

DIS 2015

XXIII International Workshop on
Deep-Inelastic Scattering and
Related Subjects

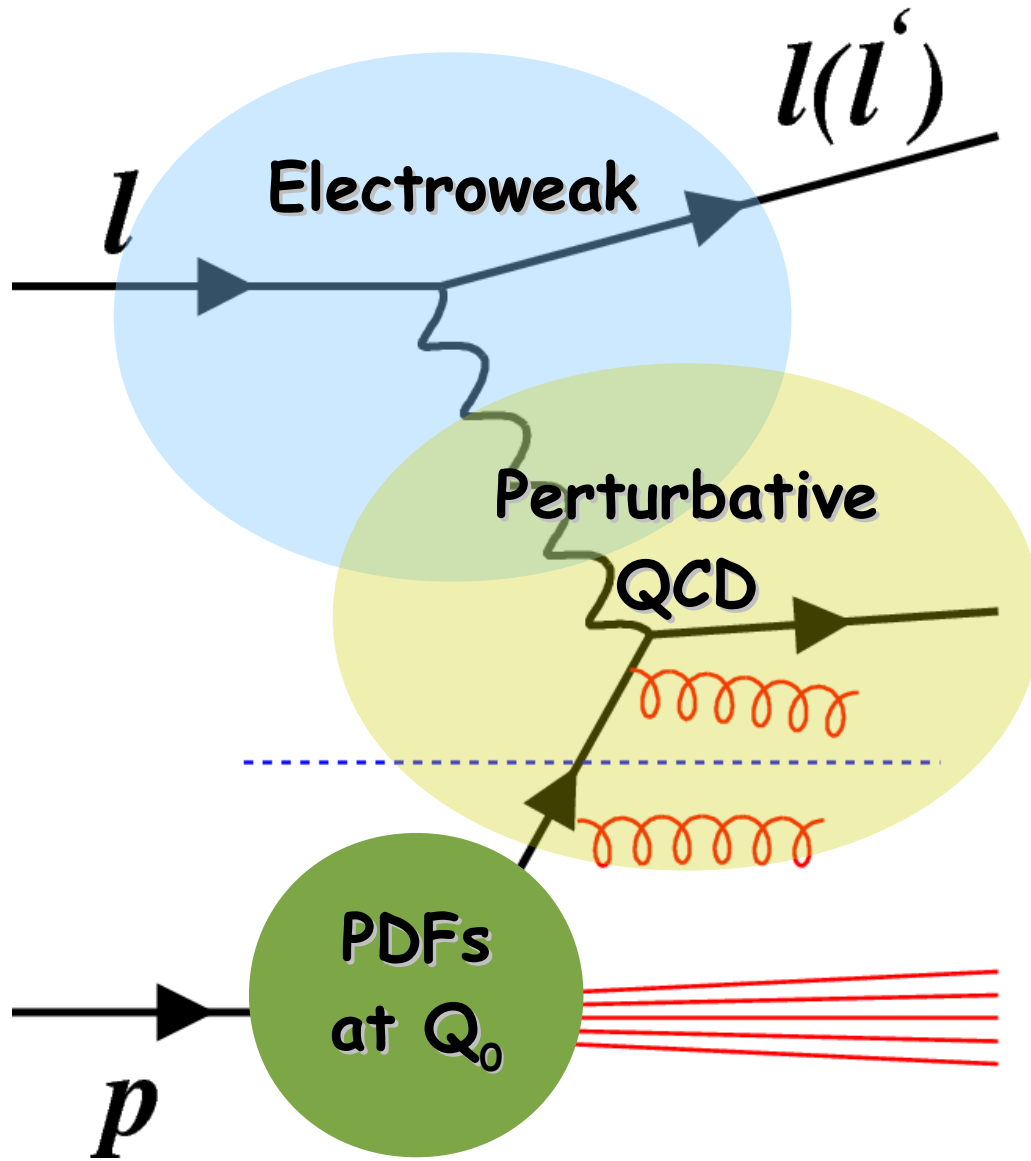
Dallas, Texas
April 27 – May 1, 2015



Combined Measurement of Inclusive ep Scattering Cross Sections at HERA

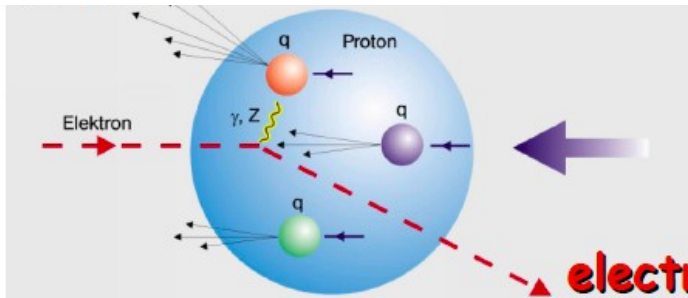
K. Wichmann on behalf of H1 and ZEUS Collaborations

Deep Inelastic Scattering @ HERA



- Fix pQCD & PDFs
! Test Electroweak
- Fix Electroweak
! Test pQCD & PDFs

- Fix Electroweak & pQCD
! Determine PDFs



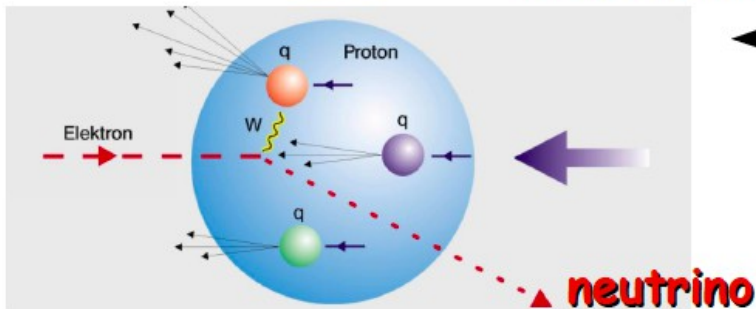
Combined inclusive DIS

← Neutral Current (NC)

γ, Z^0 exchange

← Charged Current (CC)

W^\pm exchange



$$Q^2 = -q^2 = -(k - k')^2$$

$$x_{Bj} = \frac{Q^2}{2p \cdot q} \quad y = \frac{p \cdot q}{p \cdot k}$$

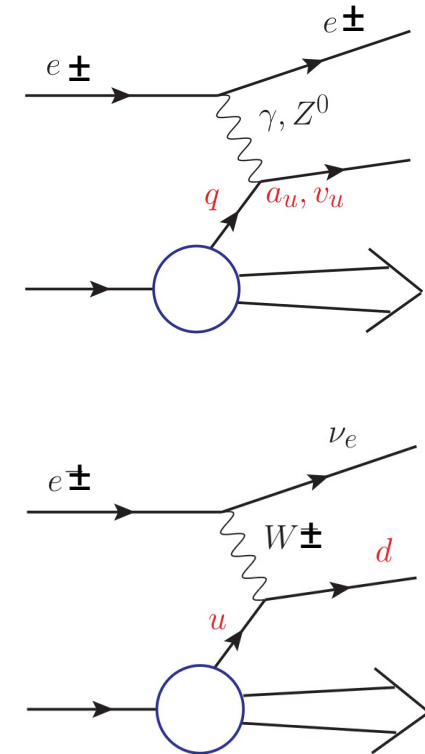
$$s = (p + k)^2 \quad Q^2 = x_{Bj} \cdot y \cdot s$$

H1 and ZEUS published all HERA inclusive DIS measurements - 1 fb⁻¹

Now we combine these measurements

Inclusive DIS data samples

- 41 final data sets with HERA inclusive measurements
- NCep and CCep
 - 21 HERA I data samples
 - 20 HERA II data samples, including:
 - 8 inclusive HERA II $E_p = 920 \text{ GeV}$
 - 4 high y data $E_p = 920 \text{ GeV}$
 - 4 high y data $E_p = 575 \text{ GeV}$
 - 4 high y data $E_p = 460 \text{ GeV}$
- Data 1994-2007: **over 10 years of data taking!**
- 22 papers between 1997-2014: **almost 20 years of data analysis!**



Total of 2927 data points combined to 1307

Full publication list

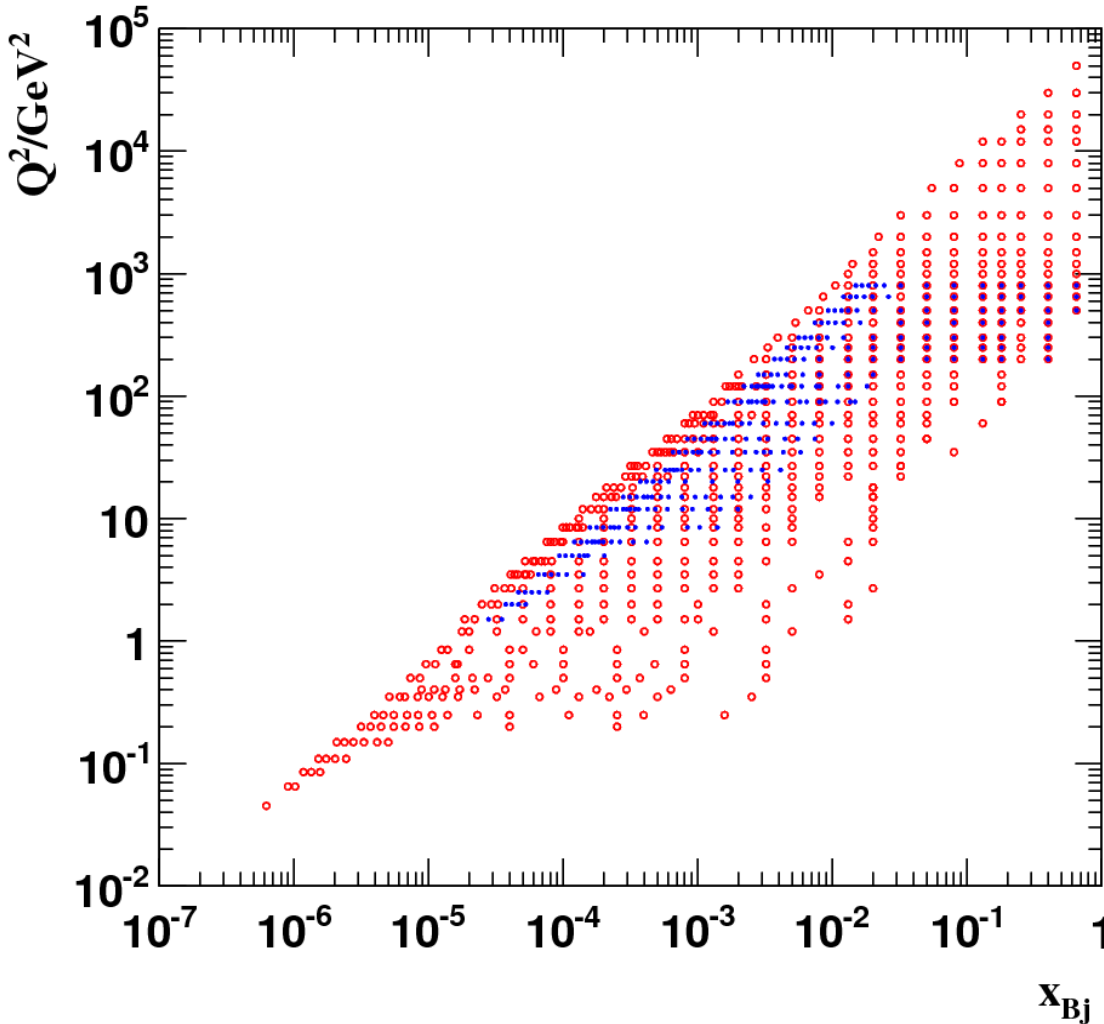
- F. Aaron *et al.* [H1 Collaboration], Eur. Phys. J. C **63**, 625 (2009), [arXiv:0904.0929].
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- C. Adloff *et al.* [H1 Collaboration], Eur. Phys. J. C **13**, 609 (2000), [hep-ex/9908059].
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- C. Adloff *et al.* [H1 Collaboration], Eur. Phys. J. C **30**, 1 (2003), [hep-ex/0304003].
- F. Aaron *et al.* [H1 Collaboration], JHEP **1209**, 061 (2012), [arXiv:1206.7007].
- V. Andreev *et al.* [H1 Collaboration], Eur. Phys. J. C **73**, 2814 (2013), [arXiv:1312.4821].
- F. Aaron *et al.* [H1 Collaboration], Eur. Phys. J. C **71**, 1579 (2011), [arXiv:1012.4355].
- J. Breitweg *et al.* [ZEUS Collaboration], Phys. Lett. B **407**, 432 (1997), [hep-ex/9707025].
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- J. Breitweg *et al.* [ZEUS Collaboration], Eur. Phys. J. C **7**, 609 (1999), [hep-ex/9809005].
- S. Chekanov *et al.* [ZEUS Collaboration], Eur. Phys. J. C **21**, 443 (2001), [hep-ex/0105090].
- J. Breitweg *et al.* [ZEUS Collaboration], Eur. Phys. J. C **12**, 411 (2000), [Erratum-ibid. C **27**, 305 (2003), [hep-ex/9907010].
- S. Chekanov *et al.* [ZEUS Collaboration], Eur. Phys. J. C **28**, 175 (2003), [hep-ex/0208040].
- S. Chekanov *et al.* [ZEUS Collaboration], Phys. Lett. B **539**, 197 (2002), [Erratum-ibid. B **552**, 308 (2003)], [hep-ex/0205091].
- S. Chekanov *et al.* [ZEUS Collaboration], Phys. Rev. D **70**, 052001 (2004), [hep-ex/0401003].
- S. Chekanov *et al.* [ZEUS Collaboration], Eur. Phys. J. C **32**, 1 (2003), [hep-ex/0307043].
- S. Chekanov *et al.* [ZEUS Collaboration], Eur. Phys. J. C **62**, 625 (2009), [arXiv:0901.2385].
- S. Chekanov *et al.* [ZEUS Collaboration], Eur. Phys. J. C **61**, 223 (2009), [arXiv:0812.4620].
- H. Abramowicz *et al.* [ZEUS Collaboration], Phys. Rev. D **87**, 052014 (2013), [arXiv:1208.6138].
- H. Abramowicz *et al.* [ZEUS Collaboration], Eur. Phys. J. C **70**, 945 (2010), [arXiv:1008.3493].
- H. Abramowicz *et al.* [ZEUS Collaboration], Phys. Rev. D **90**, 072002 (2014), [arXiv:1404.6376].

