

# QCD and electroweak fits to HERA inclusive DIS data



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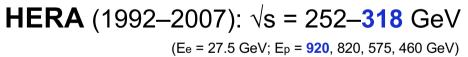
on behalf of the ZEUS Collaboration

Phys Rev D94 (2016) 052007

I. Abt, A.M. Cooper-Sarkar, B. Foster, C. Gwenlan, V. Myronenko, O. Turkot, K. Wichmann

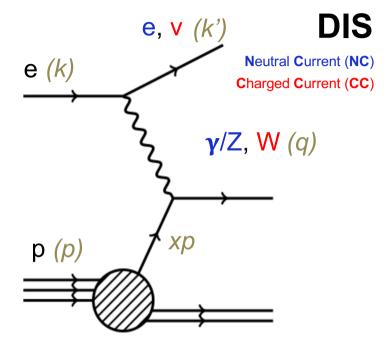
# HERA: the world's only ep collider





two general purpose detectors, **H1** and **ZEUS** collected 0.5 fb<sup>-1</sup> per experiment, equally between e<sup>+</sup> and e<sup>-</sup>

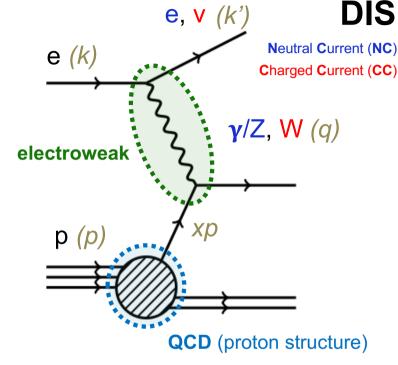
HERA-II (02–07): polarised lepton beams; crucial for electroweak measurements



$$\begin{aligned} Q^2 &= -q^2 = -(k-k')^2 \\ \text{Virtuality of the exchanged boson} \\ x &= \frac{Q^2}{2p \cdot q} \text{ Bjorken scaling parameter} \\ y &= \frac{p \cdot q}{p \cdot k} \text{ Inelasticity parameter} \\ s &= (k+p)^2 = \frac{Q^2}{xy} \text{ Invariant c.o.m.} \end{aligned}$$

# HERA: the world's only ep collider





**HERA** (1992–2007):  $\sqrt{s} = 252$ –318 GeV (Ee = 27.5 GeV; Ep = 920, 820, 575, 460 GeV)

two general purpose detectors, **H1** and **ZEUS** collected 0.5 fb<sup>-1</sup> per experiment, equally between e<sup>+</sup> and e<sup>-</sup>

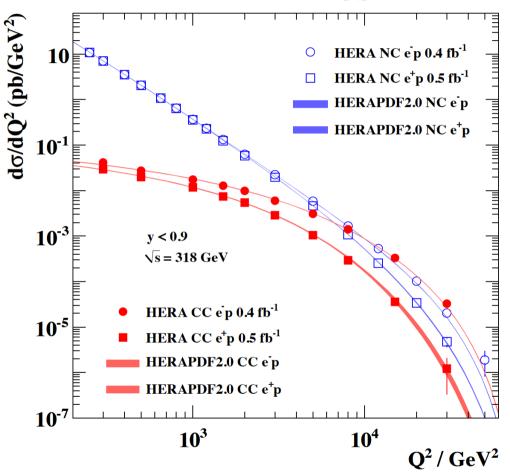
HERA-II (02–07): polarised lepton beams; crucial for electroweak measurements

#### Deep Inelastic Scattering at HERA:

- a super-microscope to study
   proton structure (PDFs)
- sensitive to EW via t-channel gauge boson exchange

#### HERA inclusive NC and CC DIS data





HERA data combination H1 and ZEUS Colls., EPJ C75 (2015), 580

extraordinary
precision of final
HERA
measurements!

$$Y_{+} = 1 \pm (1 - y)^{2}$$

$$\mathbf{NC:} \quad \sigma_{r,\mathrm{NC}}^{e^{\pm}p} = \frac{x_{\mathrm{Bj}}Q^4}{2\pi\alpha_0^2} \frac{1}{Y_+} \frac{d^2\sigma(e^{\pm}p)}{dx_{\mathrm{Bj}}dQ^2} = \tilde{F}_2(x_{\mathrm{Bj}},Q^2) \mp \frac{Y_-}{Y_+} x \tilde{F}_3(x_{\mathrm{Bj}},Q^2) - \frac{y^2}{Y_+} F_L(x_{\mathrm{Bj}},Q^2)$$

(similar equation for **CC** cross section)

# NC polarised DIS

NC: γZ interference and Z exchange affected by e-beam polarisation

$$P_e = \frac{N_R - N_L}{N_R + N_L}$$

$$\tilde{F}_{2}^{\pm} = F_{2}^{\gamma} - (v_{e} \pm P_{e}a_{e})\chi_{Z}F_{2}^{\gamma Z} + (v_{e}^{2} + a_{e}^{2} \pm 2P_{e}v_{e}a_{e})\chi_{Z}^{2}F_{2}^{Z} \qquad v_{e} = -1/2 + 2\sin^{2}\theta_{W}$$

$$a_{e} = -1/2$$

$$x\tilde{F}_{3}^{\pm} = -(a_{e} \pm P_{e}v_{e})\chi_{Z}xF_{3}^{\gamma Z} + (2v_{e}a_{e} \pm P_{e}(v_{e}^{2} + a_{e}^{2}))\chi_{Z}^{2}xF_{3}^{Z}$$

$$v_e = -1/2 + 2\sin^2\theta_W$$
$$a_e = -1/2$$

**NC** structure functions in QPM:

sensitive to EW vector and axial-vector couplings

to **light quarks**, and **sin<sup>2</sup>θw** via

$$[F_2^{\gamma},F_2^{\gamma Z},F_2^{Z}] = \sum_q [e_q^2,2e_qv_q,v_q^2+a_q^2]x(q+\bar{q})$$
 to light quarks, and  $\sin^2\theta$ w via 
$$[xF_3^{\gamma Z},xF_3^{Z}] = \sum_q [e_qa_q,v_qa_q]2x(q-\bar{q})$$
 
$$\chi_Z = \frac{1}{\sin^22\theta_W}\frac{Q^2}{M_Z^2+Q^2}\frac{1}{1-\Delta R}$$
 (where  $\Delta$ R accounts for radiative corrections)

$$\chi_Z = \frac{1}{\sin^2 2\theta_W} \frac{Q^2}{M_Z^2 + Q^2} \frac{1}{1 - \Delta R}$$

where  $\Delta R$  accounts for radiative corrections)

$$v_u = 1/2 - 4/3\sin^2\theta_W$$
  $a_u = 1/2$   $v_d = -1/2 + 2/3\sin^2\theta_W$   $a_d = -1/2$ 

on-shell scheme used:  $\sin^2 \theta_W = 1 - M_W^2/M_Z^2 = 0.22333$  (PDG14)

