

Fit of EW Parameters using Polarised DIS H1 Data



Zhiqing ZHANG
on behalf of the H1 Collaboration



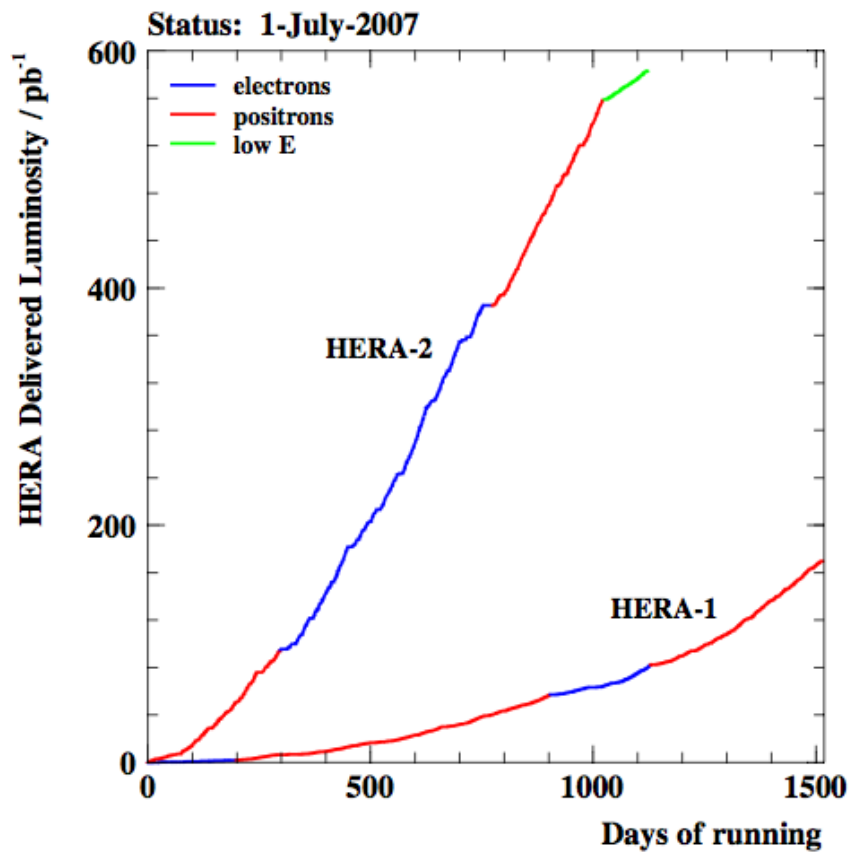
Outline

- Introduction
- New constraints from HERA-2 Data with P_e
- Results
- Summary

Introduction

ep collider, HERA, used to be the largest electron microscope

Both NC and CC inclusive cross sections were precisely measured



HERA-1 (1992-2000):

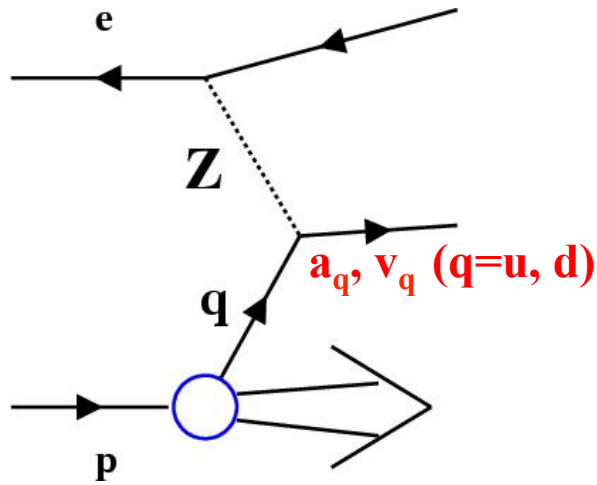
Combined HERA-1 data primary input for all modern PDF sets:

- CTEQ
- MRST
- NNPDFs
- HERAPDF1.0
-

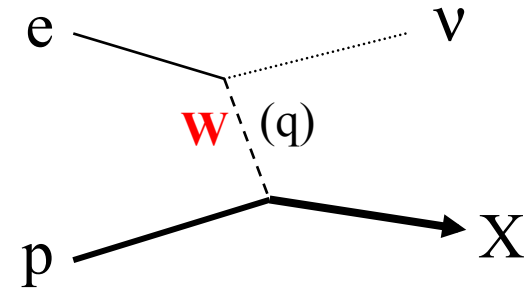
HERA-2 (2003-2007):