Data Set		x_{Bj} Grid		Q^2 [GeV ²] Grid		\mathcal{L}	e^+ / e^-	\sqrt{s}	x_{Bj}, Q^2 from
		from	to	from	to	pb ⁻¹		GeV	equations
HERA I $E_p = 820$ GeV and $E_p = 920$ GeV data sets									
H1 svx-mb	95-00	0.000005	0.02	0.2	12	2.1	$e^+ p$	301, 319	13,17,18
H1 low Q^2	96-00	0.0002	0.1	12	150	22	$e^+ p$	301, 319	13,17,18
H1 NC	94-97	0.0032	0.65	150	30000	35.6	$e^+ p$	301	19
H1 CC	94-97	0.013	0.40	300	15000	35.6	$e^+ p$	301	14
H1 NC	98-99	0.0032	0.65	150	30000	16.4	$e^- p$	319	19
H1 CC	98-99	0.013	0.40	300	15000	16.4	$e^- p$	319	14
H1 NC HY	98-99	0.0013	0.01	100	800	16.4	$e^- p$	319	13
H1 NC	99-00	0.0013	0.65	100	30000	65.2	$e^+ p$	319	19
H1 CC	99-00	0.013	0.40	300	15000	65.2	$e^+ p$	319	14
ZEUS BPC	95	0.000002	0.00006	0.11	0.65	1.65	$e^+ p$	300	13
ZEUS BPT	97	0.0000006	0.001	0.045	0.65	3.9	$e^+ p$	300	13, 19
ZEUS SVX	95	0.000012	0.0019	0.6	17	0.2	$e^+ p$	300	13
ZEUS NC	96-97	0.00006	0.65	2.7	30000	30.0	$e^+ p$	300	21
ZEUS CC	94-97	0.015	0.42	280	17000	47.7	$e^+ p$	300	14
ZEUS NC	98-99	0.005	0.65	200	30000	15.9	$e^- p$	318	20
ZEUS CC	98-99	0.015	0.42	280	30000	16.4	$e^- p$	318	14
ZEUS NC	99-00	0.005	0.65	200	30000	63.2	$e^+ p$	318	20
ZEUS CC	99-00	0.008	0.42	280	17000	60.9	$e^+ p$	318	14
HERA II $E_p = 920$ GeV data sets									
H1 NC ^{1.5p}	03-07	0.0008	0.65	60	30000	182	$e^+ p$	319	13, 19
H1 CC ^{1.5p}	03-07	0.008	0.40	300	15000	182	$e^+ p$	319	14
H1 NC ^{1.5p}	03-07	0.0008	0.65	60	50000	151.7	$e^- p$	319	13, 19
H1 CC ^{1.5p}	03-07	0.008	0.40	300	30000	151.7	$e^- p$	319	14
H1 NC med Q^2 ^{*y.5}	03-07	0.0000986	0.005	8.5	90	97.6	$e^+ p$	319	13
H1 NC low Q^2 ^{*y.5}	03-07	0.000029	0.00032	2.5	12	5.9	$e^+ p$	319	13
ZEUS NC	06-07	0.005	0.65	200	30000	135.5	$e^+ p$	318	13,14,20
ZEUS CC ^{1.5p}	06-07	0.0078	0.42	280	30000	132	$e^+ p$	318	14
ZEUS NC ^{1.5}	05-06	0.005	0.65	200	30000	169.9	$e^- p$	318	20
ZEUS CC ^{1.5}	04-06	0.015	0.65	280	30000	175	$e^- p$	318	14
ZEUS NC nominal ^{*y}	06-07	0.000092	0.008343	7	110	44.5	$e^+ p$	318	13
ZEUS NC satellite ^{*y}	06-07	0.000071	0.008343	5	110	44.5	$e^+ p$	318	13
HERA II $E_p = 575$ GeV data sets									
H1 NC high Q^2	07	0.00065	0.65	35	800	5.4	$e^+ p$	252	13, 19
H1 NC low Q^2	07	0.0000279	0.0148	1.5	90	5.9	$e^+ p$	252	13
ZEUS NC nominal	07	0.000147	0.013349	7	110	7.1	$e^+ p$	251	13
ZEUS NC satellite	07	0.000125	0.013349	5	110	7.1	$e^+ p$	251	13
HERA II $E_p = 460$ GeV data sets									
H1 NC high Q^2	07	0.00081	0.65	35	800	11.8	$e^+ p$	225	13, 19
H1 NC low Q^2	07	0.0000348	0.0148	1.5	90	12.2	$e^+ p$	225	13
ZEUS NC nominal	07	0.000184	0.016686	7	110	13.9	$e^+ p$	225	13
ZEUS NC satellite	07	0.000143	0.016686	5	110	13.9	$e^+ p$	225	13

Q^2-x_{Bj} common grids

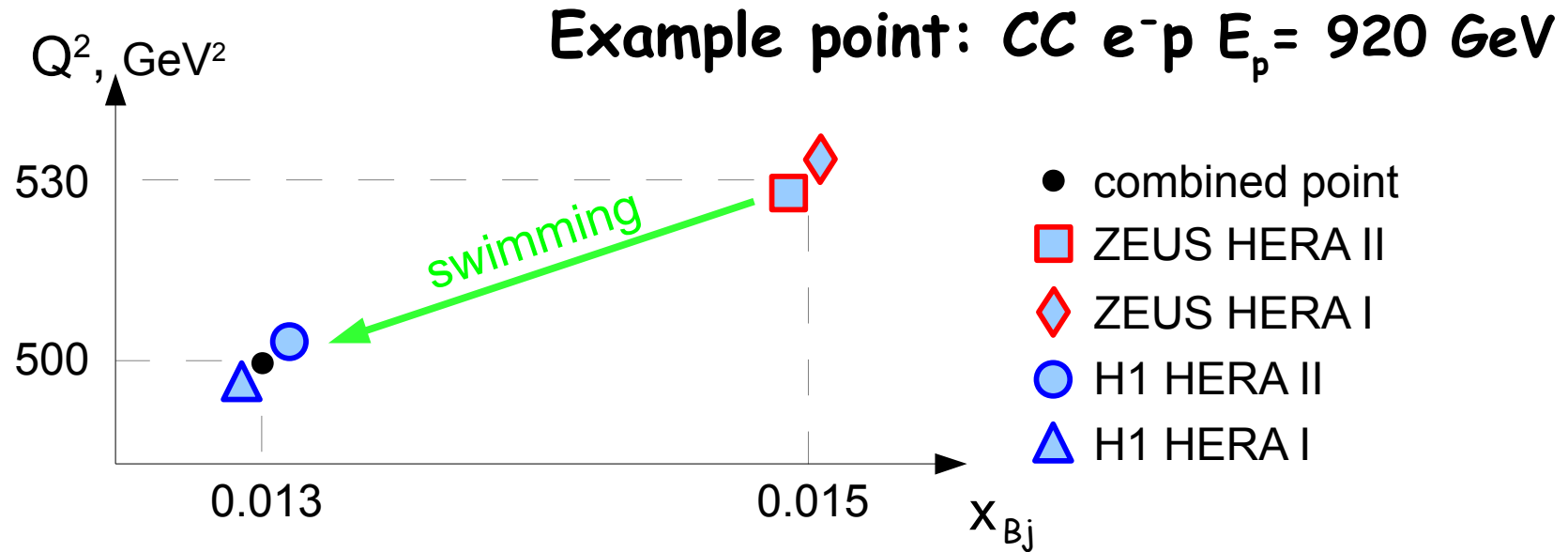
H1 and ZEUS

Two separate grids



- inclusive grid, for $E_p = 920 \text{ GeV}$ and $E_p = 820 \text{ GeV}$ data sets
- fine- x_{Bj} grid, for $E_p = 575 \text{ GeV}$ and $E_p = 460 \text{ GeV}$ data sets
- 1307 grid points
 - $0.045 < Q^2 < 50000 \text{ GeV}^2$
 - $6 \times 10^{-07} < x_{Bj} < 0.65$

Swimming procedure



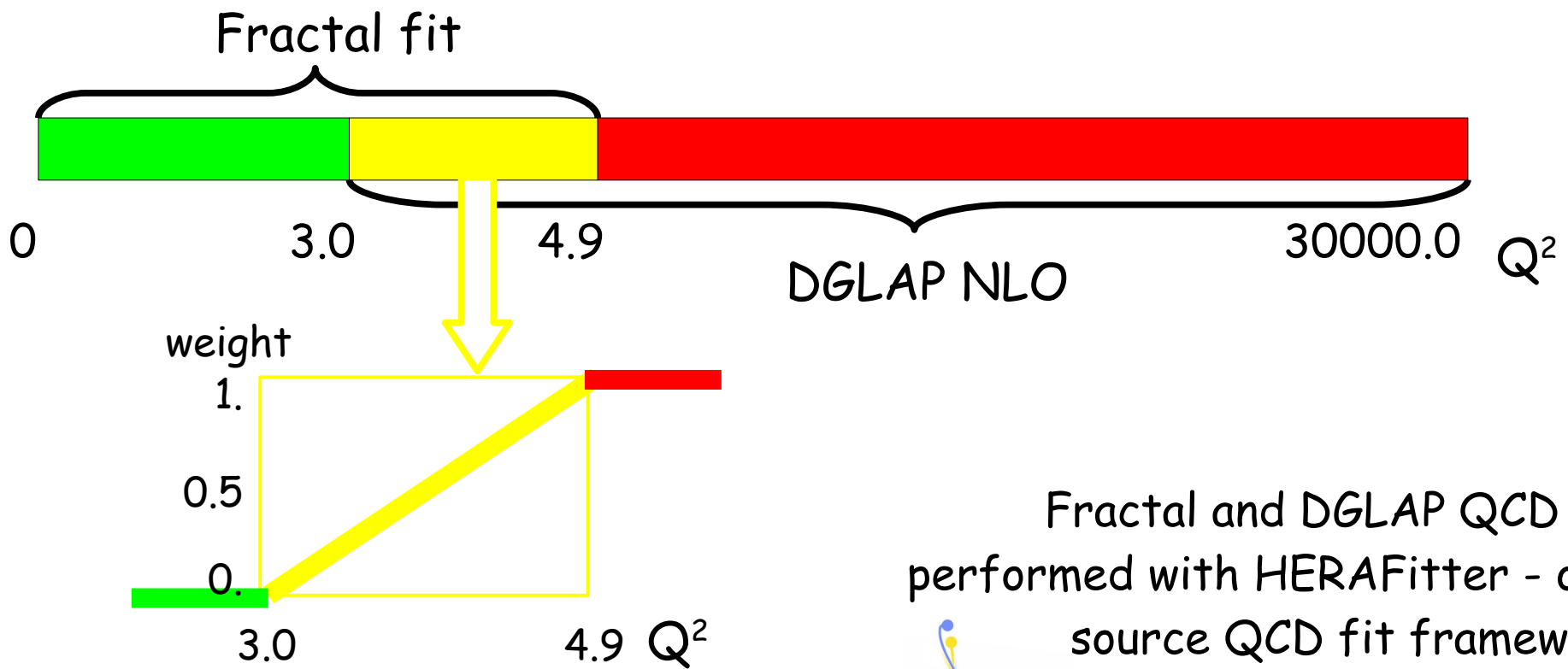
- **Swimming factors**

$$\sigma_{\text{meas}}^{e\bar{p}}(X_{\text{grid}}, Q_{\text{grid}}^2) = \frac{\sigma_{\text{model}}^{e\bar{p}}(X_{\text{grid}}, Q_{\text{grid}}^2)}{\sigma_{\text{model}}^{e\bar{p}}(X_{\text{meas}}, Q_{\text{meas}}^2)} \cdot \sigma_{\text{meas}}^{e\bar{p}}(X_{\text{meas}}, Q_{\text{meas}}^2)$$

