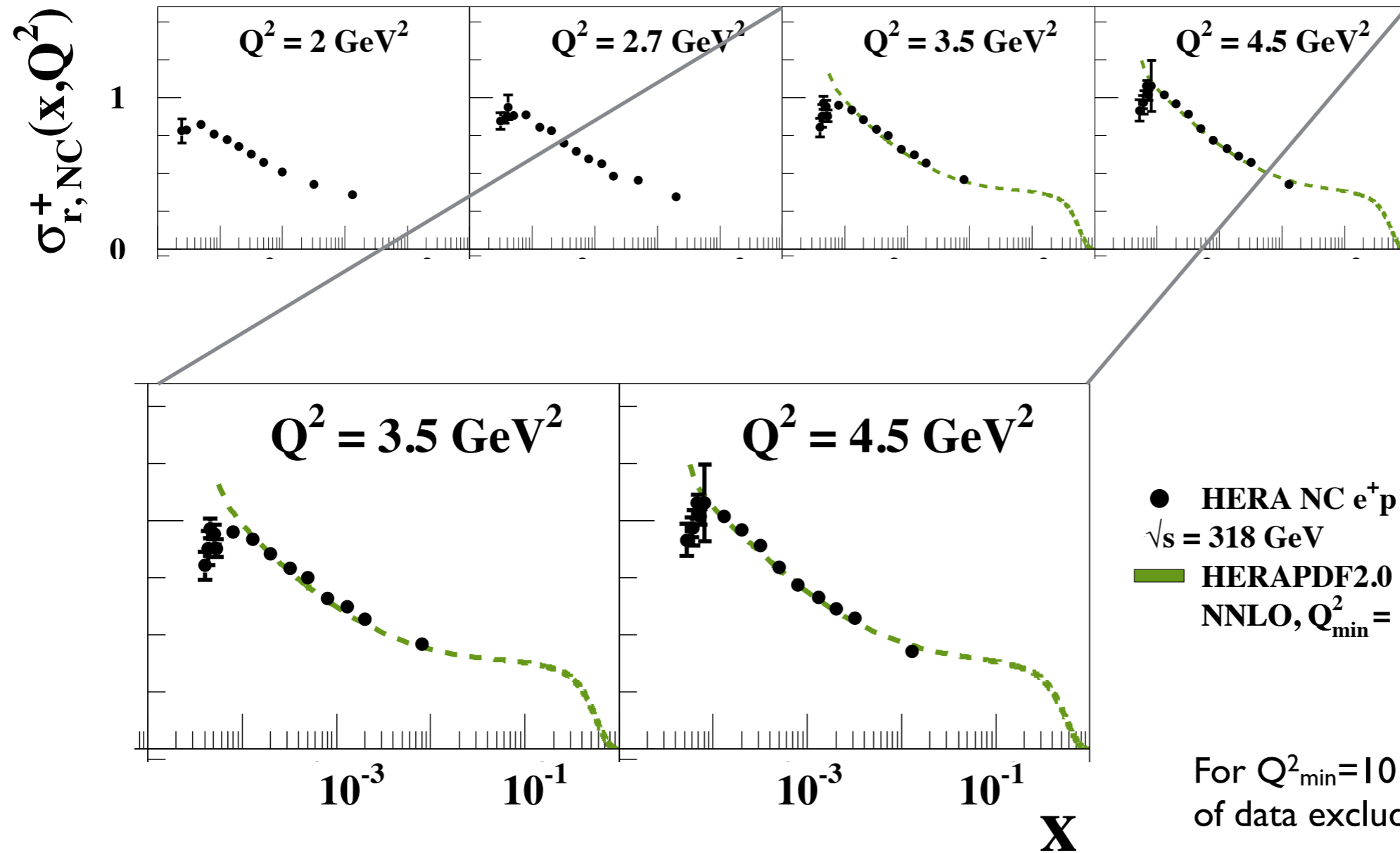
For $Q^2_{\text{min}} = 10 \text{ GeV}^2$
 $\chi^2/\text{ndf} = 1156 / 1001$ at NLO
 $\chi^2/\text{ndf} = 1150 / 1001$ at NNLO

χ^2 appears to saturate for $Q^2_{\text{min}} = 10 \text{ GeV}^2$

Similar behaviour observed for HERA-I combination
 Not so clear due to lower high Q^2 precision

For HERA-I $Q^2_{\text{min}} = 3.5 \text{ GeV}^2$
 $\chi^2/\text{ndf} = 637 / 656$ at NLO

Alternative χ^2 definitions show same behaviour
 Alternative cuts in x , Q^2_{max} have much smaller effect