# NC polarised DIS

NC: γZ interference and Z exchange affected by e-beam polarisation

$$P_e = \frac{N_R - N_L}{N_R + N_L}$$

$$\tilde{F_2}^{\pm} = F_2^{\gamma} - (\qquad \pm P_e a_e) \chi_Z F_2^{\gamma Z}$$
  $\chi z \gg \chi z^2$  and  $v_e \approx 0.04$ :  $v_q \text{ from polarised } F_2^{\gamma Z}$   $\chi \tilde{F_3}^{\pm} = -(a_e) \chi_Z x F_3^{\gamma Z}$  aq from unpolarised  $\chi F_3^{\gamma Z}$ 

**aq** from unpolarised xF<sub>3</sub>γZ

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# **CC** polarised DIS

CC:

$$P_e = \frac{N_R - N_L}{N_R + N_L}$$

$$\frac{d^2\sigma_{\rm CC}(e^+p)}{dx_{\rm Bi}dQ^2} = (1+P_e)\frac{G_F^2 M_W^4}{2\pi x_{\rm Bi}(Q^2 + M_W^2)^2} x \left[ (\bar{u} + \bar{c}) + (1-y)^2 (d+s+b) \right]$$

$$\frac{d^2\sigma_{\rm CC}(e^-p)}{dx_{\rm Bj}dQ^2} = (1 - P_e) \frac{G_F^2 M_W^4}{2\pi x_{\rm Bj}(Q^2 + M_W^2)^2} x \left[ (u+c) + (1-y)^2 (\bar{d} + \bar{s} + \bar{b}) \right]$$

$$G_F = \frac{\pi \alpha_0}{\sqrt{2} \sin^2 \theta_W M_W^2} \frac{1}{1 - \Delta R}$$

**CC** provides further sensitivity to PDFs (quark flavour separation)

and sensitivity to sin²θw, and Mw via GF and propagator

#### QCD and electroweak fit to HERA data

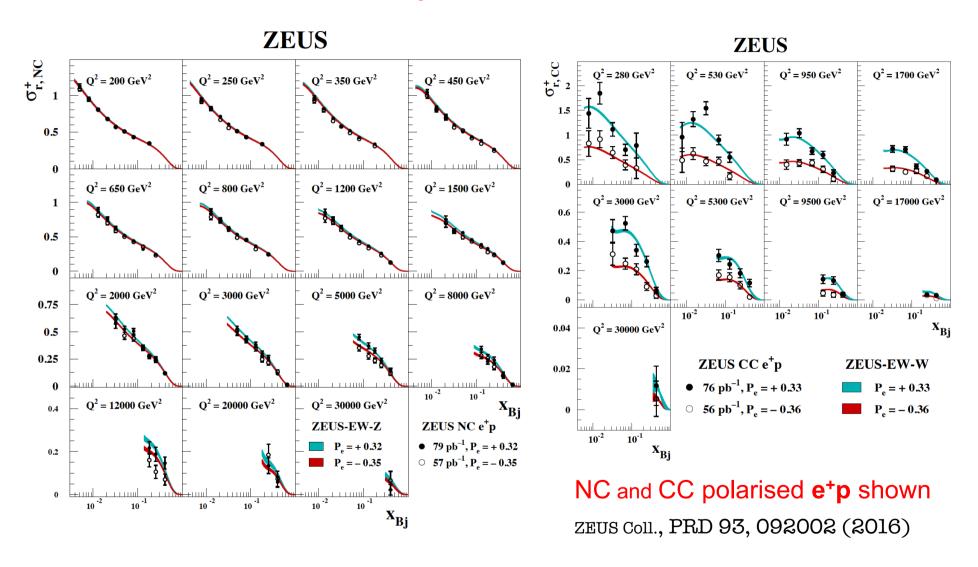
simultaneous NLO QCD and LO electroweak fit of PDF and EW parameters

- HERA NC and CC inclusive uncombined data sets as input:
- 1. datasets as used in HERA combination (EPJ C75 (2015) 580):
  HERA I H1 and ZEUS; H1 and ZEUS reduced Ep data; HERA II data from H1 (UNPOLARISED)
- 2. HERA II data from ZEUS (POLARISED)
- PDF fit, closely follows HERAPDF2.0 (EPJ C75 (2015) 580):

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A_g' x^{B_g'} (1-x)^{C_g'}, \qquad \text{start scale Q0}^2 = 1.9 \text{ GeV}^2$$
 
$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} \left(1+E_{u_v} x^2\right), \qquad \text{model and parameterisation}$$
 
$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}}, \qquad \text{uncertainties as in HERAPDF2.0}$$
 
$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}}, \qquad \text{the proof of the proof of$$

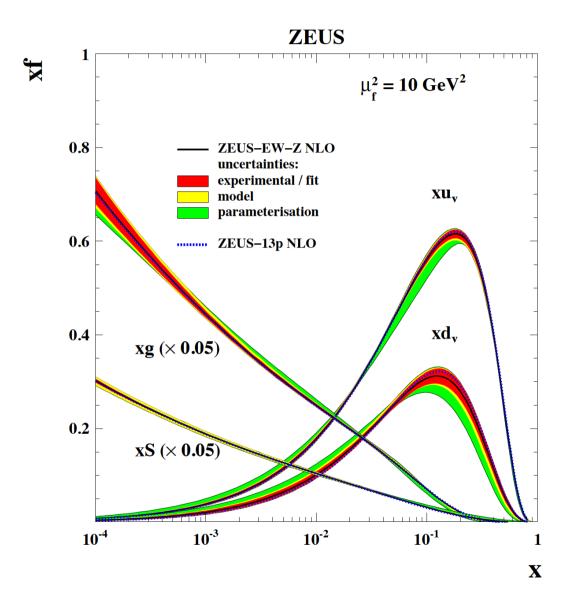
13 free PDF parameters, and 4 light quark NC EW couplings (or free sin<sup>2</sup> Ow / Mw)