- We need model for swimming
- Swimming factors are usually at level of few %

Swimming procedure

- Swimming done iteratively using our own data
 - 1st iteration uncombined HERAI+II data, later - combined data
 - Convergence after 3 iterations



Fractal and DGLAP QCD fits performed with HERAFitter - open source QCD fit framework:
www.herafitter.org



Averaging of scale factors performed as a function of Q^2

Averaging procedure

- Combination done using HERAverager: wiki-zeuthen.desy.de/HERAverager

$$\chi_{\text{exp},ds}^2(\mathbf{m}, \mathbf{b}) = \sum_i \frac{\left[m^i - \sum_j \gamma_j^{i,ds} m^i b_j - \mu^{i,ds} \right]^2}{\delta_{i,ds,stat}^2 \mu^{i,ds} \left(m^i - \sum_j \gamma_j^{i,ds} m^i b_j \right) + \left(\delta_{i,ds,uncor} m^i \right)^2} + \sum_j b_j^2$$

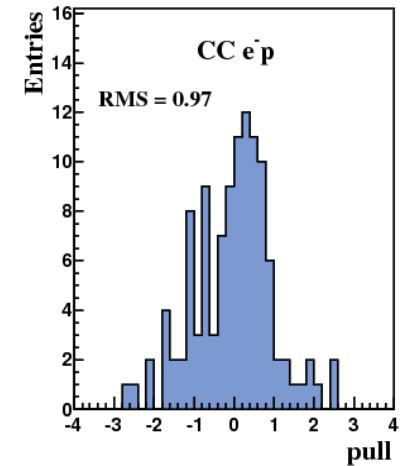
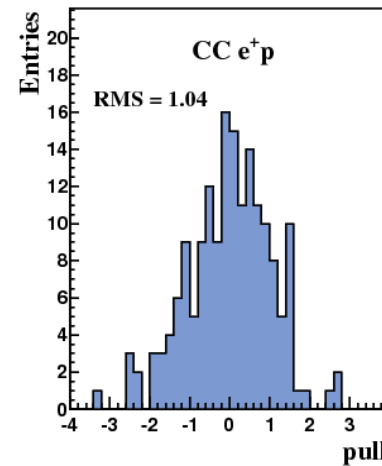
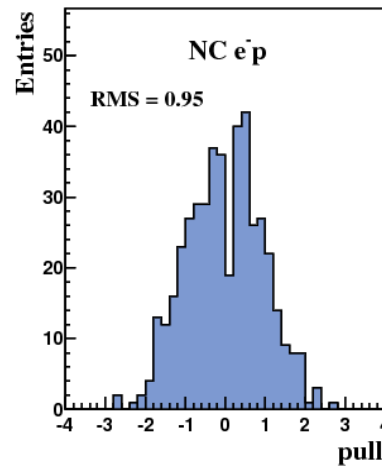
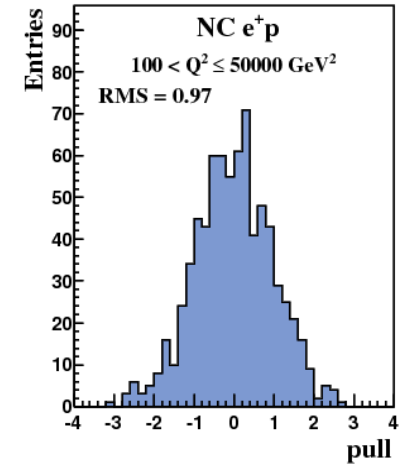
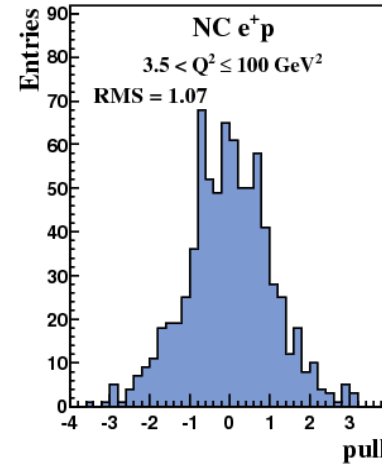
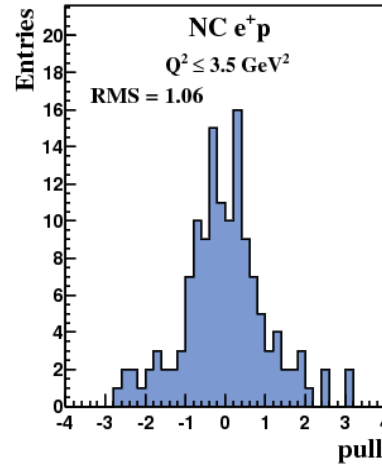
- **162** correlated systematic sources taken into account
 - treated as multiplicative
- Output
 - **7 data samples for $e^\pm p$, NC and CC, 3 CMEs**
 - Statistical and uncorrelated systematic uncertainties
 - 162 correlated statistical uncertainties
 - 7 procedural uncertainties calculated → see additional material

Averaging results

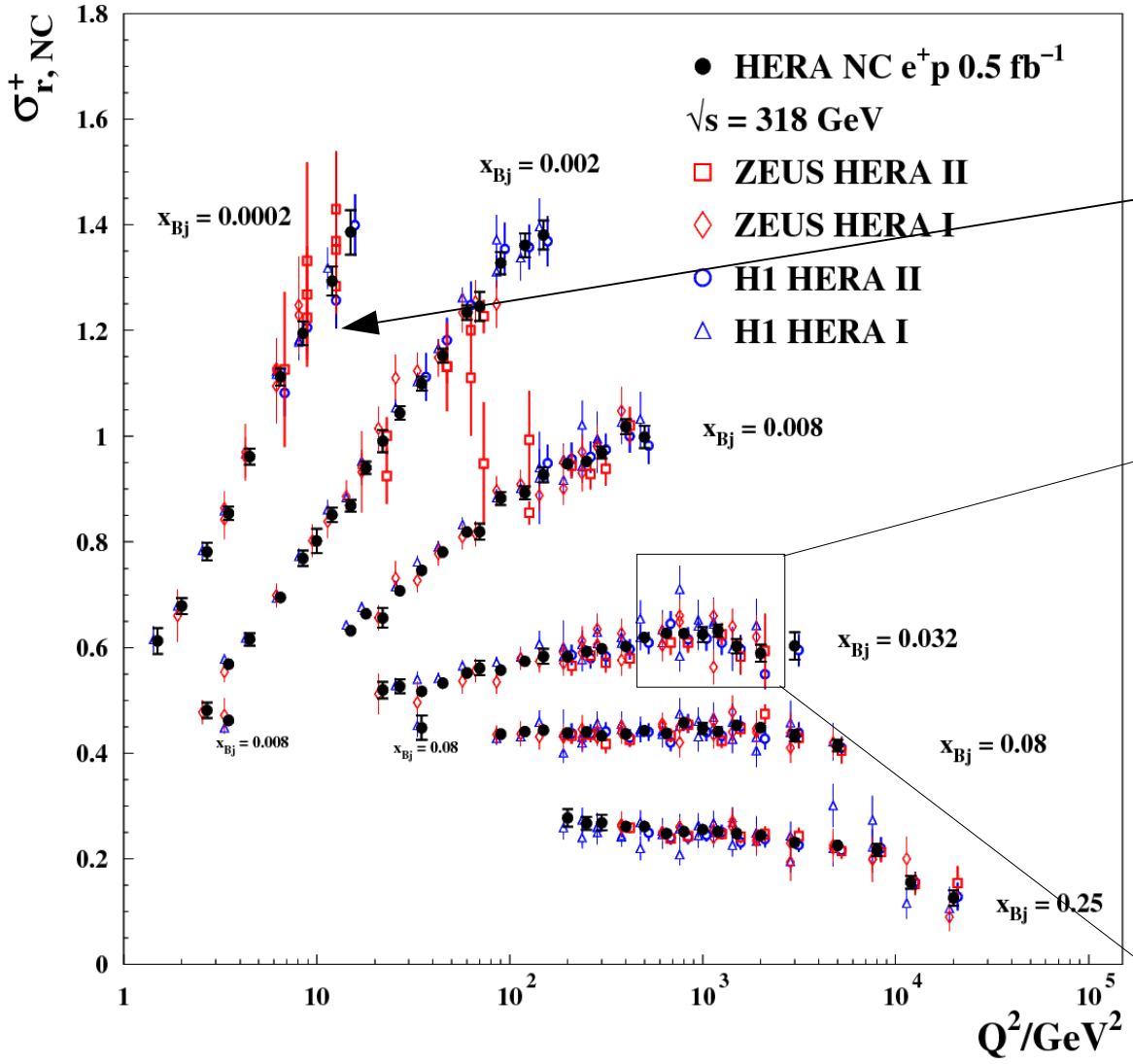
- Good data consistency: $\chi^2/\text{dof} = 1687/1620$

$$p^{i,k} = \frac{\mu^{i,k} - \mu^i \left(1 - \sum_j \gamma_j^{i,k} b'_j\right)}{\sqrt{\Delta_{i,k}^2 - \Delta_i^2}}$$