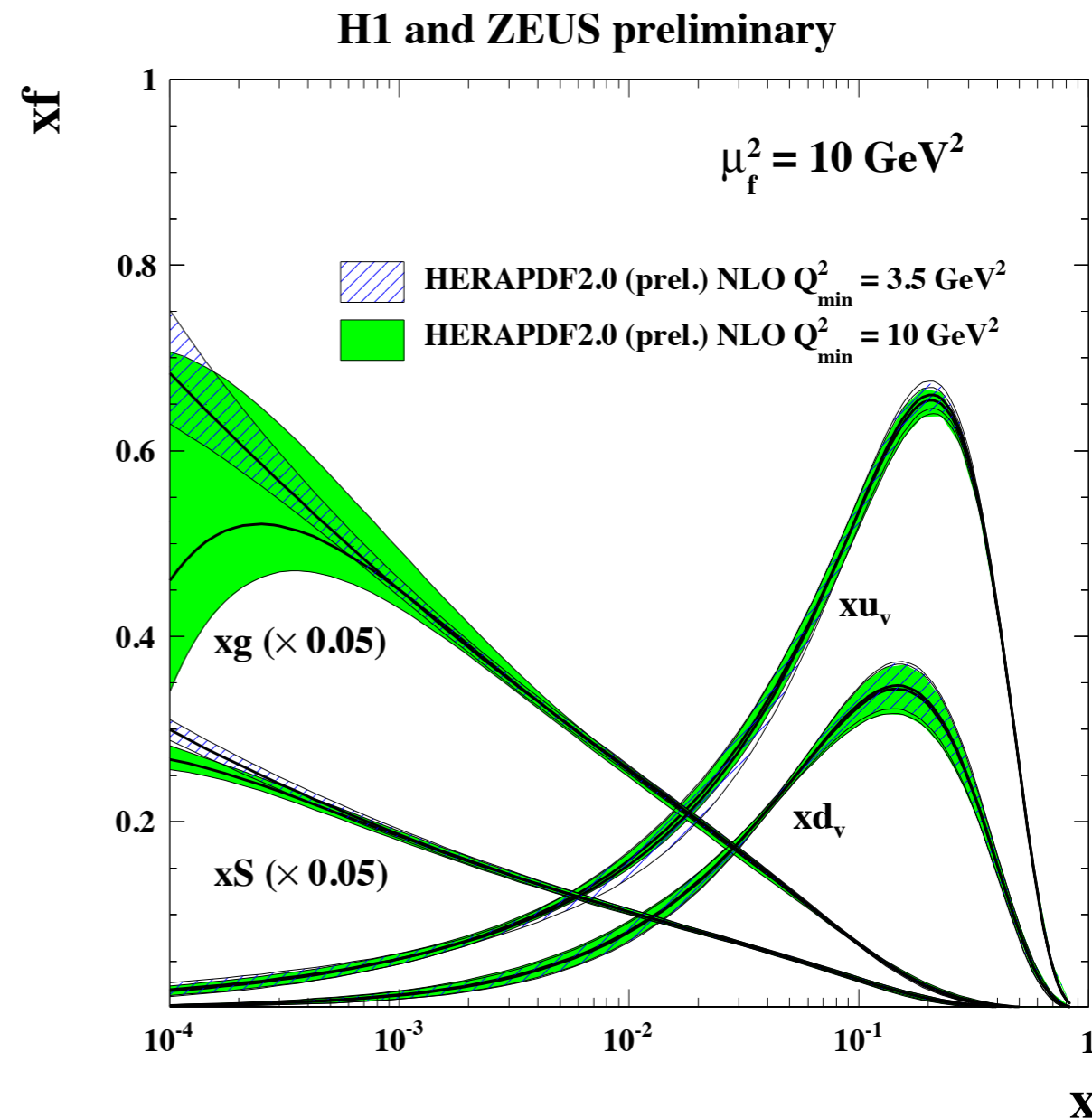
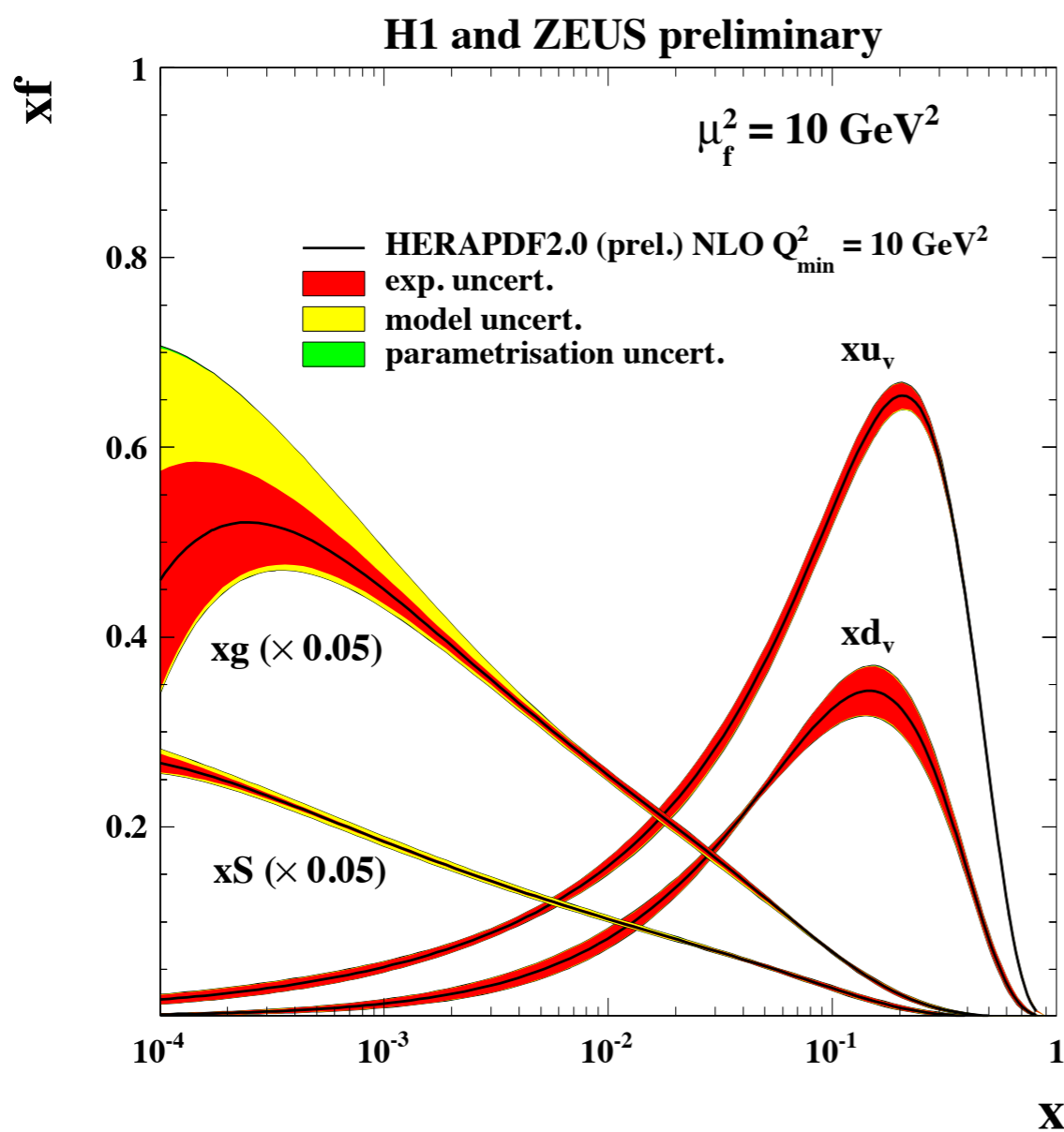
For $Q_{\min}^2 = 10 \text{ GeV}^2$ poor description of data excluded from fit