# NC and CC polarised DIS data



 $Q^{2_{min}}$  = 3.5 GeV<sup>2</sup> – number of data points is 2942, of which 501 are polarised ZEUS cross section data (X<sup>2</sup>/NDF = 1.12 for fit with NC couplings free)

#### PDF results



ZEUS Coll., PRD 93, 092002 (2016)

agreement with equivalent (13p) fit with **EW couplings** set to SM values

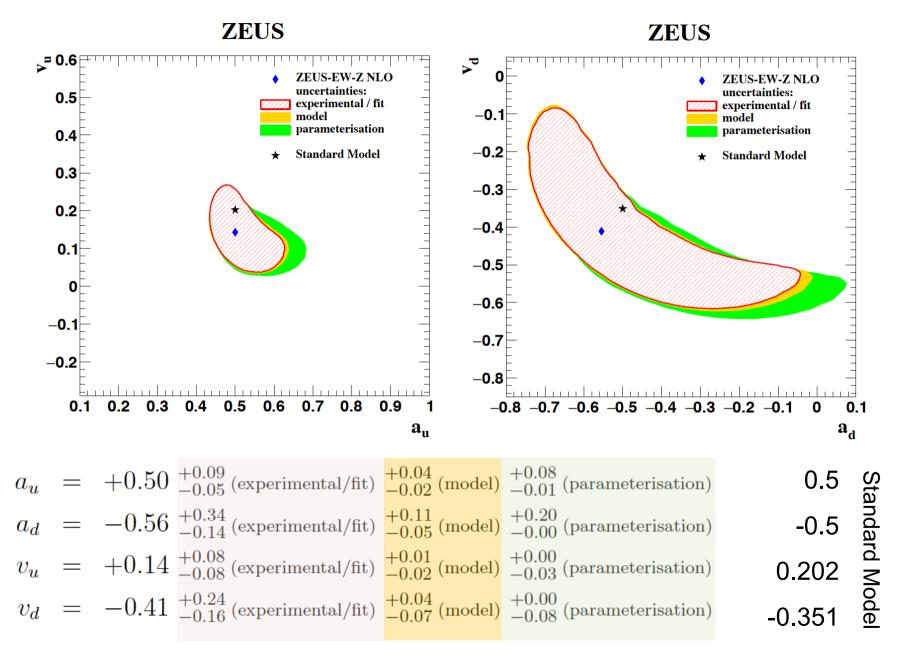
only weak correlation between

PDF and electroweak parameters

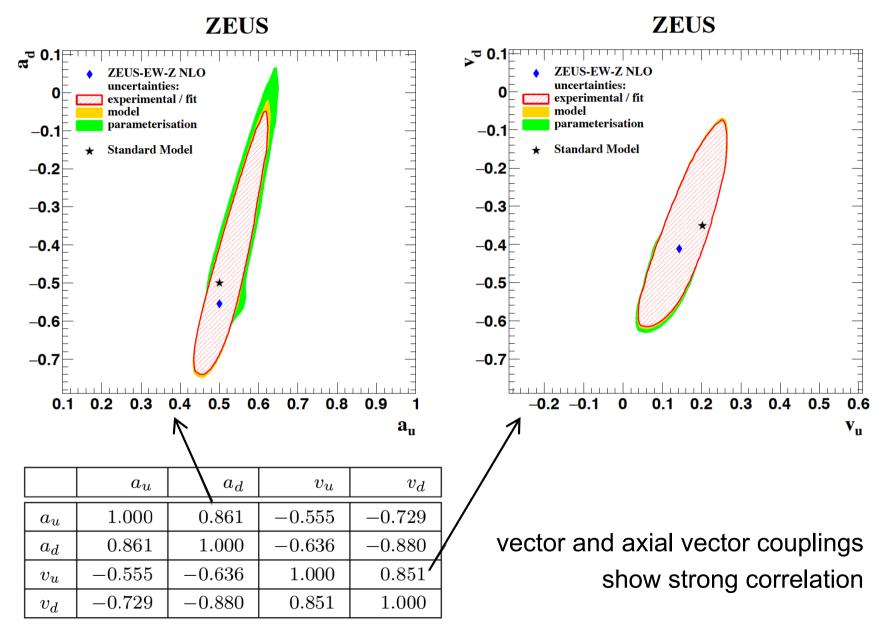
(QCD part of fit can be repeated at NNLO with little pull on EW parameters)

(also agrees well with **HERAPDF2.0** EPJ C75 (2015), 580)

