



**Combination and QCD analysis of beauty and charm
production cross section measurements in deep
inelastic ep scattering at HERA**

Oleksandr Zenaiev (DESY)
on behalf of H1 and ZEUS collaborations
[Eur.Phys.J. C78 (2018) 473]

ICHEP
Seoul, 4-11 July 2018

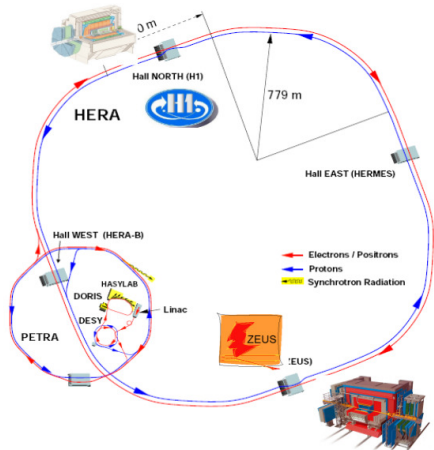
Experimental set-up

HERA Collider

- ep collisions
- $\sqrt{s} = 300 \dots 318 \text{ GeV}$
and lower energy runs

H1 and ZEUS:

- 4π multipurpose detectors
- $\mathcal{L} \sim 500 \text{ pb}^{-1}$
per each experiment



$$E_p = 920 \text{ GeV} \quad E_e = 27.5 \text{ GeV}$$
$$\sqrt{s} = 318 \text{ GeV}$$

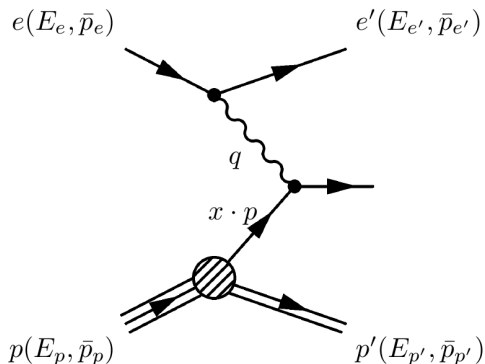
$$Q^2 = -q^2 = -(\mathbf{e} - \mathbf{e}')^2$$

$$x_{Bj} = \frac{Q^2}{2q \cdot p} \quad (= x \text{ in QPM})$$

$$y = \frac{q \cdot p}{q \cdot e}$$

$$s = (\mathbf{e} + \mathbf{p})^2$$

$$Q^2 = sx_{Bj}y$$



- Any two of the variables (Q^2 , x_{Bj} , y) define kinematics
- $Q^2 > 1 \text{ GeV}^2$ — deep inelastic scattering (DIS)
- $Q^2 < 1 \text{ GeV}^2$ — photoproduction processes (PHP)

Heavy flavour (HF) production in DIS

Test of pQCD (multiple hard scales: $Q^2, p_T(Q), m_Q$)

Charm and beauty in DIS are predominantly produced via Boson-Gluon Fusion (BGF)

$$\sigma = \text{PDF} \otimes \text{ME} \otimes \text{FF}$$

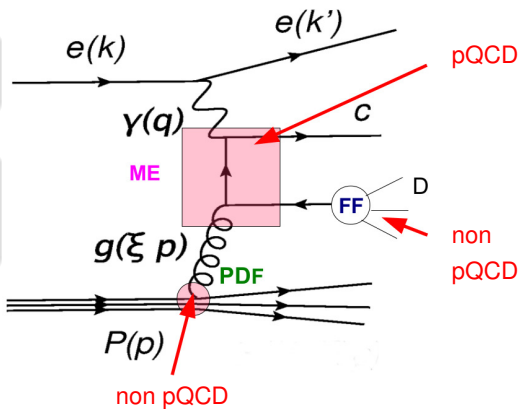


Production is directly sensitive to g PDF in the proton and HQ masses

PDF: parton distribution functions

ME: (hard) matrix element

FF: fragmentation function & fraction



Fixed Flavour Number Scheme (FFNS)

- c,b-quarks are massive \Rightarrow not a part of the proton, produced perturbatively in hard scattering
- valid for $Q^2 \sim m_{c,b}^2$

Zero Mass Variable Flavour Number Scheme (ZMVFNS)

- c,b-quarks are massless \Rightarrow a part of the proton
- valid for $Q^2 \gg m_{c,b}^2$

General Mass Variable Flavour Number Scheme (GMVFNS)

- equivalent to FFNS at low Q^2
- equivalent to ZMVFNS at high Q^2
- not unique (RT, ACOT, FONLL, ...)