Extrapolated fit systematically higher than data at low x / low Q^2

Similar for NLO fit



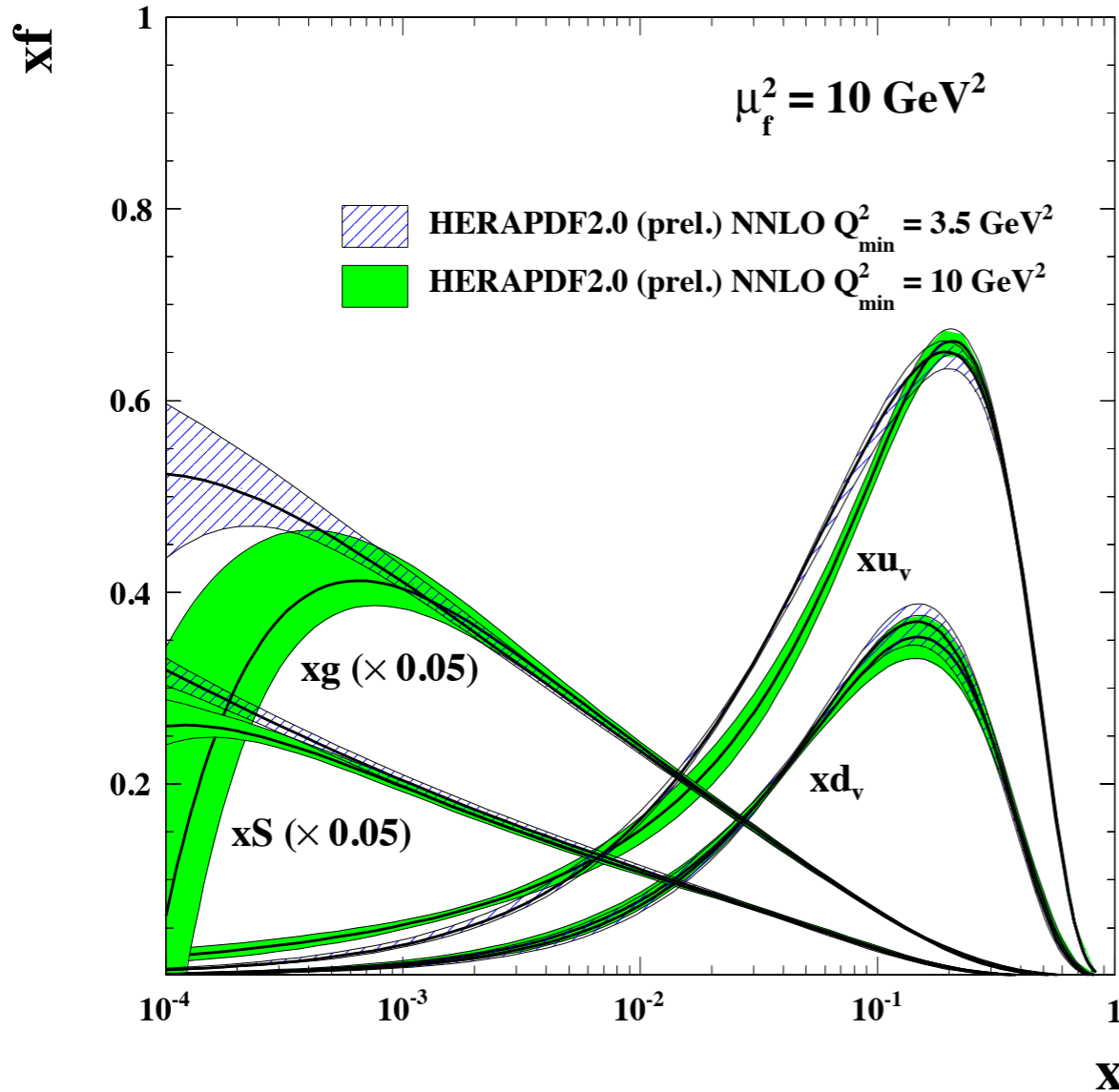
Compare PDFs at NLO with $Q_{\min}^2=3.5$ and 10 GeV^2