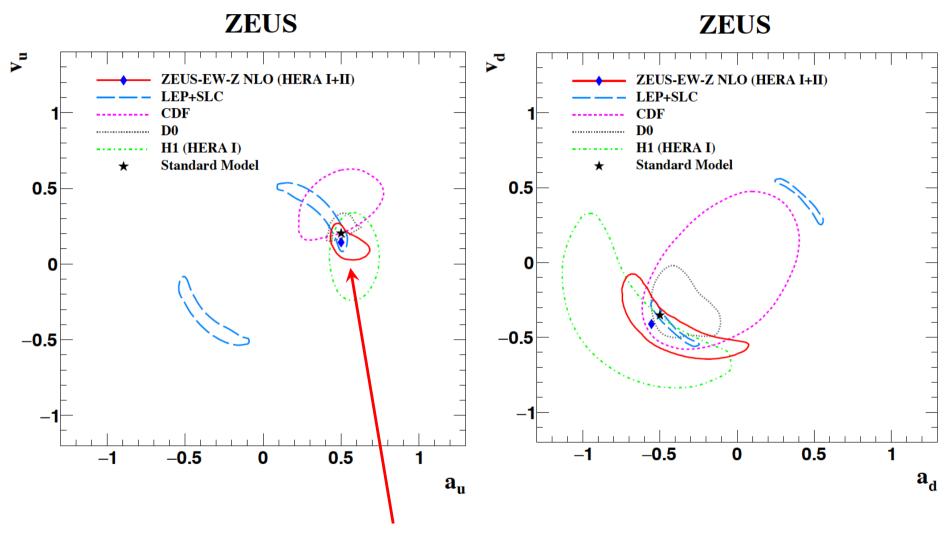
# NC electroweak couplings



# NC electroweak couplings – correlations



# comparison with other measurements

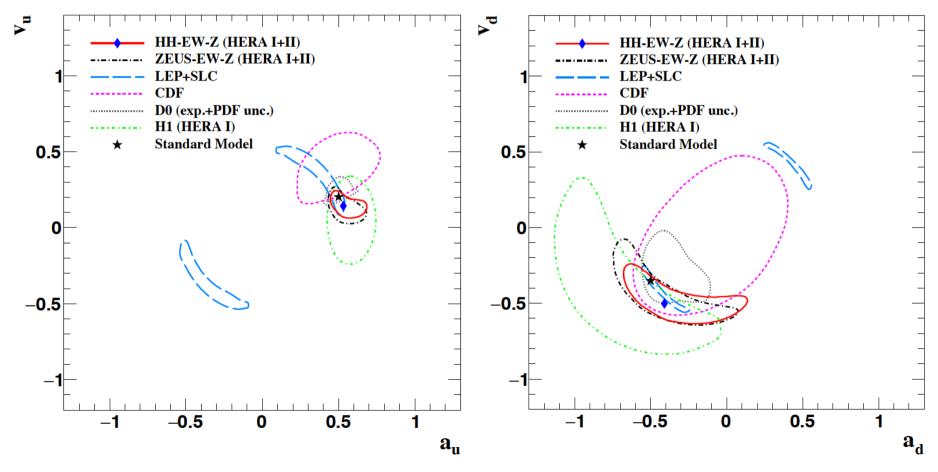


- excellent sensitivity to u-type quark couplings
- results compatible with SM expectation

# improvement from using all HERA polarised data

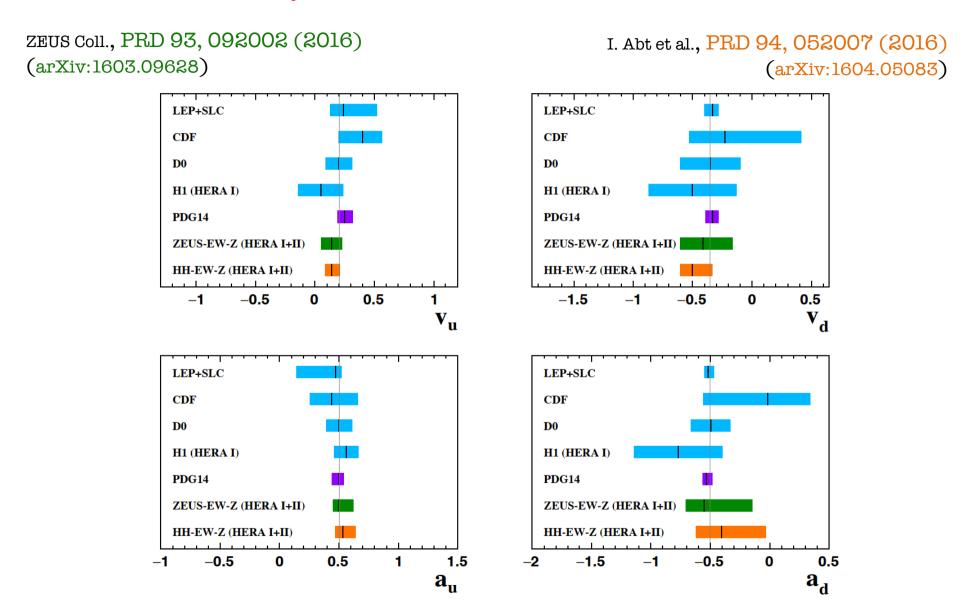
independent analysis (HH-EW-Z) performed, using also published H1 <u>polarised</u> data (H1 Coll., JHEP 1209 (2012) 061)

I. Abt et al., PRD 94, 052007 (2016) (arXiv:1604.05083)



**HERA II polarised data** especially important for **vector couplings** 

# comparison with other results



NC coupling determinations from I. Abt et al., included in PDG17 world average

#### sin<sup>2</sup> w and Mw

ZEUS Coll., PRD 93, 092002 (2016)

 sin²θw and Mw can also be extracted from the HERA inclusive DIS data

$$σNC$$
 (α,  $sin2θw$ , Mz)  
 $σCC$  (G<sub>F</sub>(α,  $sin2θw$ , Mw), Mw)

sin²θw fitted as parameter, along with PDFs:

$$\sin^2 \theta_W = 0.2252 \pm 0.0011$$
 (experimental/fit)  $^{+0.0003}_{-0.0001}$  (model)  $^{+0.0007}_{-0.0001}$  (parameterisation)

• Mw and PDF parameters fitted simultaneously (sin<sup>2</sup> 0w=0.22333 fixed):

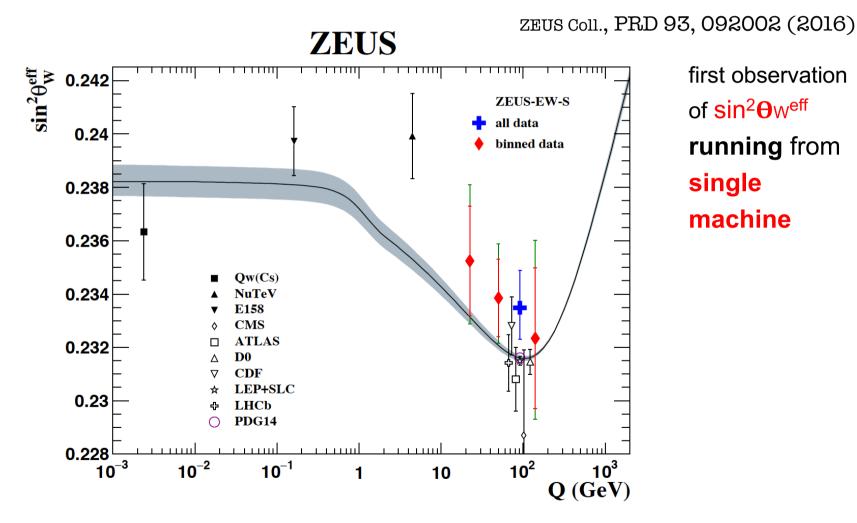
$$M_W=80.68~\pm0.28$$
 (experimental/fit)  $^{+0.12}_{-0.01}$  (model)  $^{+0.23}_{-0.01}$  (parameterisation) GeV