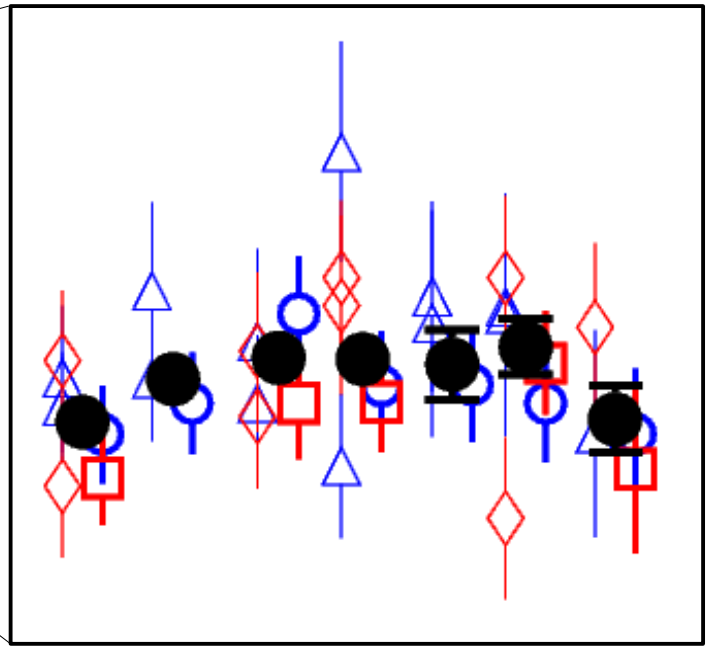
H1 and ZEUS



H1 and ZEUS

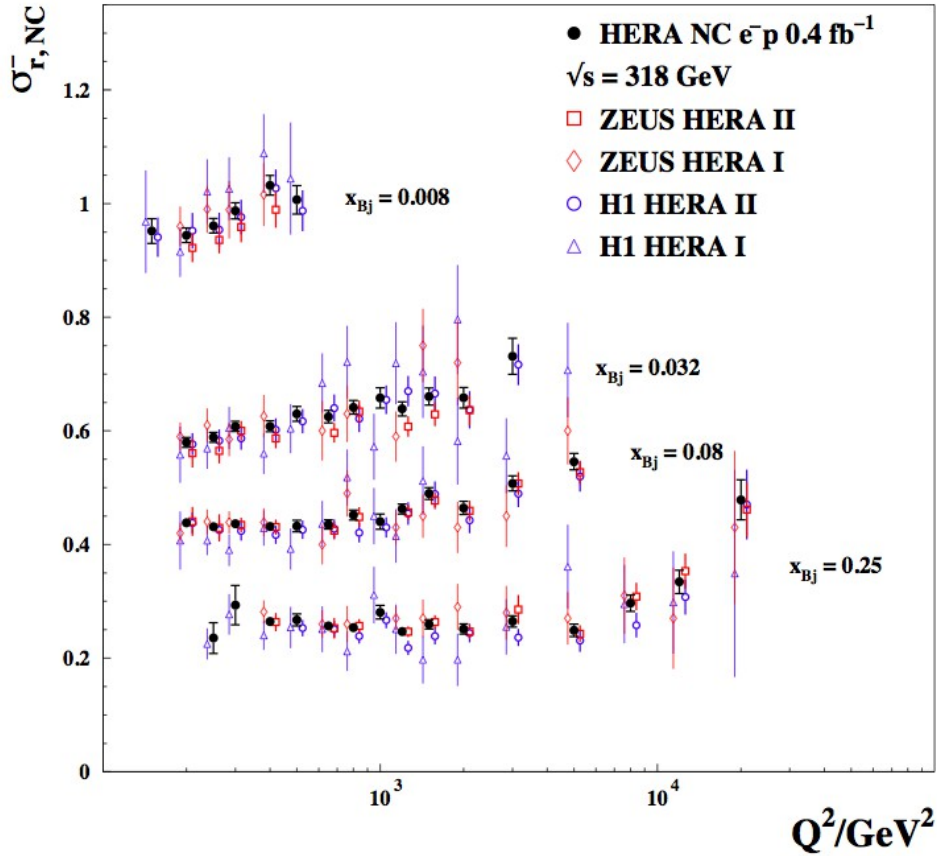


- 2927 data points combined to 1307
- Up to 6-8 data points combined to 1

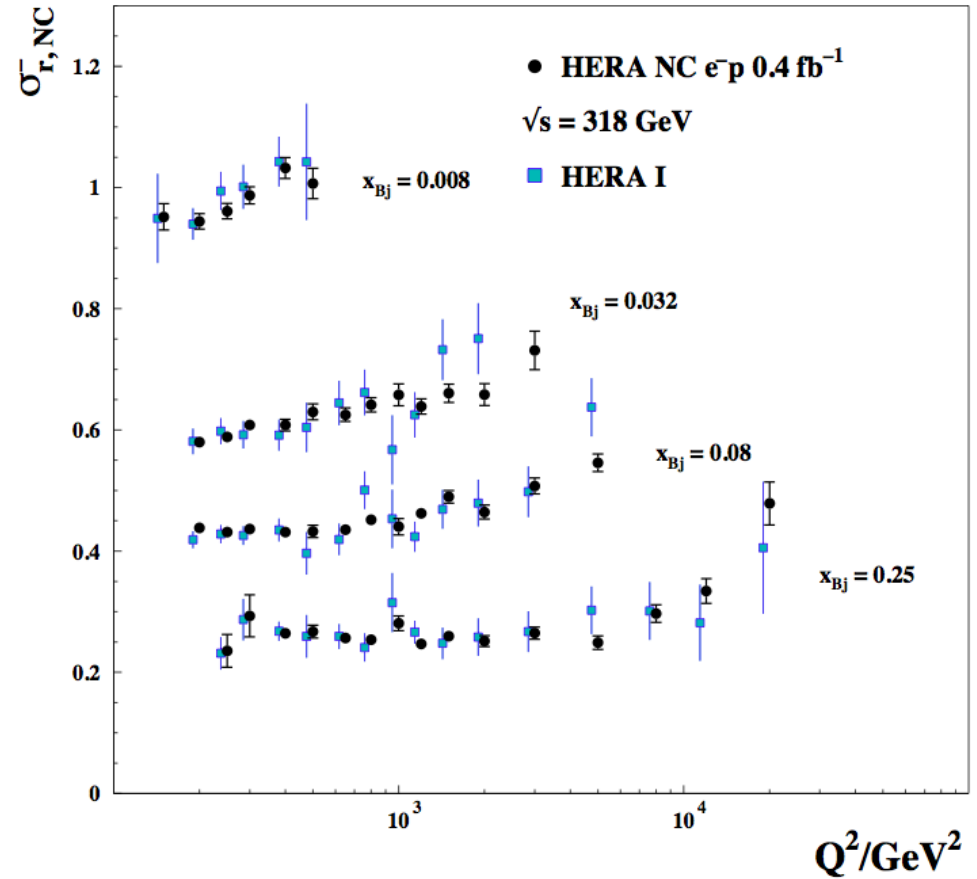


Improved precision

H1 and ZEUS



H1 and ZEUS



- Largest and most accurate data sample is for the NC $e+p$ process
- The combined data accuracy reaches $\sim 1\%$
- Largest improvement for NC $e+p$ - 10 times more luminosity
- Consistent with HERA-I + improved uncertainties

Improving previous results

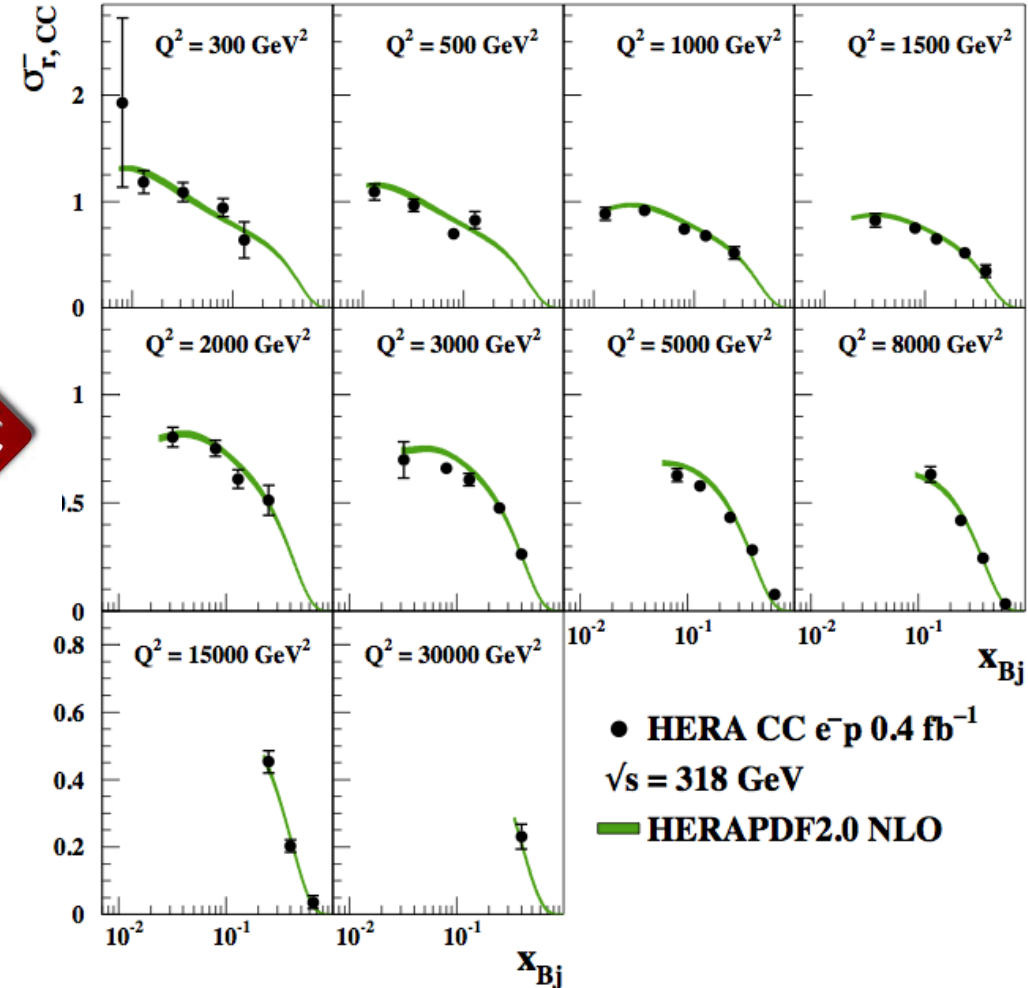
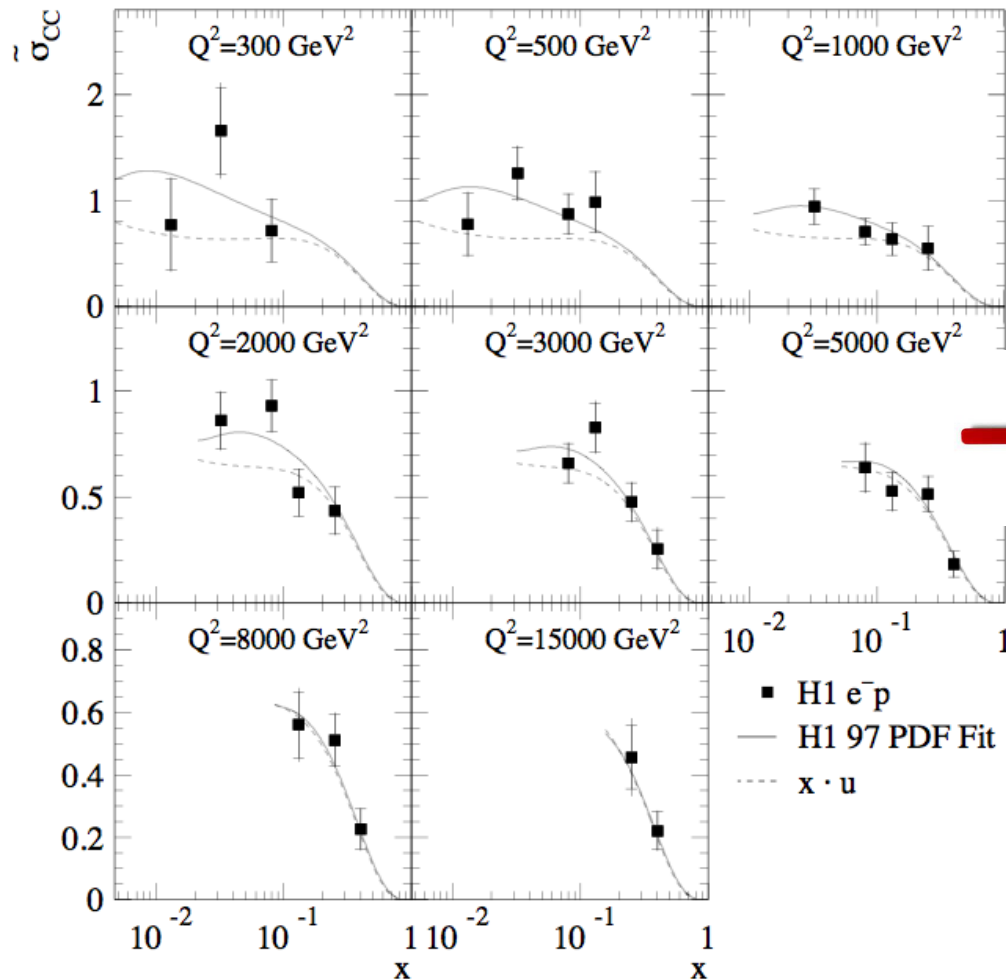
H1 Charged Current

2001



2015

H1 and ZEUS



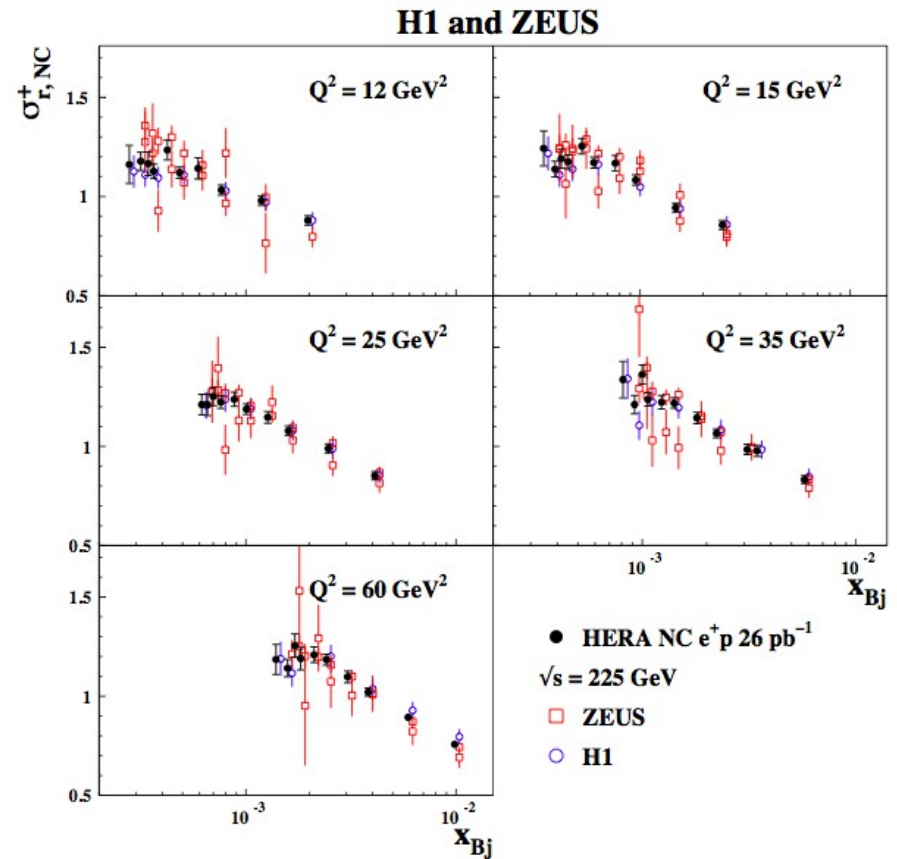
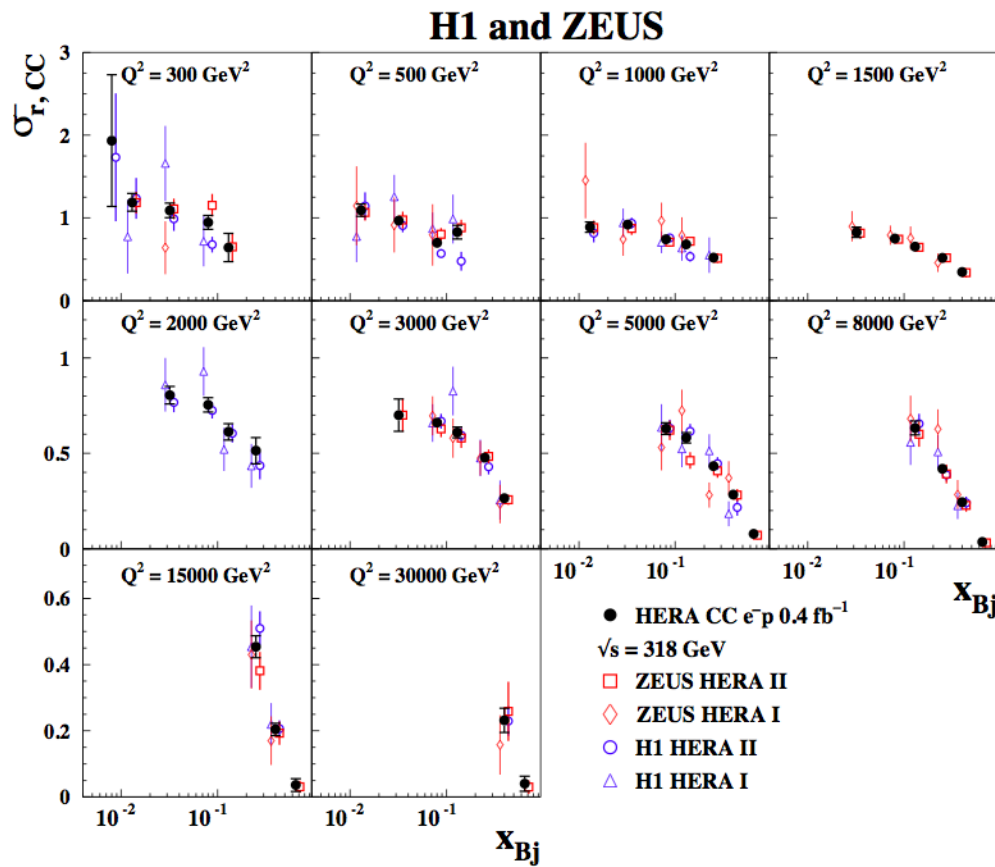
- increases statistical significance
- reduces systematic uncertainties via cross calibration techniques