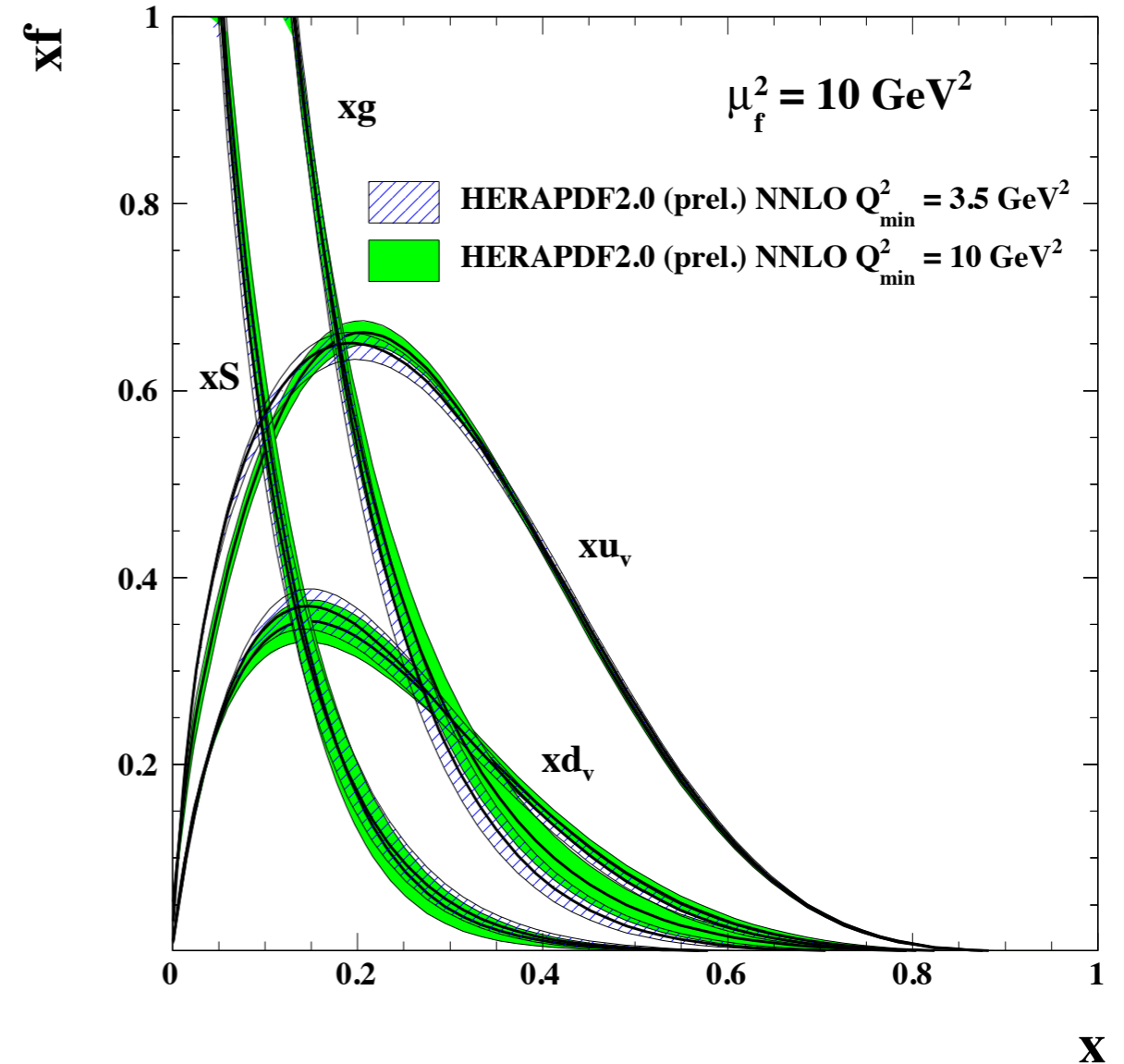
PDF central values in good agreement for $x > 10^{-3}$
 Higher Q_{\min}^2 cut increase low x gluon uncertainty as expected
 Large model uncertainty arising from Q_{\min}^2 cut variation