Mw determination from **space-like** process, <u>complementary</u> to other measurements

(simultaneous extraction of sin<sup>2</sup> \text{\text{0}} \text{V} and MW (and PDFs) also performed as cross check; results consistent with PDG world average – see backups)

#### effective sin<sup>2</sup> $\Theta$ w

measurements from full dataset, and in 3 bins of Q<sup>2</sup> (PDF parameters fixed)
 translated † to effective sin<sup>2</sup> \(\theta\)w



#### summary

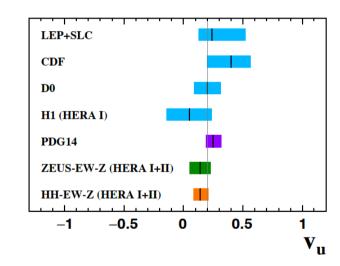
HERA polarised inclusive DIS data sensitive to electroweak parameters
 → simultaneous PDF and EW fits

NC vector and axial-vector couplings to quarks agree with world average

and SM expectation

 measurements of u-type quark couplings among most accurate from single collider

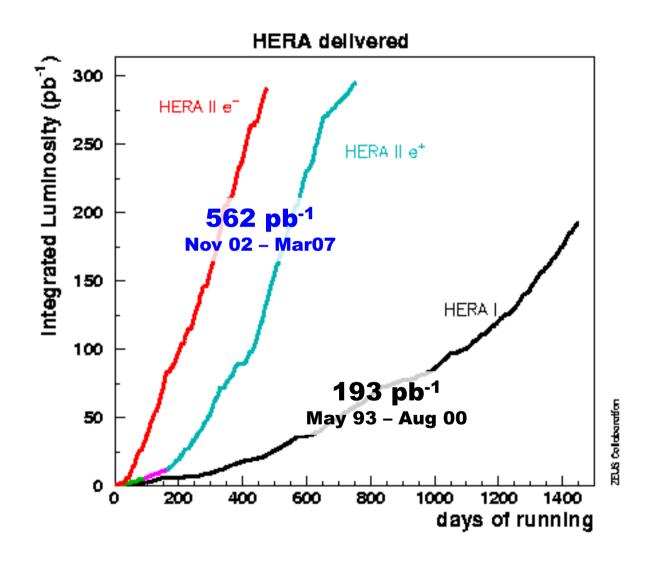
couplings from I. Abt et al. (HH-EW-Z) included in PDG17 world average



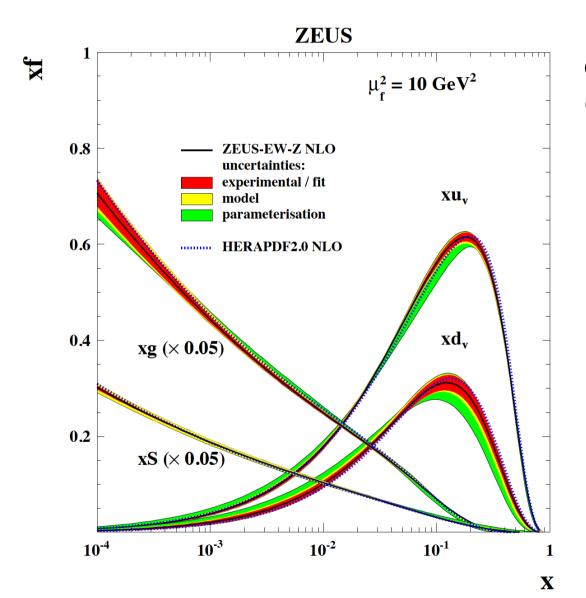
- sin²θw determined; first observation of sin²θweff running from single machine
- mass of W boson determined in space-like momentum transfer process

### extras

# HERA: world's only ep collider

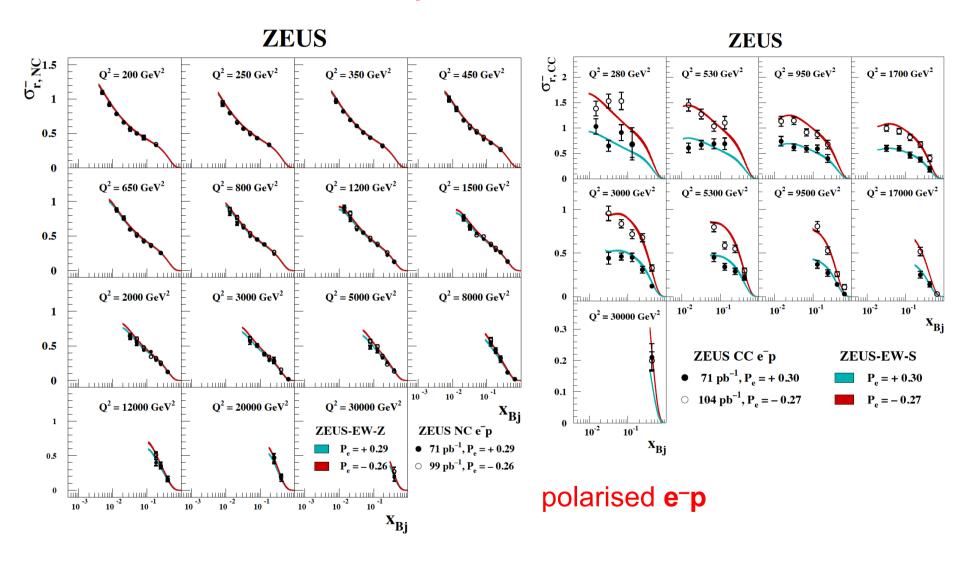


#### PDF fit results



comparison with HERAPDF2.0 (EPJ C75 (2015), 580)

# NC and CC polarised DIS data



 $Q^{2_{min}} = 3.5 \text{ GeV}^2 - \text{number of data points is 2942, of which 501 are polarised ZEUS cross section data (X<sup>2</sup>/NDF = 1.12 for fit with NC couplings free)$ 

#### correlation matrix

ZEUS Coll., PRD 93, 092002 (2016) (arXiv:1603.09628)