- Increased lumi ($\times 10$ e^- , $\times 2$ e^+)
- Long. polarized e beam
- Full combination HERA-1 & -2

Neutral and Charged Current DIS Interactions



NC interactions sensitive to light quark couplings to Z



Event kinematics:

$Q^2 = -q^2$: Boson virtuality

x : momentum fraction of struck parton

$y = Q^2/sx$: inelasticity

Coupling Sensitivity with Unpolarised HERA-I Data

$$\frac{d^2\sigma_{\text{NC}}^{\pm}}{dx dQ^2} \sim Y_+ \tilde{F}_2 \mp Y_- x \tilde{F}_3 \quad \text{with} \quad Y_{\pm} = 1 \pm (1-y)^2$$

$v_e \sim 0$, \rightarrow some of the terms are negligible

$$\tilde{F}_2 = F_2 - \cancel{v_e \kappa_Z} F_2^{\gamma Z} + (\cancel{v_e^2} + a_e^2) \kappa_Z^2 F_2^Z$$

$$x \tilde{F}_3 = -a_e \kappa_Z x F_3^{\gamma Z} + \cancel{2v_e a_e \kappa_Z^2} x F_3^Z$$

$$F_2^Z = x \sum_q (v_q^2 + a_q^2) \{q + \bar{q}\}$$

$$x F_3^{\gamma Z} = 2x \sum_q e_q a_q \{q - \bar{q}\}$$

$\rightarrow a_q$ mainly constrained by $x F_3^{\gamma Z}$

$\rightarrow v_q$ constrained by F_2^Z

$$\kappa_Z^{-1} = \frac{2\sqrt{2}\pi\alpha}{G_F M_Z^2} \frac{Q^2 + M_Z^2}{Q^2}$$

In on-mass-shell scheme:

$$G_F = \frac{\pi\alpha}{\sqrt{2}M_W^2} \left(1 - \frac{M_W^2}{M_Z^2}\right)^{-1} (1 + \Delta r)$$

$$\Delta r = \Delta r(\alpha, M_W, M_Z, m_t, m_h, \dots)$$

First determination performed by H1 [PLB 632 \(2006\) 35](#)

Additional Sensitivity with Polarised HERA-II Data

Polarized e beam (P_e) \rightarrow Additional terms

Structure function formulae
given for e^-p scattering,
for e^+p , $P_e \rightarrow -P_e$

$$\tilde{F}_2 = F_2 - (\cancel{v_e} - P_e a_e) \kappa_Z F_2^{\gamma Z} + (\cancel{v_e}^2 + a_e^2 - \cancel{2P_e v_e a_e}) \kappa_Z^2 F_2^Z$$

$$x\tilde{F}_3 = -(a_e - \cancel{P_e v_e}) \kappa_Z x F_3^{\gamma Z} + [\cancel{2v_e a_e} - P_e (\cancel{v_e}^2 + a_e^2)] \kappa_Z^2 x F_3^Z$$

$$\left[F_2^{\gamma Z}, F_2^Z \right] = x \sum_q [2e_q v_q, v_q^2 + a_q^2] \{q + \bar{q}\}$$

$$\left[xF_3^{\gamma Z}, xF_3^Z \right] = 2x \sum_q [e_q a_q, v_q a_q] \{q - \bar{q}\}$$

\rightarrow additional constraint on v_q by $F_2^{\gamma Z}$

Used Data Sets

Data set	Q^2 -range [GeV ²]	\sqrt{s} [GeV]	No. of data points	Polarization [%]	
HERA-I	e^+ Combined low- Q^2	(0.5) 12 – 150	319	81 (262)	–
	e^+ Combined low- E_p	(1.5) 12 – 90	301	118 (136)	–
	e^+ NC 94–97	150 – 30 000	301	130	–
	e^+ CC 94–97	300 – 15 000	301	25	–
	e^- NC 98–99	150 – 30 000	319	126	–
	e^- CC 98–99	300 – 15 000	319	28	–
	e^- NC 98–99 high- y	100 – 800	319	13	–
	e^+ NC 99–00	150 – 30 000	319	147	–
e^+ CC 99–00	300 – 15 000	319	28	–	
HERA-II	e^+ NC L HERA-II	120 – 30 000	319	137	-37.0 ± 1.0
	e^+ CC L HERA-II	300 – 15 000	319	28	-37.0 ± 1.0
	e^+ NC R HERA-II	120 – 30 000	319	137	$+32.5 \pm 0.7$
	e^+ CC R HERA-II	300 – 15 000	319	28	$+32.5 \pm 0.7$
	e^- NC L HERA-II	120 – 50 000	319	138	-25.8 ± 0.7
	e^- CC L HERA-II	300 – 30 000	319	29	-25.8 ± 0.7
	e^- NC R HERA-II	120 – 30 000	319	139	$+36.0 \pm 0.7$
	e^- CC R HERA-II	300 – 15 000	319	28	$+36.0 \pm 0.7$