Compare PDFs at NNLO with $Q_{\min}^2=3.5$ and 10 GeV^2

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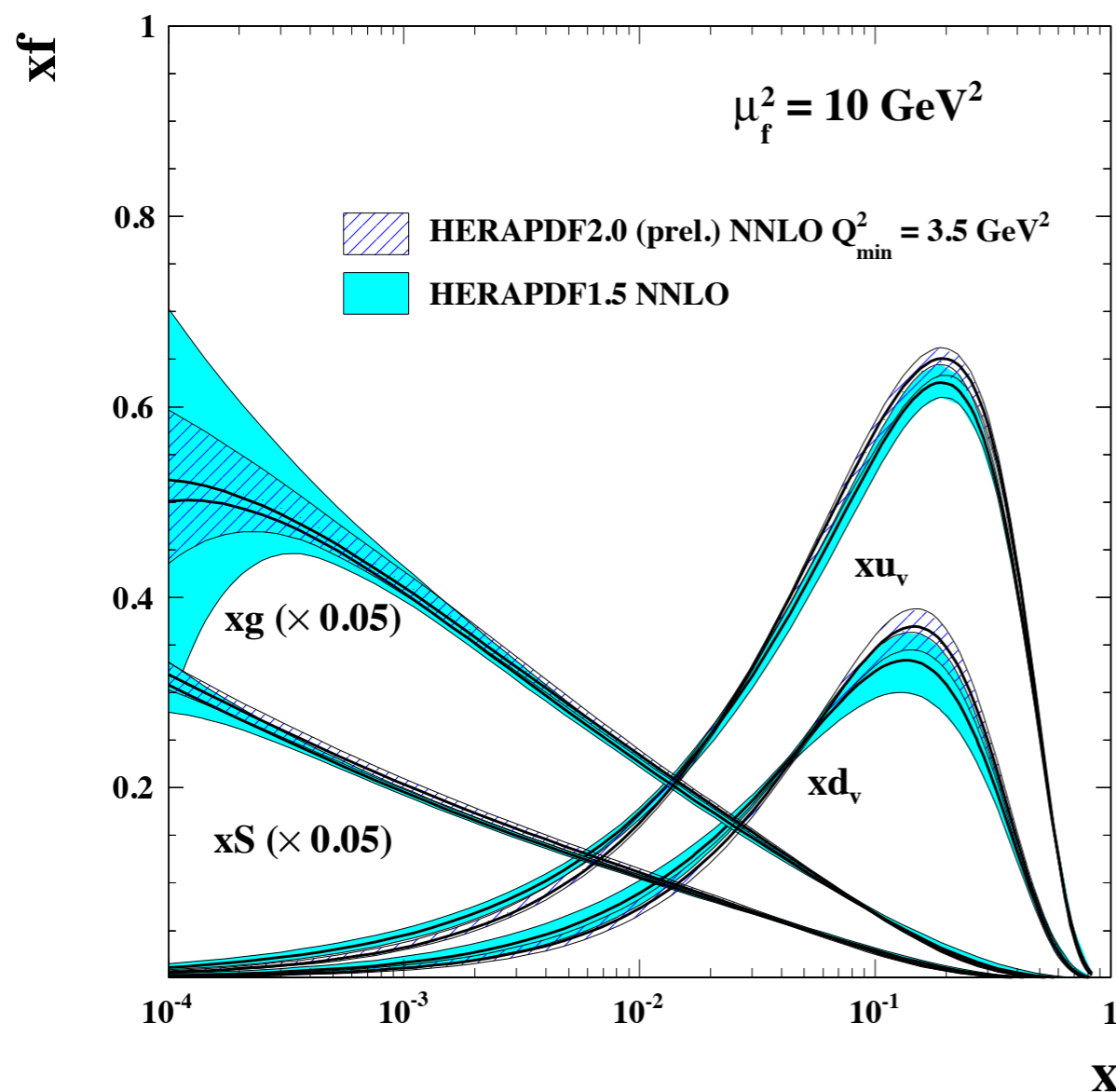
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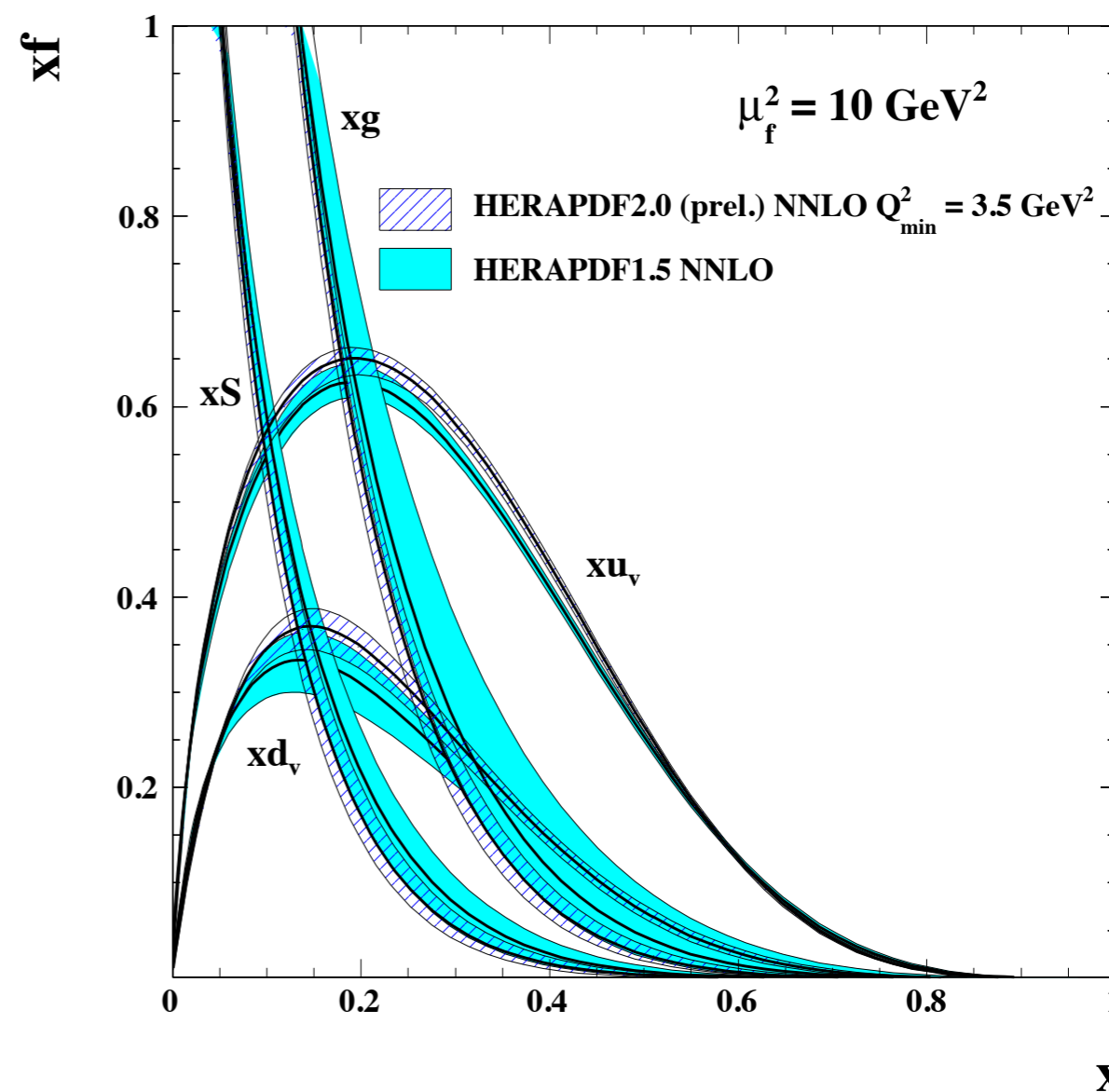
Similar story at NNLO:
 PDF central values in good agreement for $x > 10^{-3}$
 Higher Q_{\min}^2 cut increase low x gluon uncertainty as expected
 Large model uncertainty arising from Q_{\min}^2 cut variation