			,														
Parameters	xg: B	xg: C	xg: A'	xg: B'	$xu_v : B$	$xu_v$ : $C$	$xu_v$ : $E$	$xd_v \colon B$	$xd_v: C$	$x\bar{U}$ : $C$	$x\bar{D}$ : A	$x\bar{D}\colon B$	$x\bar{D}$ : $C$	$a_u$	$a_d$	$v_u$	$v_d$
xg: B	1.000	-0.014	-0.449	0.824	-0.216	0.172	0.250	-0.084	-0.085	-0.098	-0.107	-0.136	0.046	0.025	0.003	0.015	0.018
xg: C	-0.014	1.000	0.831	0.457	0.341	-0.373	-0.550	0.010	0.296	-0.018	-0.082	-0.103	-0.434	0.105	0.095	-0.098	-0.111
xg: A'	-0.449	0.831	1.000	0.120	0.548	-0.404	-0.629	0.233	0.274	0.159	0.081	0.072	-0.148	-0.052	0.000	-0.043	-0.054
xg: B'	0.824	0.457	0.120	1.000	0.106	-0.037	-0.082	0.075	0.047	0.043	0.011	-0.014	0.012	-0.029	-0.011	-0.001	-0.002
$xu_v \colon B$	-0.216	0.341	0.548	0.106	1.000	-0.409	-0.774	0.465	-0.086	0.690	0.476	0.395	0.439	-0.360	-0.178	0.079	0.070
$xu_v : C$	0.172	-0.373	-0.404	-0.037	-0.409	1.000	0.828	-0.297	-0.235	-0.188	-0.095	-0.069	-0.040	0.110	0.029	0.040	0.028
$xu_v \colon E$	0.250	-0.550	-0.629	-0.082	-0.774	0.828	1.000	-0.296	-0.066	-0.363	-0.170	-0.117	-0.092	0.192	0.087	-0.023	-0.017
$xd_v \colon B$	-0.084	0.010	0.233	0.075	0.465	-0.297	-0.296	1.000	0.518	0.405	0.350	0.291	0.673	-0.335	-0.134	0.038	0.021
$xd_v$ : C	-0.085	0.296	0.274	0.047	-0.086	-0.235	-0.066	0.518	1.000	-0.137	-0.186	-0.193	-0.139	0.110	0.128	-0.101	$\infty^{0.128}$
$x\bar{U}$ : $C$	-0.098	-0.018	0.159	0.043	0.690	-0.188	-0.363	0.405	-0.137	1.000	0.673	0.635	0.329	-0.320	-0.137	0.055	-0.052
$x\bar{D}$ : A	-0.107	-0.082	0.081	0.011	0.476	-0.095	-0.170	0.350	-0.186	0.673	1.000	0.959	0.477	-0.272	-0.137	0.056	0.059
$x\bar{D}$ : B	-0.136	-0.103	0.072	-0.014	0.395	-0.069	-0.117	0.291	-0.193	0.635	0.959	1.000	0.415	-0.239	-0.120	0.047	0.053
$x\bar{D}$ : $C$	0.046	-0.434	-0.148	0.012	0.439	-0.040	-0.092	0.673	-0.139	0.329	0.477	0.415	1.000	-0.449	-0.271	0.148	0.153
$a_u$	0.025	0.105	-0.052	-0.029	-0.360	0.110	0.192	-0.335	0.110	-0.320	-0.272	-0.239	-0.449	1.000	0.861	-0.555	-0.729
$a_d$	0.003	0.095	0.000	-0.011	-0.178	0.029	0.087	-0.134	0.128	-0.137	-0.137	-0.120	-0.271	0.861	1.000	-0.636	-0.880
$v_u$	0.015	-0.098	-0.043	-0.001	0.079	0.040	-0.023	0.038	-0.101	0.055	0.056	0.047	0.148	-0.555	-0.636	1.000	0.851
$v_d$	0.018	-0.111	-0.054	-0.002	0.070	0.028	-0.017	0.021	-0.128	0.052	0.059	0.053	0.153	-0.729	-0.880	0.851	1.000

Table 2: The correlation matrix of all parameters of the ZEUS-EW-Z fit.

# EW parameter cross checks

 studies performed to check stability of EW couplings with respect to various QCD parameters

	$a_u$	exp	tot	$a_d$	exp	tot	$v_{oldsymbol{u}}$	exp	tot	$v_d$	exp	tot
EW-Z	+0.50	$^{+0.09}_{-0.05}$	$^{+0.12}_{-0.05}$	-0.56	$^{+0.34}_{-0.14}$	$^{+0.41}_{-0.15}$	+0.14	$^{+0.08}_{-0.08}$	$^{+0.09}_{-0.09}$	-0.41	$^{+0.24}_{-0.16}$	$^{+0.25}_{-0.20}$
13p	+0.49	$^{+0.07}_{-0.04}$		-0.57	$^{+0.30}_{-0.13}$		+0.15	$^{+0.08}_{-0.08}$		-0.40	$^{+0.22}_{-0.17}$	
HPDF1	+0.47	$^{+0.06}_{-0.03}$		-0.62	$^{+0.23}_{-0.11}$		+0.16	$^{+0.08}_{-0.08}$		-0.35	$^{+0.22}_{-0.19}$	
HPDF2	+0.49	$^{+0.06}_{-0.03}$		-0.63	$^{+0.24}_{-0.11}$		+0.15	$^{+0.08}_{-0.08}$		-0.36	$^{+0.22}_{-0.19}$	
SM	+0.50			-0.50			+0.20			-0.35		

**Table 3:** The results on the axial-vector and vector couplings of the Z boson to u- and d-type quarks from ZEUS-EW-Z. Given are the experimental/fit (exp) and total (tot) uncertainties. Also listed are results of fits with the PDFs fixed to ZEUS-13p and HERAPDF2.0, HPDF1 and HPDF2, for which only the couplings of the Z were free parameters. The HPDF1 fit was performed with the on-shell value of  $\sin^2 \theta_W$  used in the fit while HPDF2 was performed with the  $\sin^2 \theta_W$  value used for the extraction of HERAPDF2.0. Also listed are the predictions of the SM for the a and v couplings in the on-shell scheme.