Great gain in precision

New kinematic ranges explored

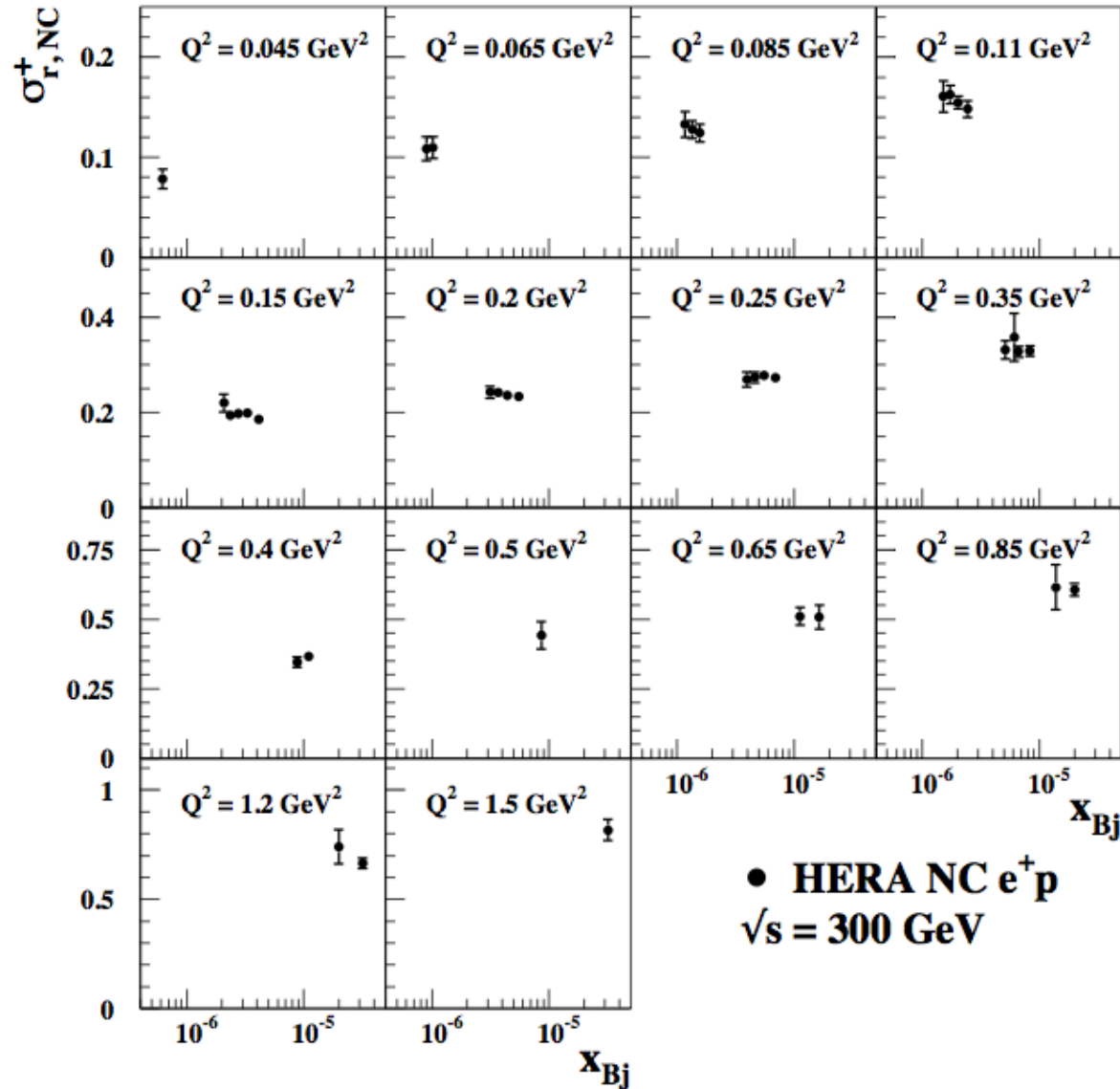
- Kinematic range extended for existing data samples

- Low energies added: $CME = 225$ GeV and 251 GeV



Low Q^2 combined data

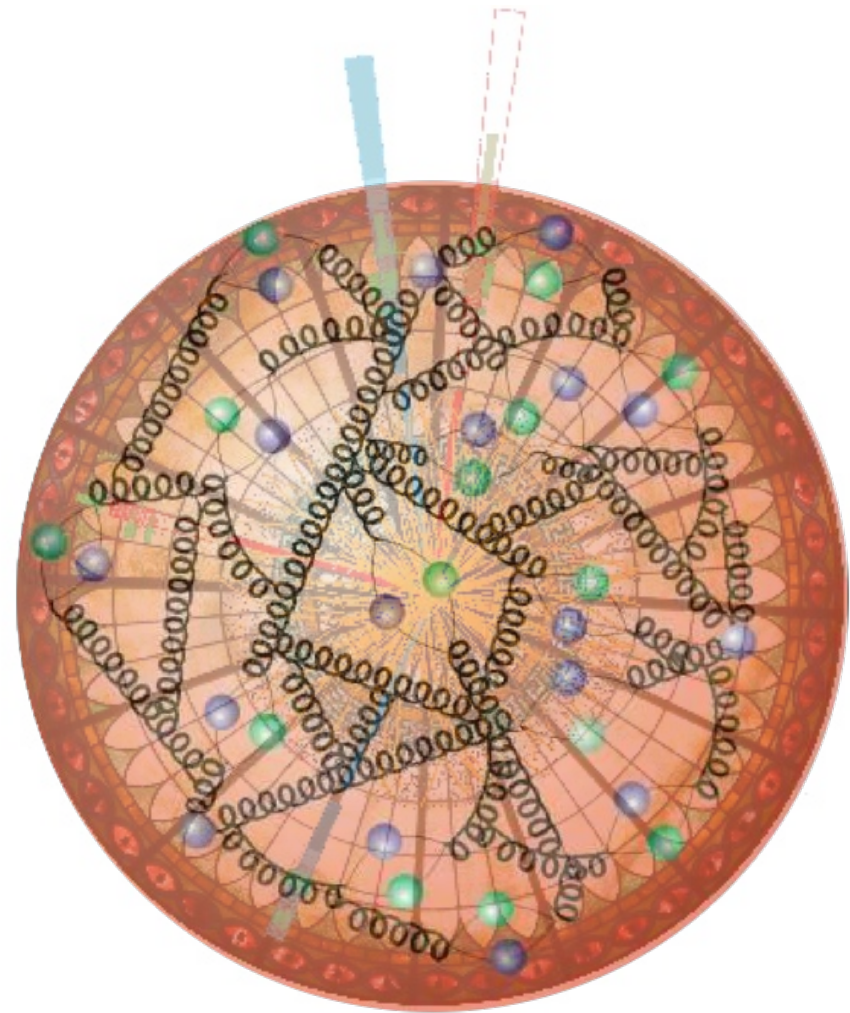
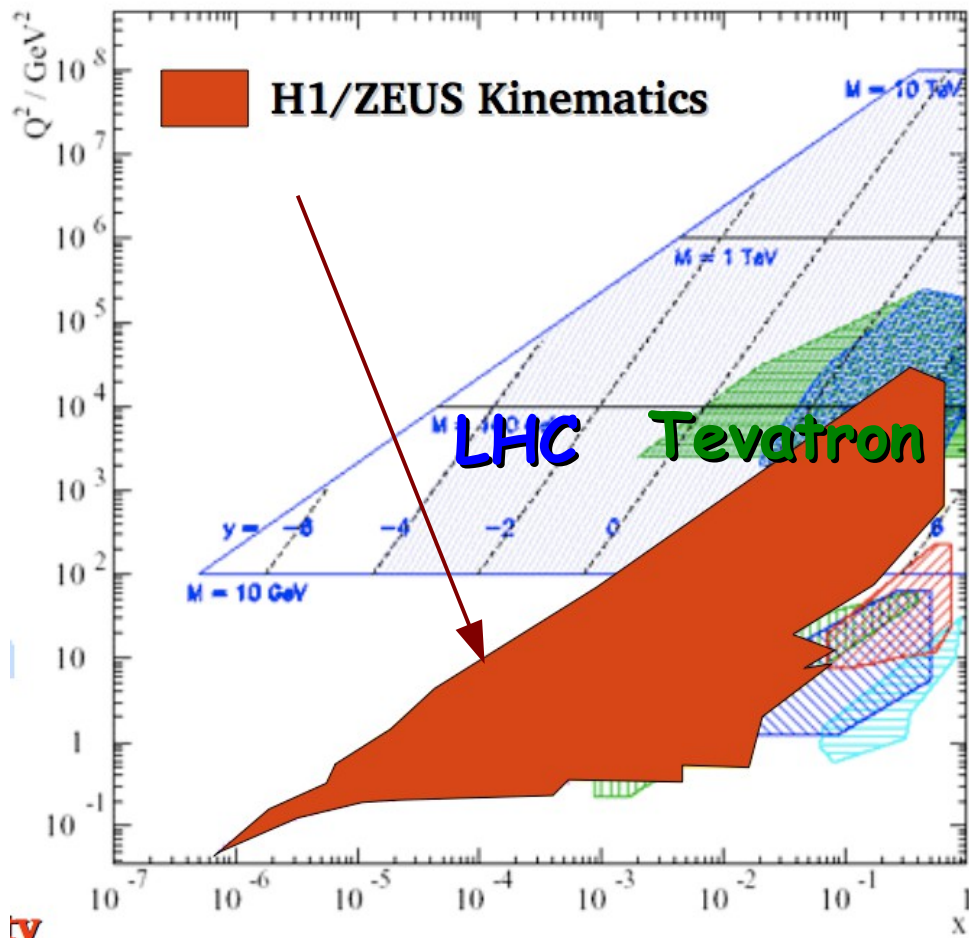
H1 and ZEUS



- Combined inclusive cross sections for low Q^2
- Available for two CMEs
 - 300 GeV
 - 318 GeV
- Interesting for
 - dipole/saturation models
 - studying higher twists