Compare HERAPDF1.5 and HERAPDF2.0 at NNLO

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At high x gluon and sea uncertainties reduced
 gluon & sea distributions become softer in HERAPDF2.0
 Uncertainties on valence distributions are reduced

HERA data provided detailed insight into parton dynamics

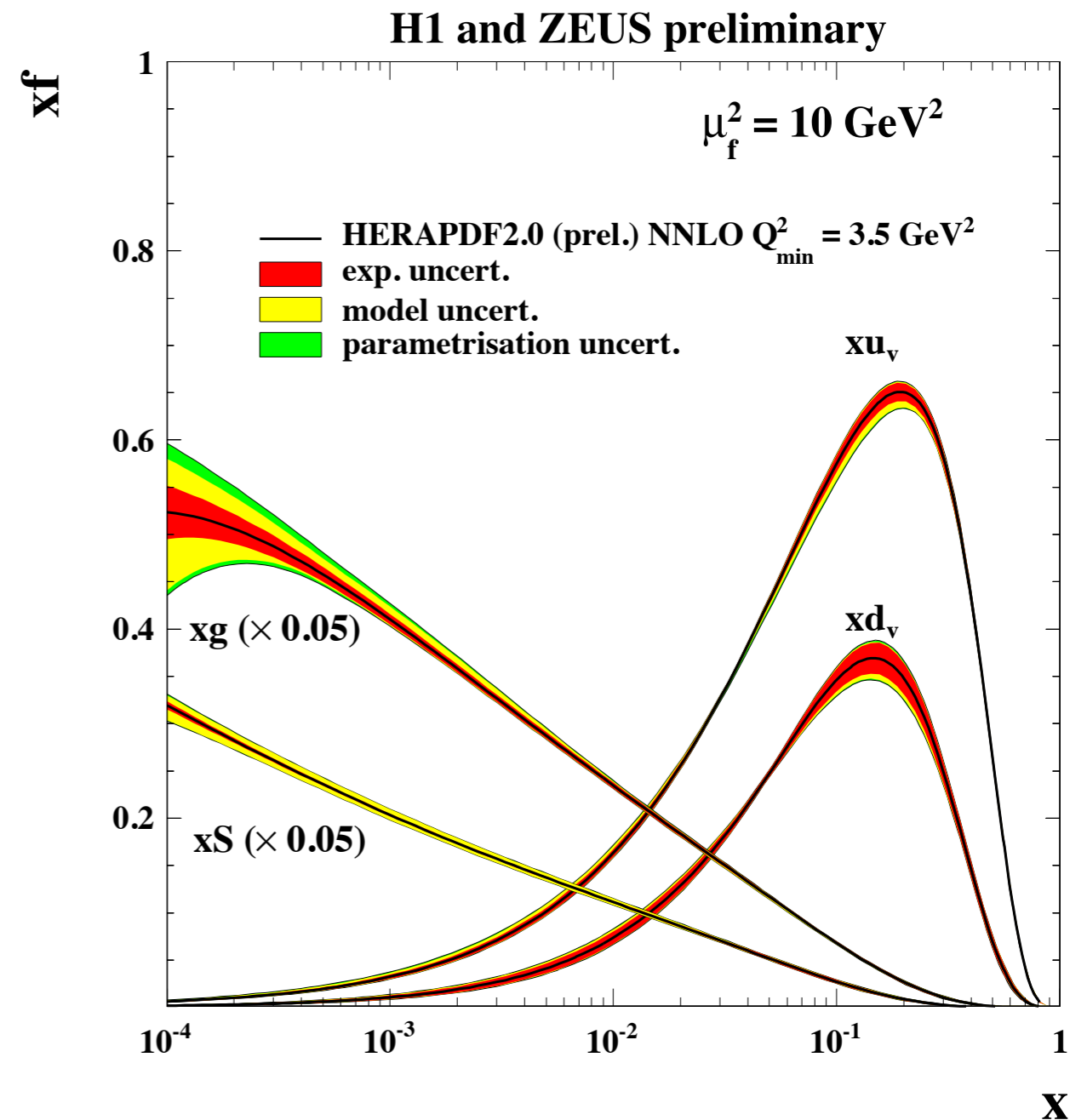
Helped experimentally establish NNLO pQCD