#### sin<sup>2</sup> w and Mw

DIS inclusive cross sections depend on sin<sup>2</sup> through:

#### **N**eutral **C**urrent:

• Xz term in NC cross section: 
$$\chi_Z = \frac{1}{\sin^2 2\theta_W} \frac{Q^2}{M_Z^2 + Q^2} \frac{1}{1 - \Delta R}$$

• NC vector couplings to quarks:  $v_u = 1/2 - 4/3 \sin^2 \theta_W$   $v_d = -1/2 + 2/3 \sin^2 \theta_W$ 

#### **Charged Current**

 $\begin{array}{ll} \bullet & \text{CC cross sections, via GF} & \frac{d^2\sigma_{\mathrm{CC}}(e^+p)}{dx_{\mathrm{Bj}}dQ^2} = (1+P_e)\frac{G_F^2M_W^4}{2\pi x_{\mathrm{Bj}}(Q^2+M_W^2)^2}\,x\,[(\bar{u}+\bar{c})+(1-y)^2(d+s+b)] \\ G_F = \frac{\pi\alpha_0}{\sqrt{2}\,\sin^2\theta_W\,M_W^2}\,\frac{1}{1-\Delta R} & \frac{d^2\sigma_{\mathrm{CC}}(e^-p)}{dx_{\mathrm{Bj}}dQ^2} = (1-P_e)\frac{G_F^2M_W^4}{2\pi x_{\mathrm{Bj}}(Q^2+M_W^2)^2}\,x\,[(u+c)+(1-y)^2(\bar{d}+\bar{s}+\bar{b})] \end{array}$ 

GF re-expressed through sin<sup>2</sup> w and Mw meaning both NC and CC used to extract sin<sup>2</sup> w

X<sub>F</sub> and G<sub>F</sub> are most important for sin<sup>2</sup> ⊕w determination

Mw sensitivity comes from GF and W propagator in CC events

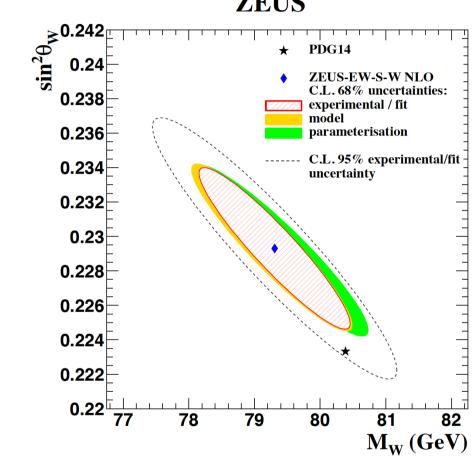
#### sin<sup>2</sup>⊕w

bin	$Q_{\min}^2$	$Q_{\rm max}^2$	scale	$\sin^2 \theta_W$	exp	$\sin^2  heta_W^{ ext{eff}}$	exp	PDF
	$(\mathrm{GeV}^2)$	$(\mathrm{GeV}^2)$	(GeV)	on-shell	unc.	effective	unc.	unc.
1	200	1000	22.3	0.2254	±0.0020	0.2352	$\pm 0.0020$	$^{+0.0020}_{-0.0012}$
2	1000	5000	49.9	0.2251	$\pm 0.0014$	0.2339	$\pm 0.0015$	$^{+0.0014}_{-0.0008}$
3	5000	50000	139.8	0.2240	$\pm 0.0026$	0.2323	$\pm 0.0026$	$^{+0.0025}_{-0.0015}$
All I	Data		$M_Z$	0.2252	±0.0011	0.2335	±0.0011	$+0.0008 \\ -0.0004$

Table 4: The on-shell and effective values of  $\sin^2 \theta_W$  as determined for three bins in  $Q^2$  and for all data. Experimental/fit (exp) uncertainties are given as determined by the one-parameter fits for each bin or ZEUS-EW-S, respectively; model and parameterisation uncertainties as determined by ZEUS-EW-S were added in quadrature and are denoted as PDF uncertainties. They are identical for on-shell and effective values at the accuracy given.

#### sin<sup>2</sup> w and Mw





simultaneous extraction of sin<sup>2</sup>  $\Theta$  w and Mw (together with PDFs) also performed as cross-check

#### **PDG14**:

 $\sin^2\Theta w = 0.22333 \pm 0.00011$  (on-shell)

 $Mw = 80.385 \pm 0.015$ 

$$\sin^2 \theta_W = 0.2293 \pm 0.0031 \text{ (experimental/fit) } ^{+0.0005}_{-0.0001} \text{ (model) } ^{+0.0003}_{-0.0001} \text{ (parameterisation)}$$

$$M_W=79.30~\pm 0.76~(\text{experimental/fit})~^{+0.38}_{-0.08}~(\text{model})~^{+0.48}_{-0.10}~(\text{parameterisation})~\text{GeV}$$
 .

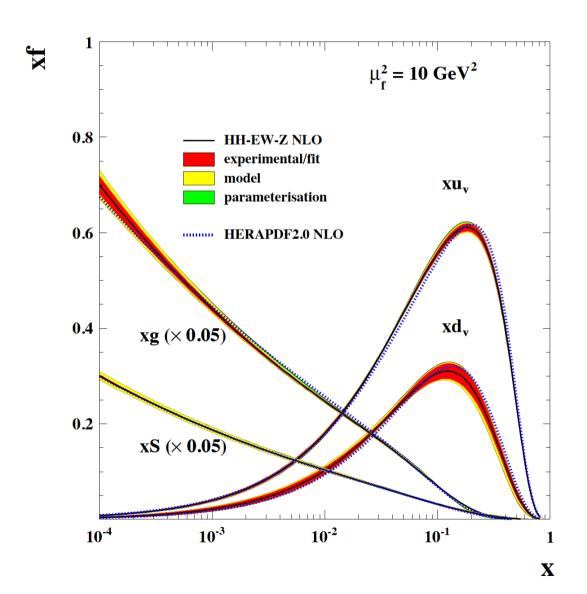
# comparison of NC light quark couplings

ZEUS Coll., PRD 93, 092002 (2016) (arXiv:1603.09628)