For the first 2 data sets, only data above 12GeV^2 are included

Fit Strategy

- 5 sets of PDFs parameterised at starting scale $Q_0^2=1.9 \text{ GeV}^2$

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g},$$

$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2),$$

$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}},$$

$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}$$

Momentum sum rule and quark counting rules applied to constrain

A_g, A_{u_v}, A_{d_v} (C'_g fixed to 25)

Other constraints applied: $A_{\bar{U}} = A_{\bar{D}}, B_{\bar{U}} = B_{\bar{D}}$

- DGLAP evolution & cross section calculations in NNLO QCD

Fit Strategy

- Fits performed with log-normal based likelihood function

$$\chi^2 = \sum_{ij} \log \frac{d_i}{\tilde{\sigma}_i} V_{ij}^{-1} \log \frac{d_j}{\tilde{\sigma}_j}$$

Correlation in data (d) taken into account in covariance matrix (V)

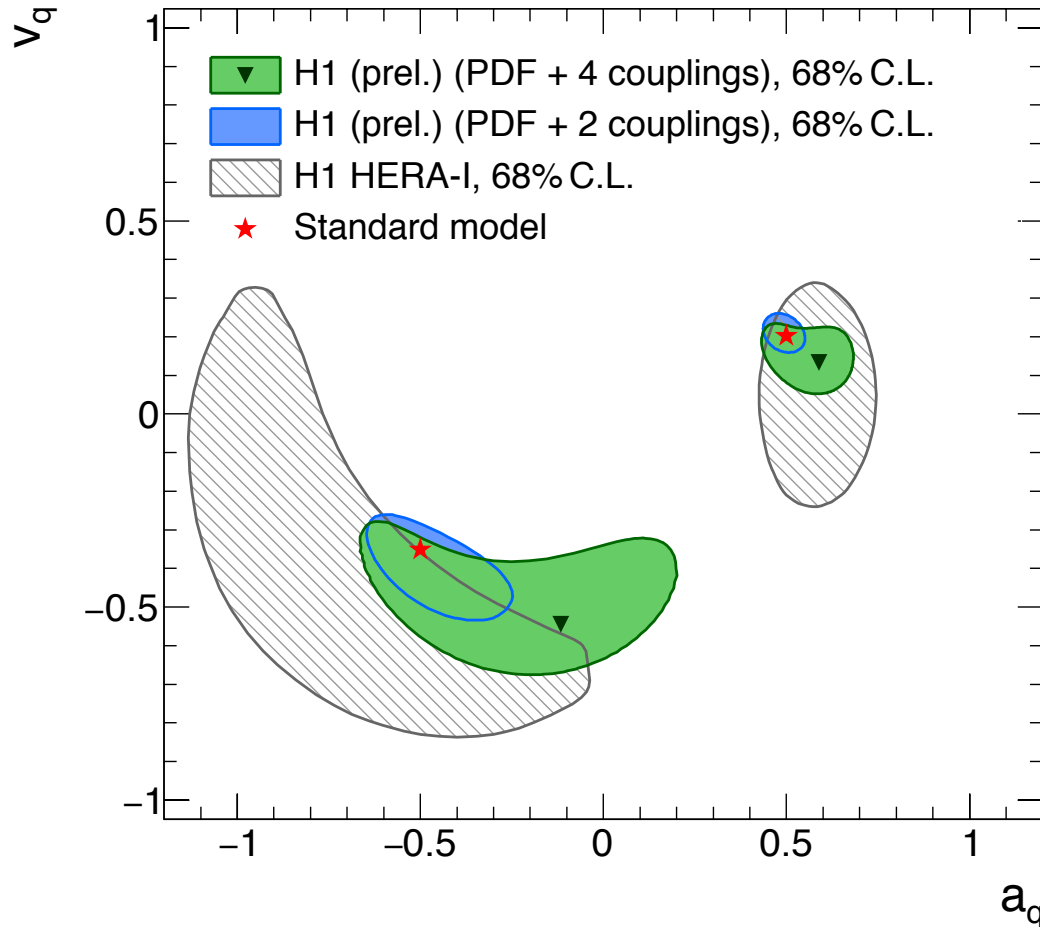
- Fit-1: Quark couplings + PDFs

- 4 or 2 couplings + 13 PDF parameters
- chi2 value: $1370.5/(1388-21)=1.0$

- Fit-2: M_W + PDFs (chi2 value: $1372.3/(1388-18)=1.0$)

- Translate to $\sin^2\theta_W$ in on-mass-shell scheme by using known M_Z
- Divide data sets in several Q^2 ranges
- $\sin^2\theta_W$ extracted at different scale $\mu = \sqrt{Q^2}$
- chi2 value: $1365.3/(1388-24)=1.0$

Fit-1 Results



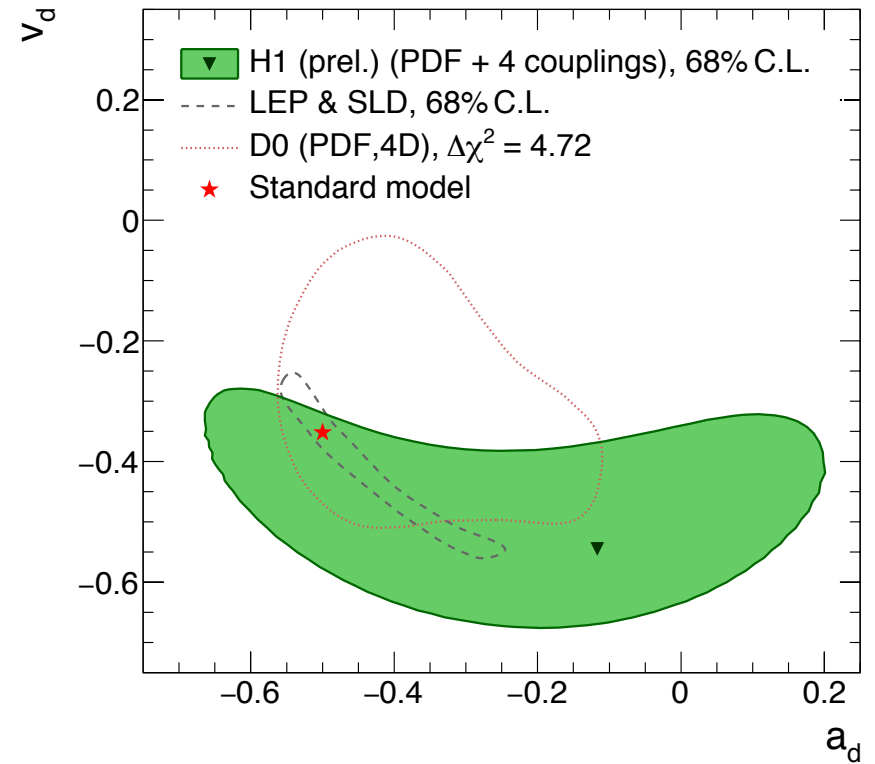
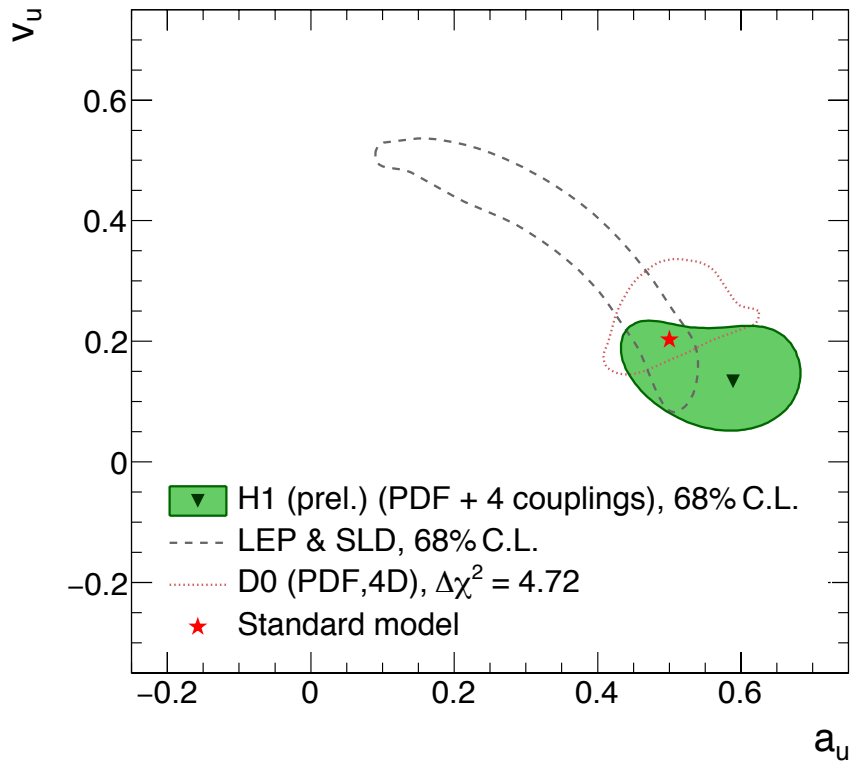
Fixing