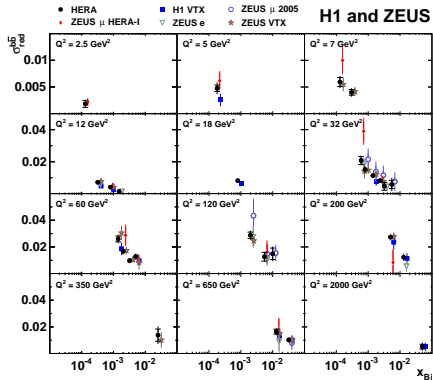
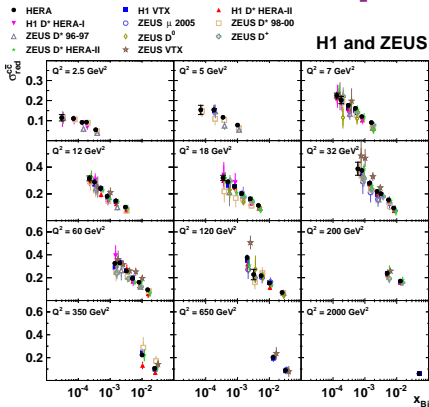
detailed discussion in [EPJ C73 (2013) 2311]

Input data

Data set	Tagging	Q^2 range [GeV ²]	N_c	\mathcal{L} [pb ⁻¹]	\sqrt{s} [GeV]	N_b
1 H1 VTX [8]	VTX	5 – 2000	29	245	318	12
2 H1 D^{*+} HERA-I [9]	D^{*+}	2 – 100	17	47	318	
3 H1 D^{*+} HERA-II (medium Q^2) [10]	D^{*+}	5 – 100	25	348	318	
4 H1 D^{*+} HERA-II (high Q^2) [11]	D^{*+}	100 – 1000	6	351	318	
5 ZEUS D^{*+} 96-97 [12]	D^{*+}	1 – 200	21	37	300	
6 ZEUS D^{*+} 98-00 [13]	D^{*+}	1.5 – 1000	31	82	318	
7 ZEUS D^0 2005 [14]	D^0	5 – 1000	9	134	318	
8 ZEUS μ 2005 [7]	μ	20 – 10000	8	126	318	8
9 ZEUS D^+ HERA-II [2]	D^+	5 – 1000	14	354	318	
10 ZEUS D^{*+} HERA-II [3]	D^{*+}	5 – 1000	31	363	318	
11 ZEUS VTX HERA-II [4]	VTX	5 – 1000	18	354	318	17
12 ZEUS e HERA-II [5]	e	10 – 1000		363	318	9
13 ZEUS μ + jet HERA-I [6]	μ	2 – 3000		114	318	11

(corresponding references can be found in backup)

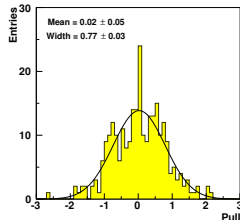
- Combined reduced cross sections: $\sigma_{\text{red}}^{Q\bar{Q}} = \frac{d^2\sigma^{Q\bar{Q}}}{dx_{\text{Bj}}dQ^2} \cdot \frac{x_{\text{Bj}}Q^4}{2\pi\alpha^2(1+(1-y)^2)}$
- $2.5 \leq Q^2 \leq 2000 \text{ GeV}^2$, $3 \times 10^{-5} \leq x_{\text{Bj}} \leq 5 \times 10^{-2}$
- Input **209 c**, **52 b** data points \Rightarrow combined **52 c**, **27 b** points
- **Extends previous HERA charm combination with 3 new c data sets and 5 new b: first combination of HERA b data**