I. Abt et al., PRD 94, 052007 (2016) (arXiv:1604.05083)

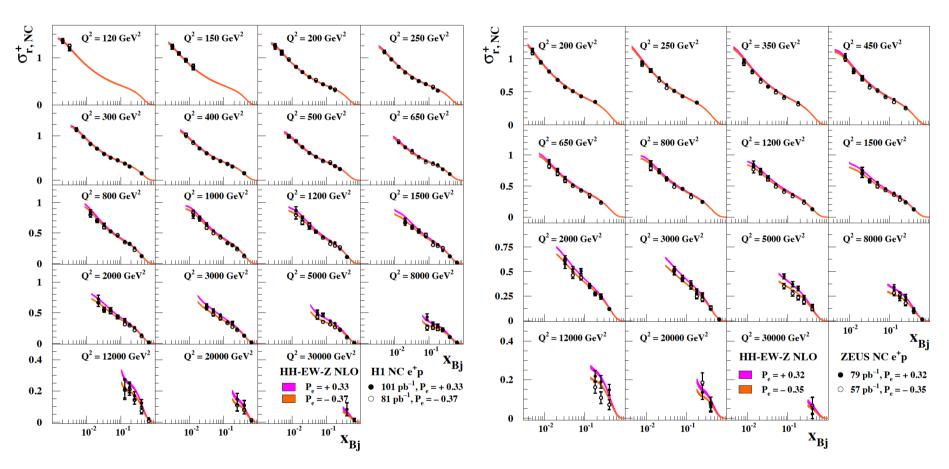
$$a_u = +0.532^{+0.081}_{-0.058}$$
 (experimental/fit)  $a_d = -0.409^{+0.327}_{-0.199}$  (experimental/fit)  $a_d = +0.144^{+0.065}_{-0.050}$  (experimental/fit)  $a_d = -0.503^{+0.168}_{-0.093}$  (experimental/fit)  $a_d = -0.503^{+0.168}_{-0.093}$  (experimental/fit)  $a_d = -0.503^{+0.168}_{-0.093}$  (experimental/fit)  $a_d = -0.503^{+0.168}_{-0.093}$  (experimental/fit)  $a_d = -0.028^{+0.060}_{-0.028}$  (model)  $a_d = -0.008^{+0.060}_{-0.025}$  (parameterisation)

#### PDF fit results – HH-EW-Z



comparison with HERAPDF2.0 (EPJ C75 (2015), 580)

# NC polarised DIS data from H1 and ZEUS



polarised e-p

 $Q^{2}_{min} = 3.5 \text{ GeV}^{2} - X^{2}/NDF = 3556/3231=1.10 \text{ for fit with NC couplings free}$ 

#### correlation matrix

I. Abt et al., PRD 94, 052007 (2016) (arXiv:1604.05083)

Parameters	xg: B	xg: C	xg: A'	xg: B'	$xu_v \colon B$	xu <sub>v</sub> : C	$xu_v \colon E$	$xd_v \colon B$	$xd_v$ : $C$	xŪ: C	хD: А	хÐ: В	х <u></u> D: С	$a_u$	$a_d$	$v_u$	$v_d$
xg: B	1.000	0.491	-0.224	0.935	0.012	0.106	0.044	-0.049	-0.078	-0.049	-0.098	-0.140	0.018	0.057	0.061	-0.039	-0.051
xg: C	0.491	1.000	0.660	0.707	0.287	-0.267	-0.464	-0.054	0.196	-0.047	-0.140	-0.175	-0.369	0.106	0.093	-0.124	-0.114
xg: A'	-0.224	0.660	1.000	0.125	0.513	-0.361	-0.593	0.226	0.254	0.162	0.084	0.072	-0.100	-0.038	0.003	-0.065	-0.070
xg: B'	0.935	0.707	0.125	1.000	0.200	-0.002	-0.144	0.048	-0.008	0.042	-0.017	-0.056	0.018	0.033	0.057	-0.058	-0.074
$xu_v \colon B$	0.012	0.287	0.513	0.200	1.000	-0.337	-0.760	0.510	-0.084	0.698	0.498	0.409	0.507	-0.256	-0.095	0.019	-0.032
$xu_v: C$	0.106	-0.267	-0.361	-0.002	-0.337	1.000	0.796	-0.249	-0.247	-0.140	-0.055	-0.032	-0.013	0.092	0.044	0.026	0.013
$xu_v \colon E$	0.044	-0.464	-0.593	-0.144	-0.760	0.796	1.000	-0.298	-0.057	-0.363	-0.165	-0.105	-0.127	0.133	0.045	0.024	0.043
$xd_v \colon B$	-0.049	-0.054	0.226	0.048	0.510	-0.249	-0.298	1.000	0.502	0.437	0.406	0.344	0.727	-0.221	-0.056	0.014	-0.056
$xd_v : C$	-0.078	0.196	0.254	-0.008	-0.084	-0.247	-0.057	0.502	1.000	-0.116	-0.168	-0.175	-0.097	0.107	0.115	-0.092	-0.109
$x\bar{U}:C$	-0.049	-0.047	0.162	0.042	0.698	-0.140	-0.363	0.437	-0.116	1.000	0.685	0.647	0.366	-0.234	-0.082	-0.006	-0.028
$x\bar{D}$ : $A$	-0.098	-0.140	0.084	-0.017	0.498	-0.055	-0.165	0.406	-0.168	0.685	1.000	0.961	0.525	-0.231	-0.114	0.049	0.021
x <b>D</b> : B	-0.140	-0.175	0.072	-0.056	0.409	-0.032	-0.105	0.344	-0.175	0.647	0.961	1.000	0.460	-0.210	-0.106	0.046	0.026
<i>x</i> <b>D</b> : <i>C</i>	0.018	-0.369	-0.100	0.018	0.507	-0.013	-0.127	0.727	-0.097	0.366	0.525	0.460	1.000	-0.327	-0.168	0.133	0.056
$a_u$	0.057	0.106	-0.038	0.033	-0.256	0.092	0.133	-0.221	0.107	-0.234	-0.231	-0.210	-0.327	1.000	0.928	-0.665	-0.779
$a_d$	0.061	0.093	0.003	0.057	-0.095	0.044	0.045	-0.056	0.115	-0.082	-0.114	-0.106	-0.168	0.928	1.000	-0.714	-0.876
$v_u$	-0.039	-0.124	-0.065	-0.058	0.019	0.026	0.024	0.014	-0.092	-0.006	0.049	0.046	0.133	-0.665	-0.714	1.000	0.880
$v_d$	-0.051	-0.114	-0.070	-0.074	-0.032	0.013	0.043	-0.056	-0.109	-0.028	0.021	0.026	0.056	-0.779	-0.876	0.880	1.000

Table 1: The correlation matrix of all parameters of the HH-EW-Z fit.