α , M_Z , M_W in NC

G_F , M_W in CC

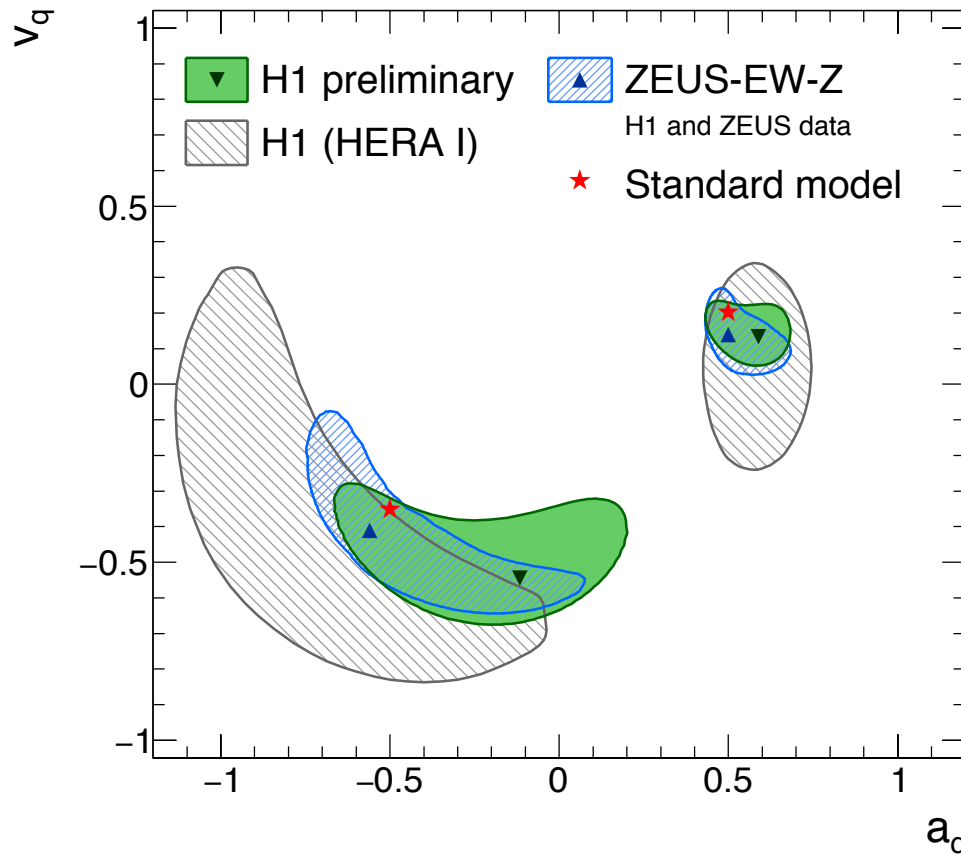
- Significant improvement over HERA-I determination
- 2 coupling fit is more precise due to the reduced correlation

Comparison with LEP and Tevatron Results



- Precision (in particular for a_u , v_u) competitive with LEP & D0
- LEP determinations have ambiguity in sign