$$\chi^2/\text{dof} = 149/187$$

→ input data are consistent

→ significantly reduced uncertainties as compared to the individual measurements



Theoretical predictions (FFNS) compared to combined data

Predictions obtained with OPENQCDRAD interfaced in xFitter

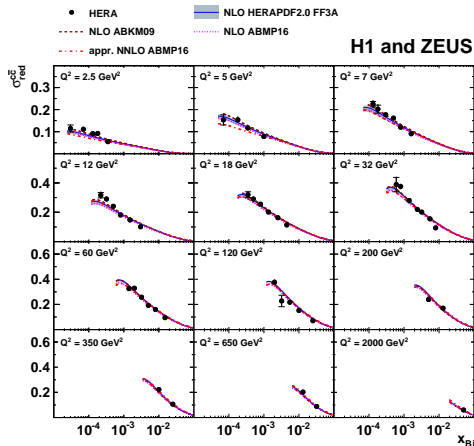
www-zeuthen.desy.de/~alekhin/OPENQCDRAD

www.xfitter.org

- input PDFs: HERAPDF2.0FF3A, ABM11, ABKM09, ABMP16
- $\mu_f = \mu_r = \sqrt{Q^2 + 4m_Q^2}$, varied by factor 2 (dominant unc.)
- $m_c(m_c) = 1.27 \pm 0.03$ GeV, $m_b(m_b) = 4.18 \pm 0.03$ GeV [PDG2016]

FFNS, $n_f = 3$: reliable in this kinematic range

FFNS, CHARM (beauty in BACKUP)



FFNS predictions compared to data: ratio to HERAPDF2.0FF3A

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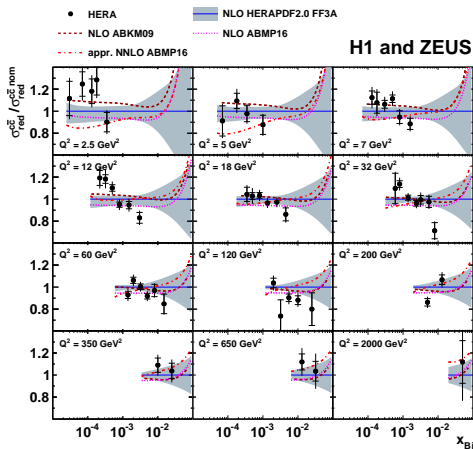
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FFNS, $n_f = 3$: reliable in this kinematic range

- overall fair description, somewhat different x slope
- description not improved at approx. NNLO or VFNS (*backup*)

FFNS, CHARM (beauty in BACKUP)



Similar to HERAPDF2.0 FF:

- performed using xFitter [www.xfitter.org]
- inclusive HERA data + **new combined c&b data**
- NLO DGLAP [QCDNUM] and matrix elements [OPENQCDRAD], $n_f = 3$
- $\mu_f = \mu_r = \sqrt{Q^2 + 4m_Q^2}$ varied by factor 2 (model unc.)
- **free $m_c(m_c)$, $m_b(m_b)$**
- $\alpha_s(M_Z)^{n_f=3} = 0.106$ ($\rightarrow \alpha_s(M_Z)^{n_f=5} = 0.118$)
- HERAPDF parametrisation, 14p
- fit uncertainty using $\Delta\chi^2 = 1$, model and parametrisation uncertainties

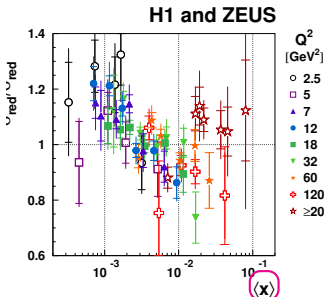
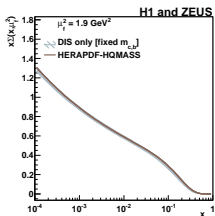
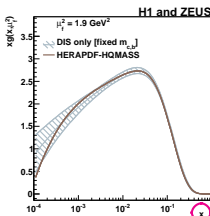
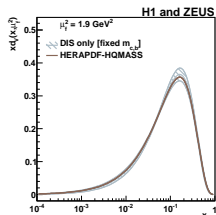
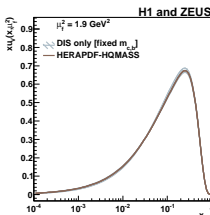
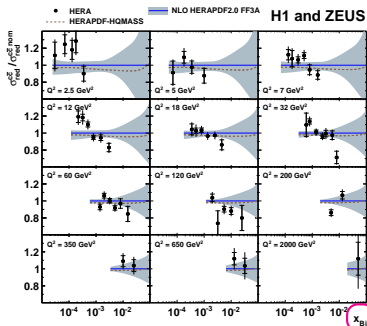
$$m_c(m_c) = 1290_{-41}^{+46}(\text{fit})_{-14}^{+62}(\text{mod})_{-31}^{+3}(\text{par}) \text{ MeV}$$