Proton structure

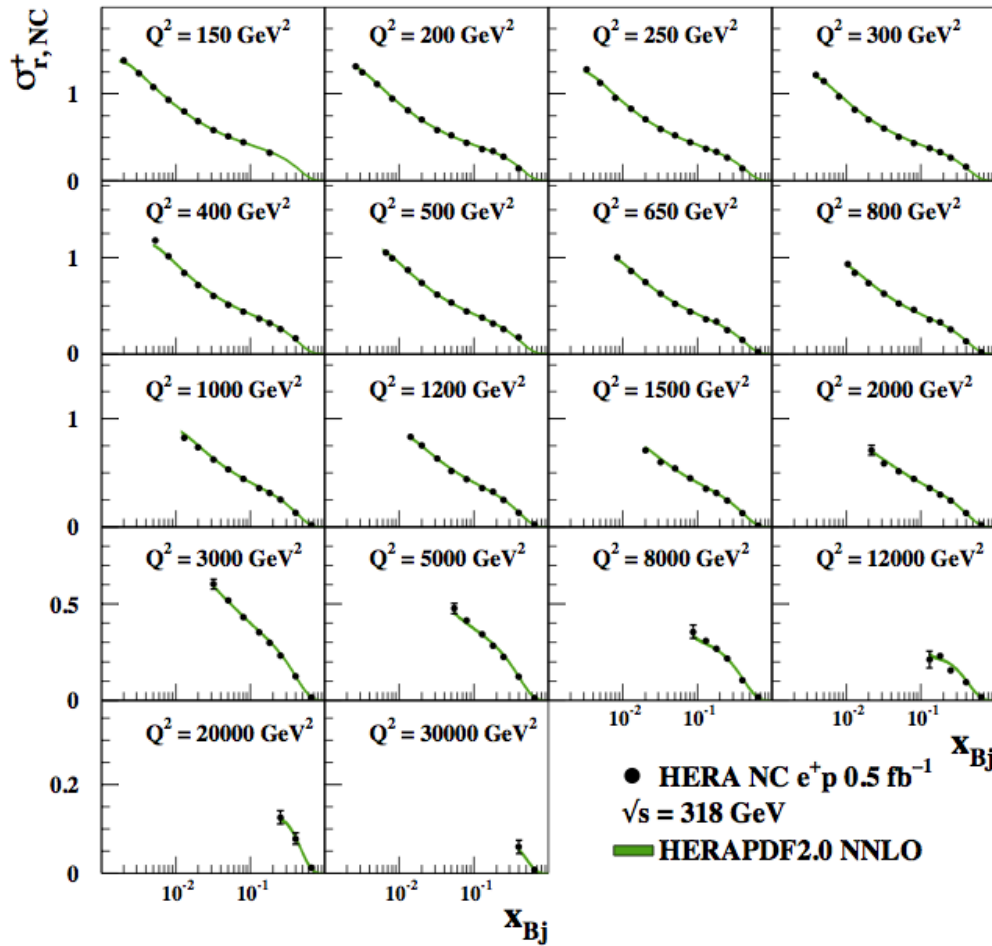
Inclusive measurements from HERA are core of every parton density extraction



Neutral Current

$$\frac{d^2\sigma_{NC}^{\pm}}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left[Y_+ F_2 \mp Y_- xF_3 - y^2 F_L \right]$$

H1 and ZEUS



Proton structure functions

$$F_2 = x \sum e_q^2 [q(x) + \bar{q}(x)]$$

- Sensitive to quarks

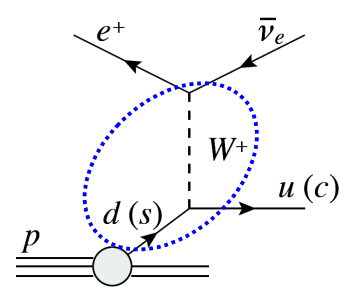
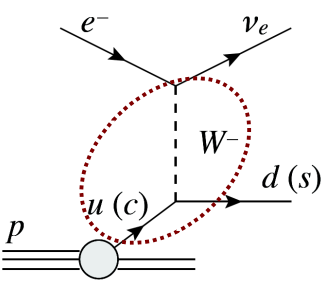
$$xF_3 = x \sum 2e_q a_q [q(x) - \bar{q}(x)]$$

- Sensitive to valence distributions

$$F_L \sim \alpha_s x g$$

- Sensitive to gluon
- Gluon also from scaling violation and charm+jet data

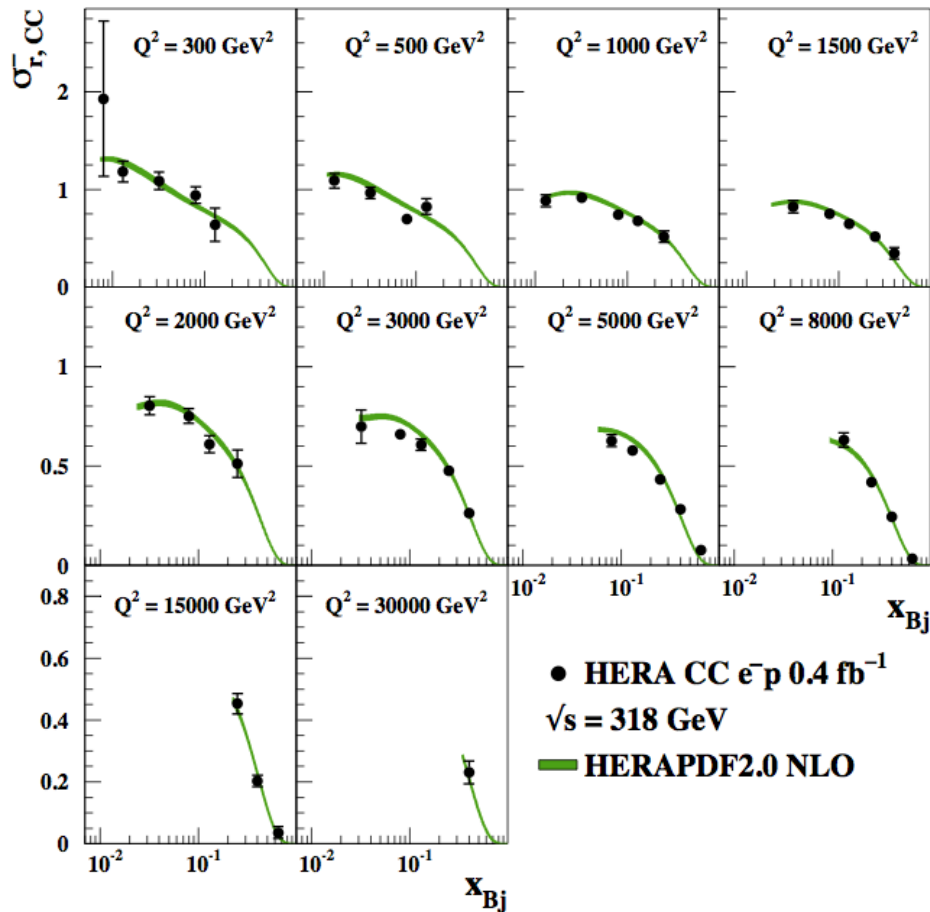
Charge Current: flavor decomposition



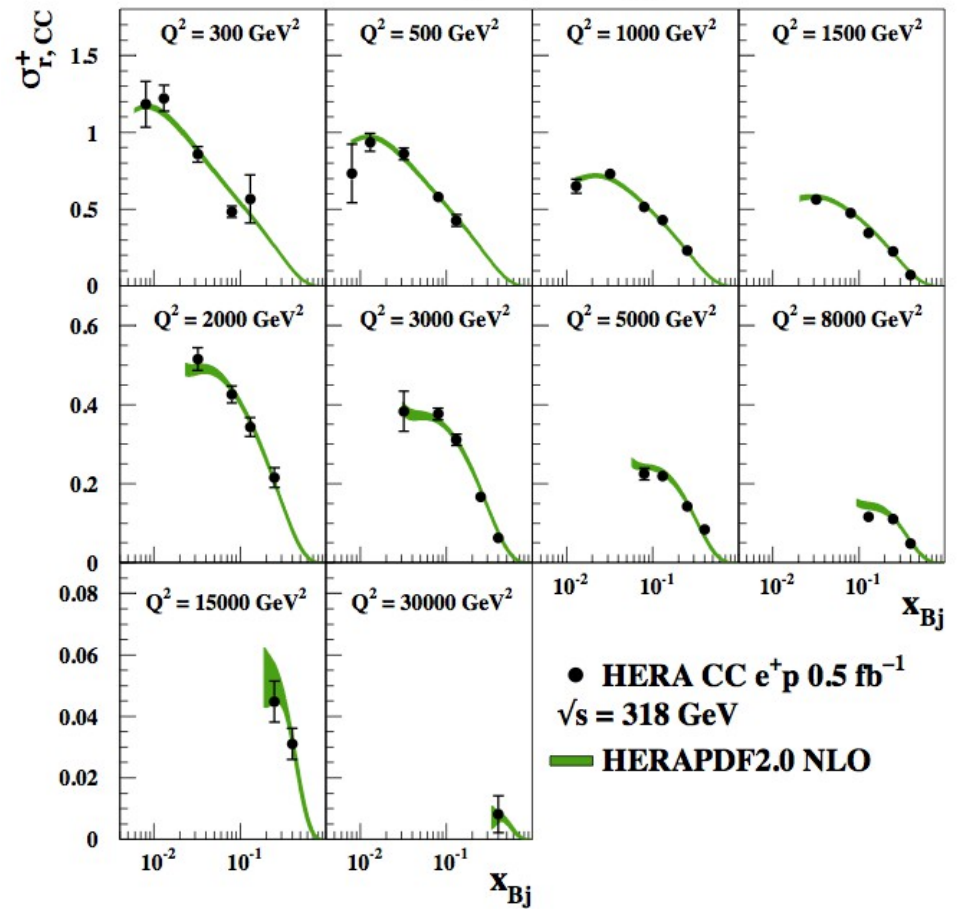
$$\sigma_{CC}^- \sim x[u + c] + x(1 - y)^2[\bar{d} + \bar{s}]$$