Comparison with ZEUS Results



- This result comparable with a similar one from ZEUS (previous talk)
- ZEUS fit included HERA-I and -II data sets from H1 with $P_e=0$

ZEUS: [PRD 93 \(2016\) 092002](#)

Fit-2: M_W + PDFs

SM overconstrained

- at HERA, W boson appears as a virtual boson exchange
- Probing space-like momentum transfers
- M_W determined in on-mass-shell scheme by fixing α , M_Z , m_t , m_h
- Correlation with PDFs properly taken into account

$$M_W = 80.407 \pm 0.118(\text{exp, PDF-fit}) \pm 0.005(M_Z, m_t, m_h) \text{ GeV}$$

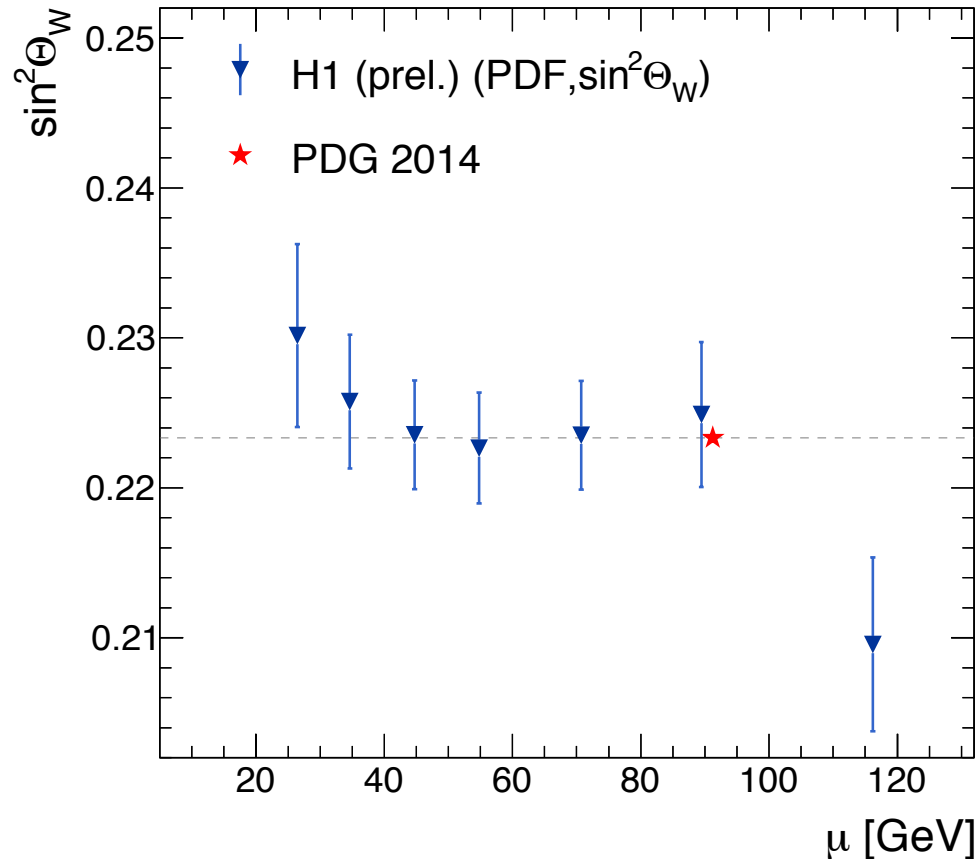
to be compared with HERA-I result:

$$M_W = 80.786 \pm 0.205(\text{exp})_{-0.098}^{+0.063}(\text{th}) \text{ GeV}$$

⇒ A factor ~ 2 improvement!

⇒ Extract $\sin^2 \theta_W(\text{on-mass-shell}) = 1 - \frac{M_W^2(\text{fit})}{M_Z^2(\text{input})}$

Fit-2: Weak Mixing Angle versus Q^2



- ▶ $\sin^2\theta_W$ showing no strong scale dependence as expected
- ▶ Results consistent with precise Z-pole measurements

Summary

- (Light) quark couplings determined with much improved precision, thanks to
 - the new sensitivity with polarised e^+/e^- beams at HERA-II
 - more HERA-II high Q^2 cross section measurement
- A M_W (and $\sin^2\theta_W$) determination
 - A factor of 2 improvement in precision over HERA-I
- The final results (including 1-loop EW corrections) will be published soon