$$m_b(m_b) = 4049_{-109}^{+104}(\text{fit})_{-32}^{+90}(\text{mod})_{-31}^{+1}(\text{par}) \text{ MeV}$$

\Rightarrow **determined precise HQ masses consistent with world average**

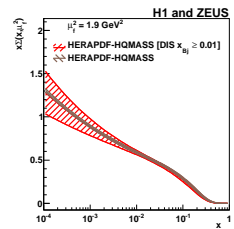
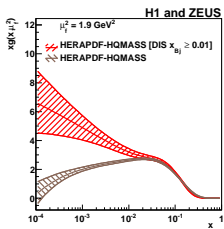
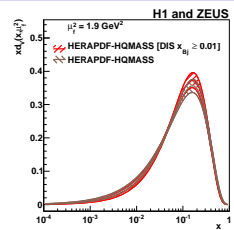
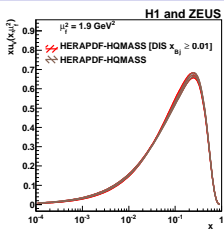
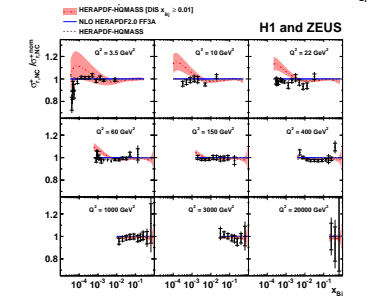
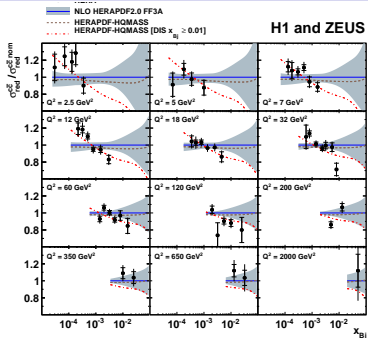
PDG2016: $m_c(m_c) = 1270 \pm 30 \text{ MeV}$, $m_b(m_b) = 4180_{-30}^{+40} \text{ MeV}$

QCD analysis of combined charm and beauty data: PDFs



- $x \neq x_{Bj}$ for BGF!
- small impact of HF data on PDFs
- difference in x slope persists after fit

QCD analysis of combined charm and beauty data: PDFs



- cut $x_{Bj} > 0.01$ on inclusive data
- observed change for low x gluon:
- better description of HF data
- but worse description of (not fitted) inclus. data

New combined HERA charm and beauty data:

- improvement in precision w.r.t previous HERA results for charm
- first combined HERA results for beauty
- enable precise determination of charm and beauty masses
- reveal tension in describing simultaneously HF and inclusive HERA data

[Eur.Phys.J. C78 (2018) 473]

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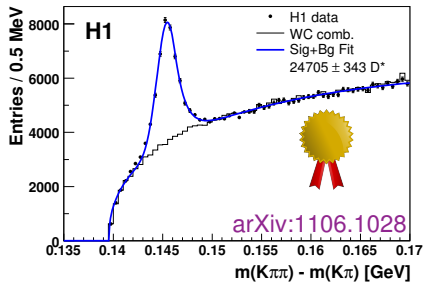
[Eur.Phys.J. C78 (2018) 473]

*HERA experiments continue producing valuable results
> 10 years after HERA was shut down!*