$$\sigma_{CC}^+ \sim x[\bar{u} + \bar{c}] + x(1 - y)^2[d + s]$$

H1 and ZEUS

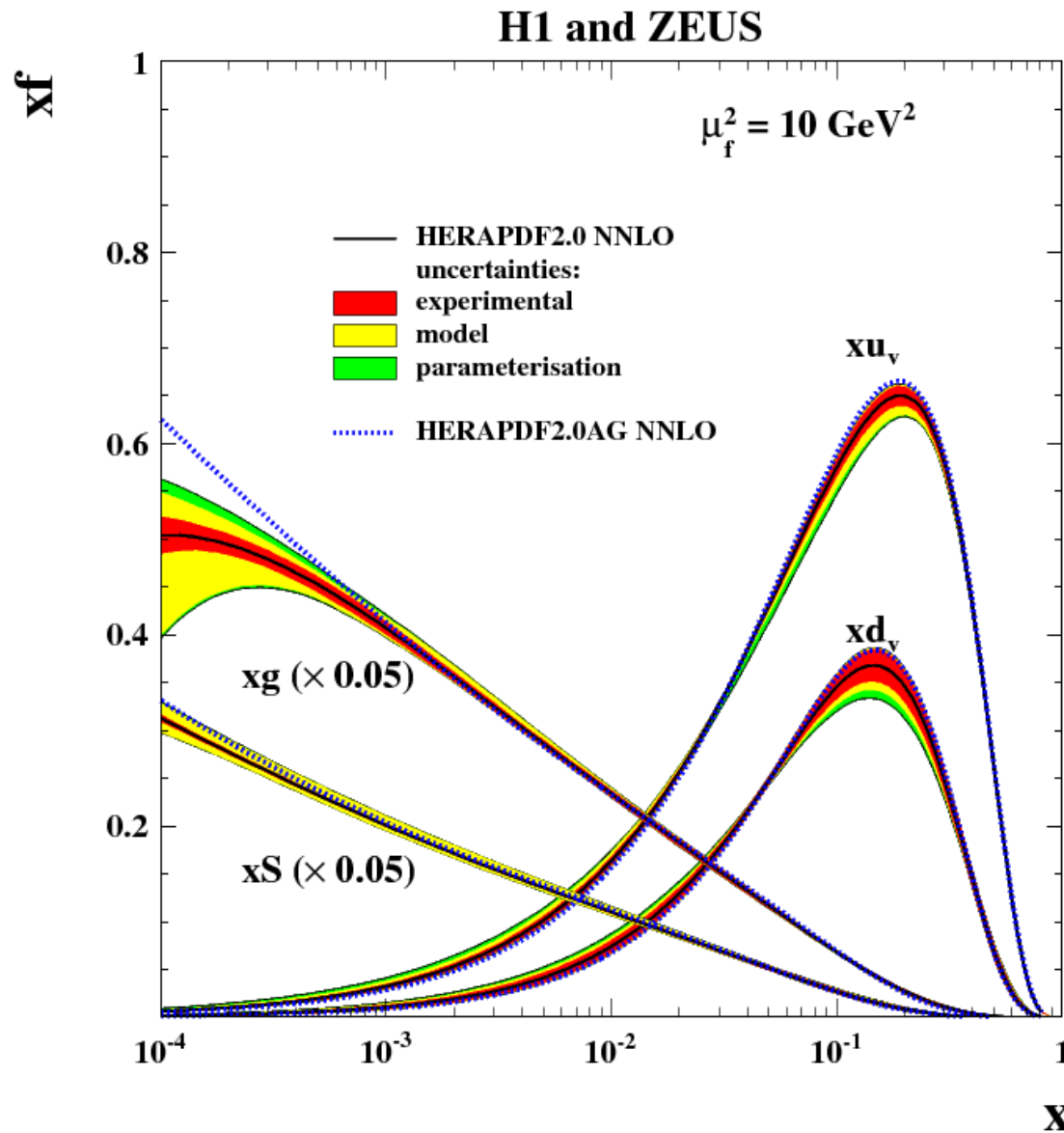


H1 and ZEUS



HERAPDF2.0

- HERAPDF2.0 used HERA data only → see talk of V. Myronenko





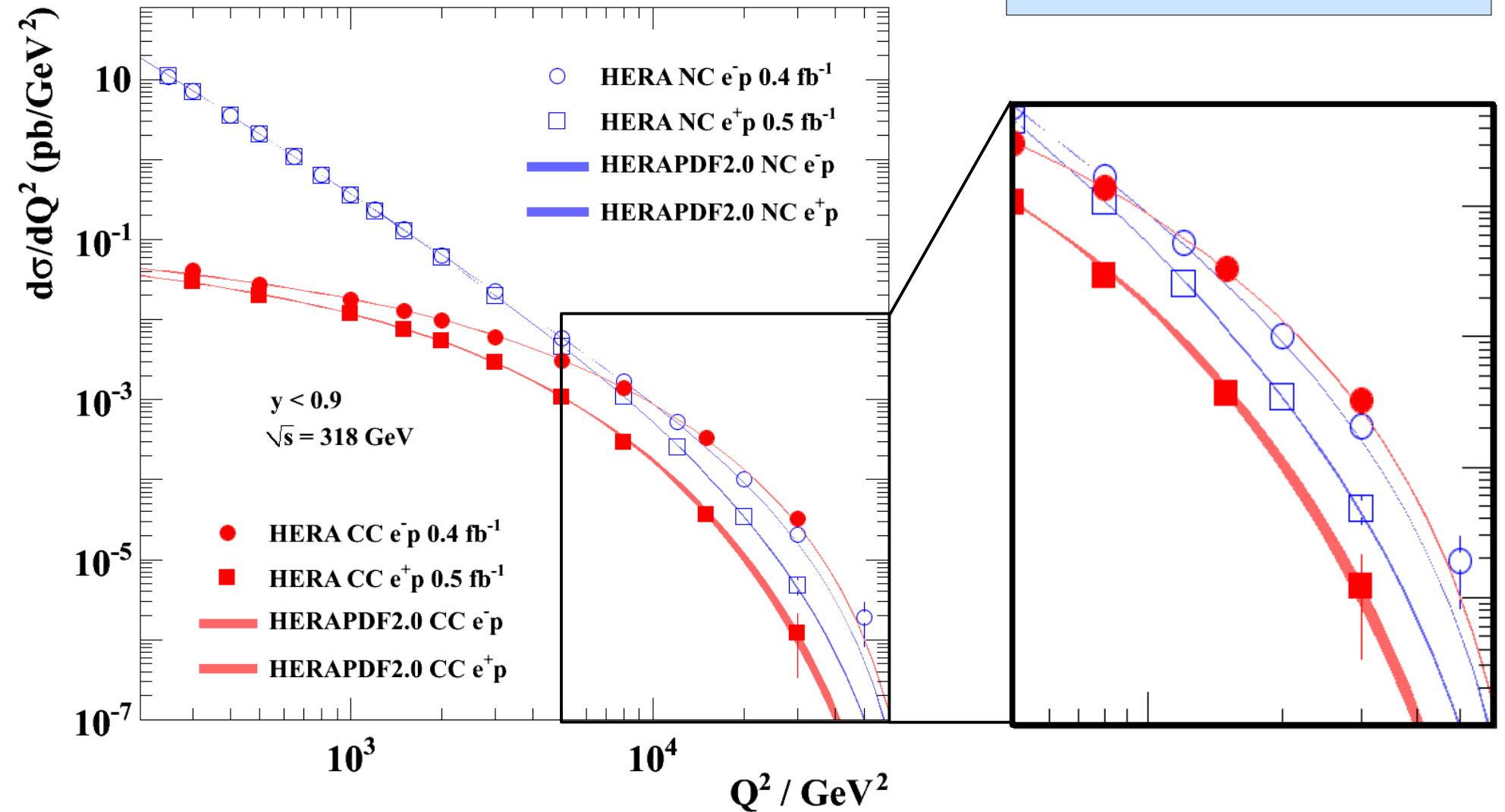
~~MORTAL KOMBAT~~

HERA LEGACY

Electroweak unification

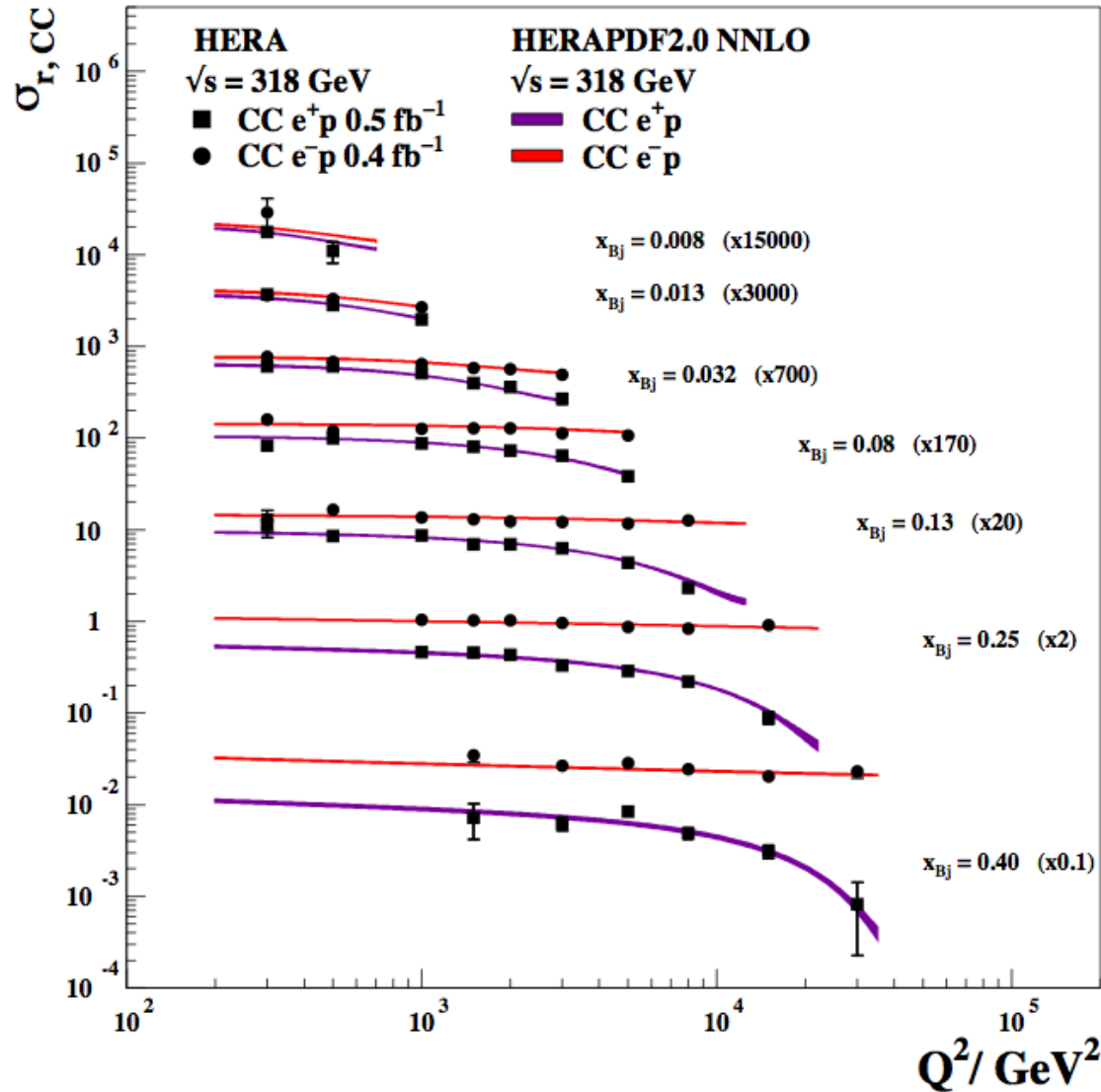
H1 and ZEUS

Fantastic precision of HERA final data



CC: helicity effects

H1 and ZEUS



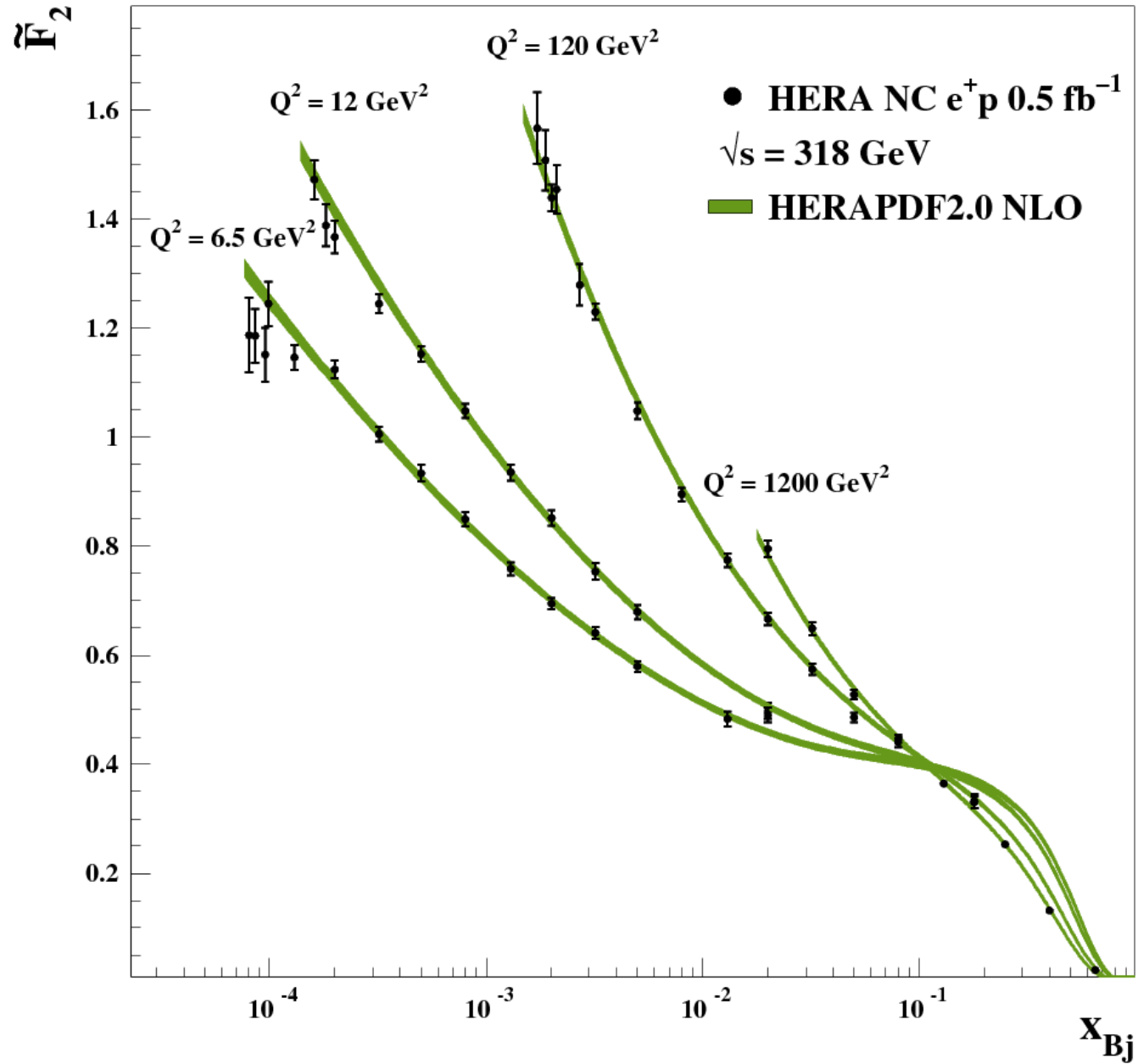
$$\sigma_{CC}^+ \sim x[\bar{u} + \bar{c}] + x(1-y)^2[d + s]$$

$$\sigma_{CC}^- \sim x[u + c] + x(1-y)^2[\bar{d} + \bar{s}]$$

- e^+p : d_v quarks are suppressed at high Q^2
- e^+p : helicity factor applies to sea quarks only