Underpins all LHC measurements

Precise determination of PDFs (specially gluon)
 \Rightarrow accurate predictions of LHC Higgs production

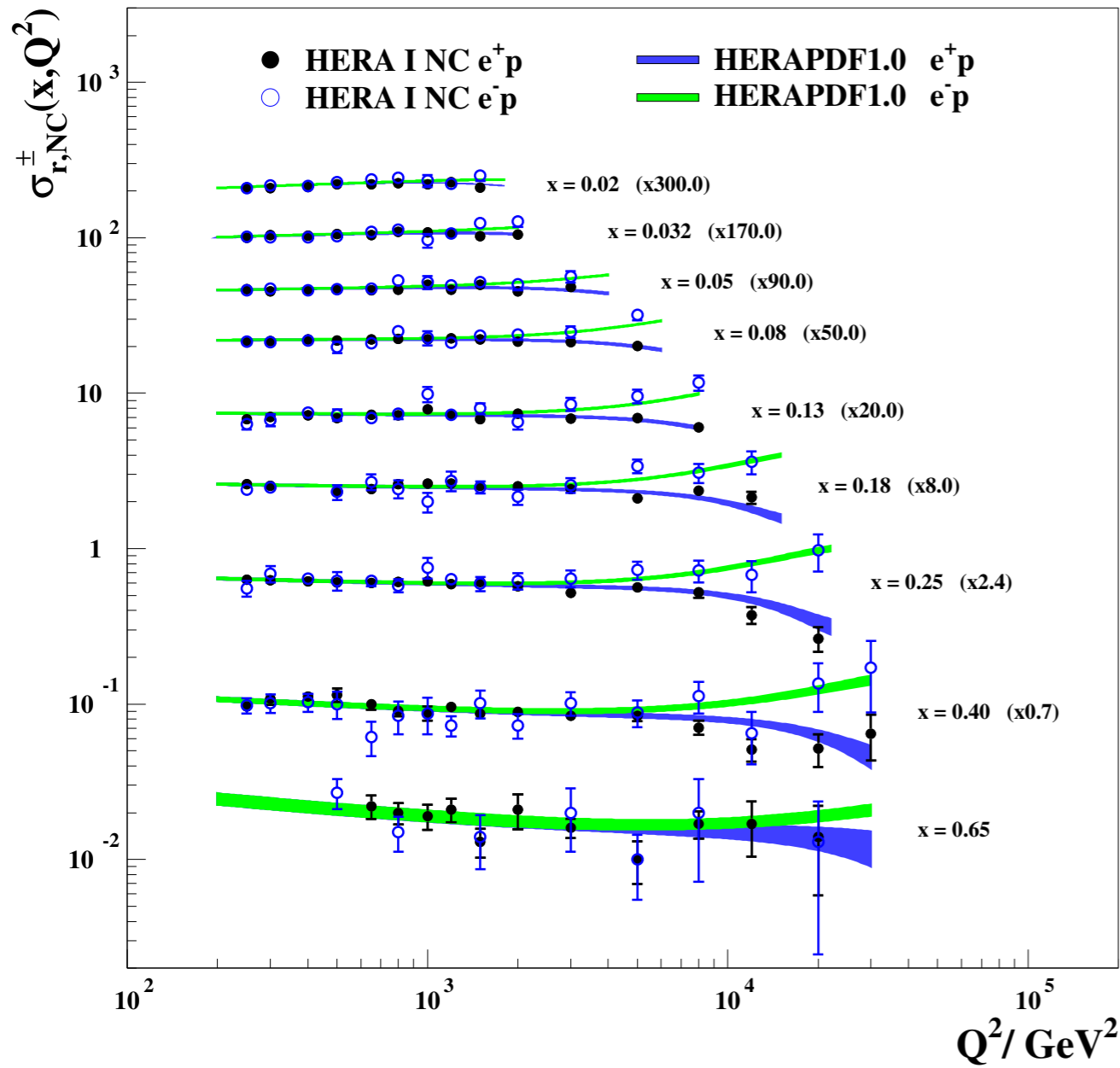
Plan:

publish the combined inclusive data & HERAPDF2.0





H1 and ZEUS



H1 and ZEUS preliminary