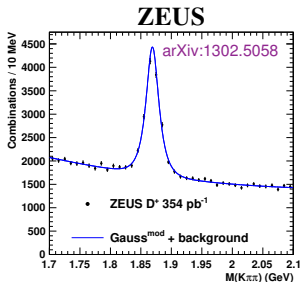
BACKUP

BACKUP. Measurement of charm production at HERA

“Golden” decay channel
 $D^* \rightarrow D^0(K\pi)\pi_s$



Weakly decaying charm
 hadrons

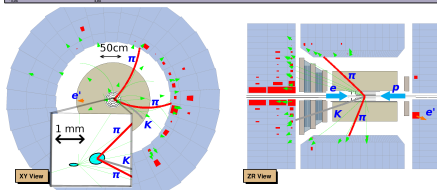


Dedicated H1ZEUS combination:

“Combination of differential $D^{*\pm}$
 cross-section measurements in
 deep-inelastic ep scattering at HERA”

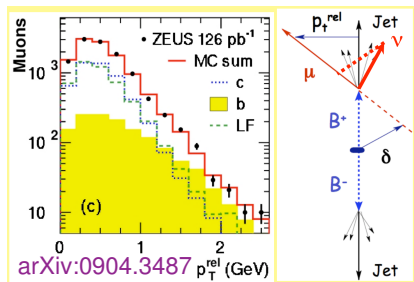
[JHEP09 (2015) 149]

ZEUS Run 61453 Event 76692				date: 26-11-2006 time: 08:38:10	
E_{beam} [GeV]	E_{reco} [GeV]	E_{miss} [GeV]	E_{had} [GeV]	E_{had} [GeV]	E_{had} [GeV]
p_{beam} [GeV]	p_{reco} [GeV]	p_{miss} [GeV]	p_{had} [GeV]	p_{had} [GeV]	p_{had} [GeV]
η_{beam} [GeV]	η_{reco} [GeV]	η_{miss} [GeV]	η_{had} [GeV]	η_{had} [GeV]	η_{had} [GeV]
ϕ_{beam} [GeV]	ϕ_{reco} [GeV]	ϕ_{miss} [GeV]	ϕ_{had} [GeV]	ϕ_{had} [GeV]	ϕ_{had} [GeV]

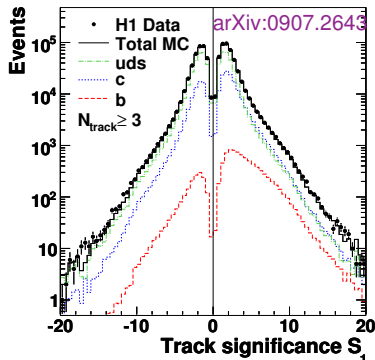


BACKUP. Measurement of c and b production at HERA

Semi-leptonic (SL) HQ decays



Inclusive lifetime tagging



Recent reviews of HF production at HERA:

- O. Behnke, A. Geiser, M. Lisovskyi, “Charm, Beauty and Top at HERA”, Prog. Part. Nucl. Phys. 84 (2015) 1
- O.Z., “Charm Production and QCD Analysis at HERA and LHC”, Eur. Phys. J. C77 (2017) 151

BACKUP. Combination procedure

- fiducial cross sections extrapolated to full phase space using consistent NLO predictions [HVQDIS], account for relevant unc.
- combined at the level of **reduced cross sections** $\sigma_{\text{red}}^{c\bar{c}}$, $\sigma_{\text{red}}^{b\bar{b}}$
$$\sigma_{\text{red}}^{Q\bar{Q}} = \frac{d^2\sigma^{Q\bar{Q}}}{dx_{\text{Bj}}dQ^2} \cdot \frac{x_{\text{Bj}}Q^4}{2\pi\alpha^2(1+(1-y)^2)}$$
 (full phase space)
($Q\bar{Q}$ stands either for $c\bar{c}$ or $b\bar{b}$)
- combination accounts for correlation of systematic uncertainties, as well as correlation of c and b from same measurements
- \Rightarrow **significant improvement in precision** via cross calibration of different measurement techniques and c/b

Combined using HERAverager program

[<https://wiki-zeuthen.desy.de/HERAverager>]

well established combination method used in:

- previous HERA charm combination [EPJ C73 (2013) 2311]
- HERAPDF2.0 [EPJ C75 (2015) 580]
- ATLAS papers [1603.09222, 1512.02192, 1606.01736, 1612.03016]