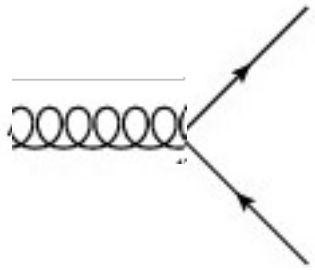
Low-x rise of F_2

H1 and ZEUS

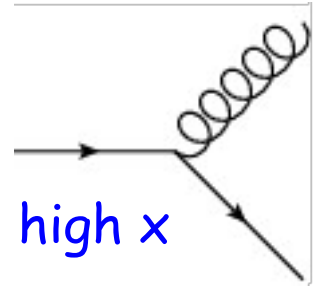
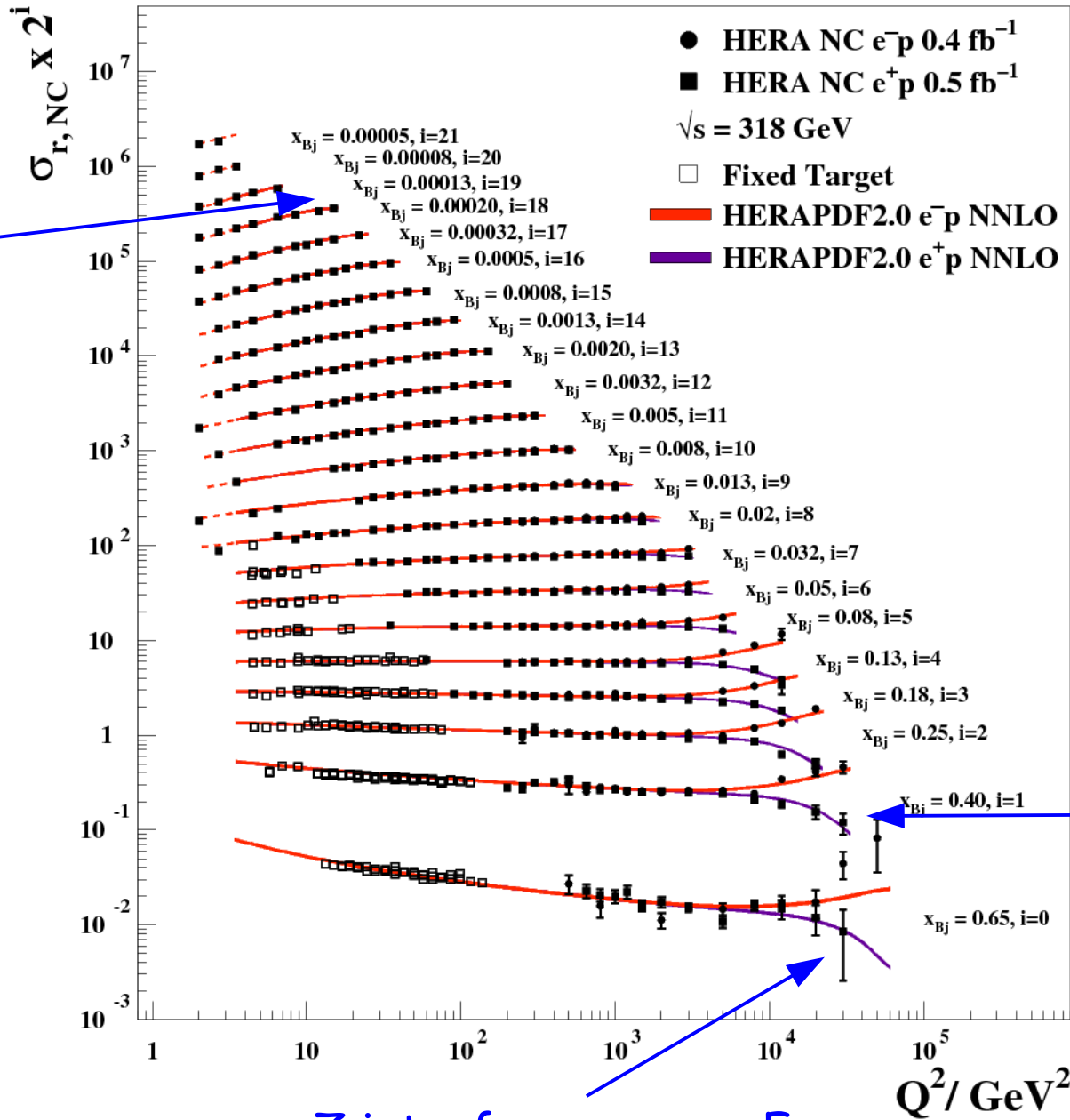


QCD and electroweak effects

H1 and ZEUS



@ low x

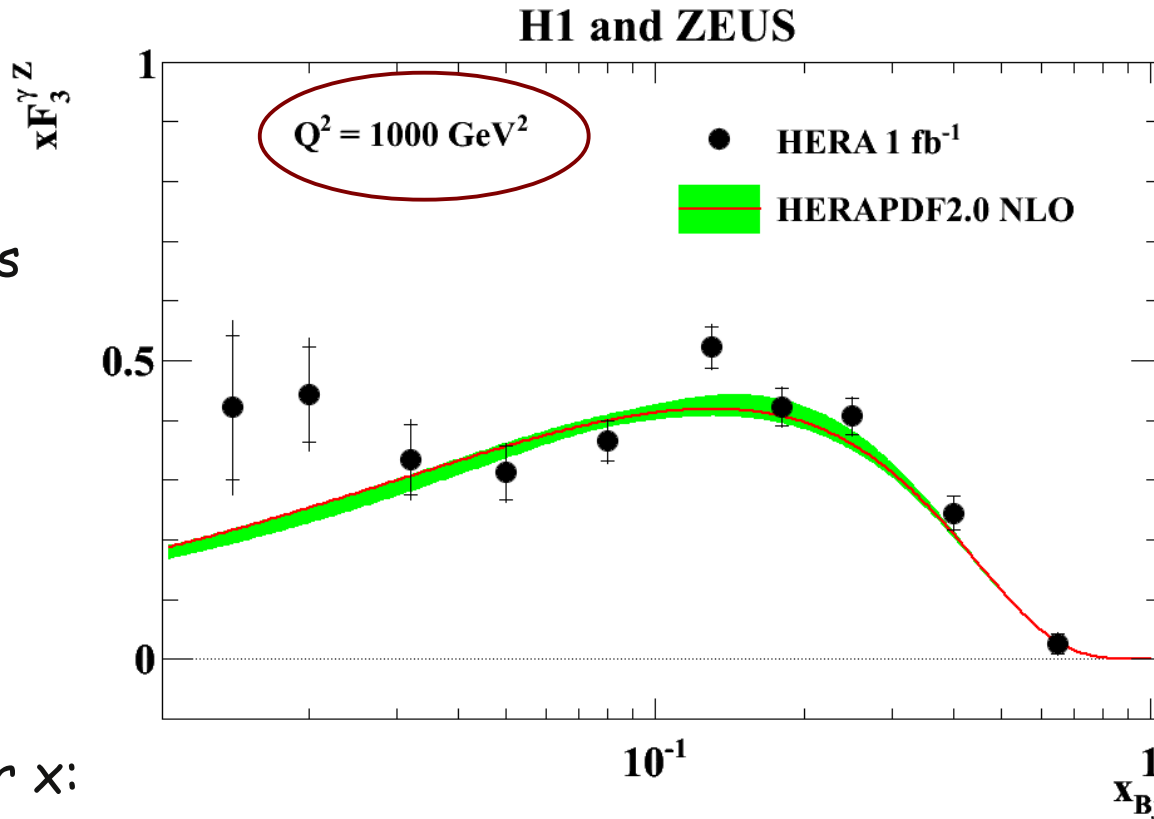


@ high x

γZ interference $\rightarrow xF_3$

$x F_3^{gZ}$ from combined data

- $x F_3^{gZ}$ from subtracting the NC e^+p from the NC e^-p cross sections
- Function of x_{Bj} in bins of Q^2
- Weak Q^2 dependence \rightarrow translated to $Q^2 = 1000 \text{ GeV}^2$ and averaged



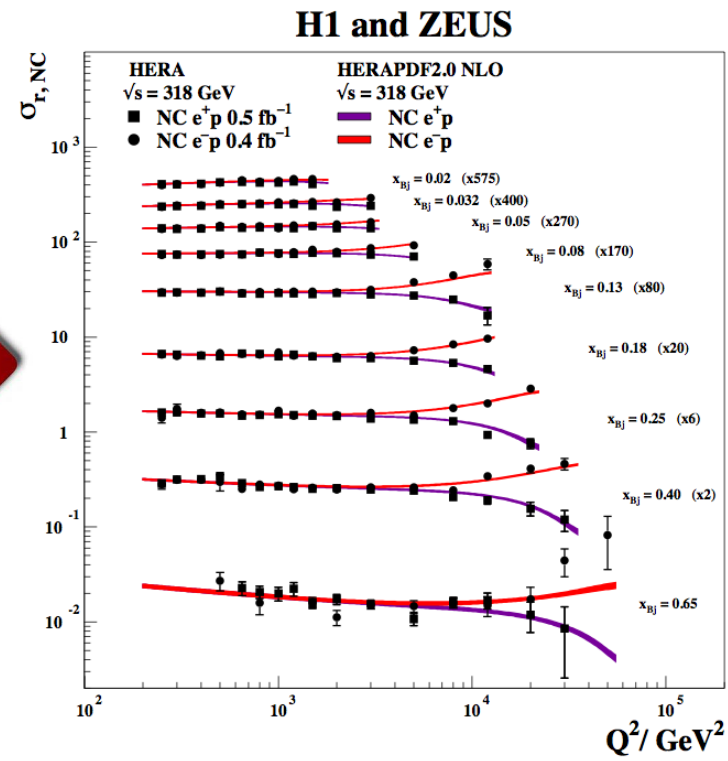
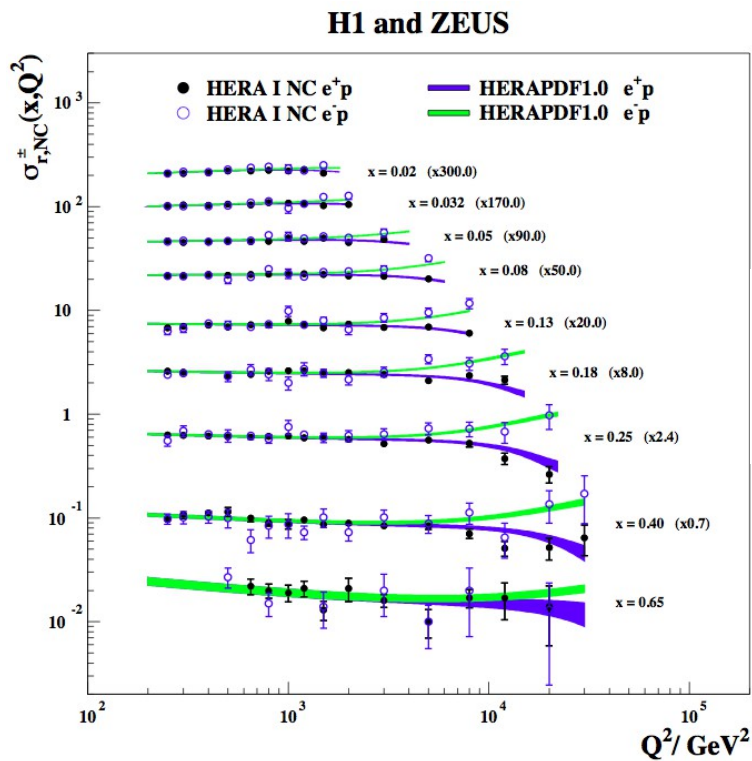
- Good agreements with predictions

- Integrated over x :

$0.016 < x_{Bj} < 0.725$	HERAPDF2.0 : $1.165^{+0.042}_{-0.053}$	Data : $1.314 \pm 0.057(\text{stat}) \pm 0.057(\text{syst})$
$0 < x_{Bj} < 1$	HERAPDF2.0 : $1.588^{+0.078}_{-0.100}$	Data : $1.790 \pm 0.078(\text{stat}) \pm 0.078(\text{syst})$
	QPM: 5/3	

Summary

- HERA combined measurements of inclusive DIS final
- Combined HERA data set provides ultimate sample for inclusive neutral and charged current cross section studies in wide kinematic range.
 - HERAPDF2.0 PDF based on final combination
 - Low Q^2 data provide additional checks of the QCD calculations
- Plethora of beautiful physics seen in inclusive DIS measurements
 - HERA legacy of almost 25 years of activity



Additional slides

Procedural uncertainties

- Combination done using HERAverager: wiki-zeuthen.desy.de/HERAverager

$$\chi_{\text{exp},ds}^2(\mathbf{m}, \mathbf{b}) = \sum_i \frac{\left[m^i - \sum_j \gamma_j^{i,ds} m^i b_j - \mu^{i,ds} \right]^2}{\delta_{i,ds,stat}^2 \mu^{i,ds} \left(m^i - \sum_j \gamma_j^{i,ds} m^i b_j \right) + \left(\delta_{i,ds,uncor} m^i \right)^2} + \sum_j b_j^2$$

- 162** correlated systematic sources taken into account
 - treated as multiplicative

- Procedural errors calculated
 - multiplicative vs additive
 - possible correlations between data sets (H1/ZEUS, HERAI/HERAII)
 - photoproduction background
 - hadronic energy scale
 - connected with large pulls in combinator

H1 and ZEUS