- [2] H. Abramowicz *et al.* [ZEUS Collaboration], "Measurement of D^{\pm} Production in Deep Inelastic ep Scattering with the ZEUS detector at HERA", JHEP **05**, (2013) 023 [arXiv:1302.5058].
- [3] H. Abramowicz *et al.* [ZEUS Collaboration], "Measurement of D^{\pm} Production in Deep Inelastic Scattering at HERA", JHEP **05**, (2013) 097 [arXiv:1303.6578]. Erratum-ibid JHEP **02**, (2014) 106.
- [4] H. Abramowicz *et al.* [ZEUS Collaboration], "Measurement of beauty and charm production in deep inelastic scattering at HERA and measurement of the beauty-quark mass", JHEP **09**, (2014) 127 [arXiv:1405.6915].
- [5] H. Abramowicz *et al.* [ZEUS Collaboration], "Measurement of beauty production in deep inelastic scattering at HERA using decays into electrons", Eur. Phys. J. **C71**, (2011) 1573 [arXiv:1101.3692].
- [6] H. Abramowicz *et al.* [ZEUS Collaboration], "Measurement of beauty production in DIS and F2bb extraction at ZEUS", Eur. Phys. J. **C69**, (2010) 347 [arXiv:1005.3396].
- [7] S. Chekanov *et al.* [ZEUS Collaboration], "Measurement of charm and beauty production in deep inelastic ep scattering from decays into muons at HERA", Eur. Phys. J. **C65**, (2010) 65 [arXiv:0904.3487].
- [8] F. D. Aaron *et al.* [H1 Collaboration], "Measurement of the Charm and Beauty Structure Functions using the H1 Vertex Detector at HERA", Eur. Phys. J. **C65**, (2010) 89 [arXiv:0907.2643].
- [9] A. Aktas *et al.* [H1 Collaboration], "Production of D^{*+} Mesons with Dijets in Deep-Inelastic Scattering at HERA", Eur. Phys. J. **C51**, (2007) 271 [hep-ex/0701023].
- [10] F. D. Aaron *et al.* [H1 Collaboration], "Measurement of $D^{*{\pm}}$ Meson Production and Determination of F_2^{charm} at low Q2 in Deep-Inelastic" Eur. Phys. J. **C71**, (2011) 1769 [arXiv:1106.1028].
- [11] F. D. Aaron *et al.* [H1 Collaboration], "Measurement of the D^{*+} Meson Production Cross Section and $F(2)^*(c\text{-}\bar{c})$, at High Q^{*2} , in ep Scattering at HERA", Phys. Lett. **B686**, (2010) 91 [arXiv:0911.3989].
- [12] J. Breitweg *et al.* [ZEUS Collaboration], "Measurement of D^{*+} production and the charm contribution to F2 in deep inelastic scattering at HERA", Eur. Phys. J. **C12**, (2000) 35 [hep-ex/9908012].
- [13] S. Chekanov *et al.* [ZEUS Collaboration], "Measurement of D^{*+} production in deep inelastic e^+p scattering at HERA", Phys. Rev. **D69**, (2004) 012004 [hep-ex/0308068].
- [14] S. Chekanov *et al.* [ZEUS Collaboration], "Measurement of D^{*+} and D_0 production in deep inelastic scattering using a lifetime tag at HERA", Eur. Phys. J. **C63**, (2009) 171 [arXiv:0812.3775].

BACKUP. Combination procedure

- Take measured visible x-section σ_{vis} and extrapolate to full phase space σ_{red} using consistent NLO setup: $\sigma_{\text{red}} = \sigma_{\text{vis}} \frac{\sigma_{\text{red}}^{\text{NLO}}}{\sigma_{\text{vis}}^{\text{NLO}}}$ [HVQDIS]
- Combine σ_{red} accounting for bin-to-bin correlations [HERAverager]

NLO setup for extrapolation as in [DESY-12-172]

- pole masses $m_c = 1.5 \pm 0.15$ GeV, $m_b = 4.5 \pm 0.25$ GeV
consistent with extracted from data: $m_c = 1.43 \pm 0.04$ GeV, $m_b = 4.35 \pm 0.11$ GeV
and consistent with PDG: $m_c = 1.67 \pm 0.07$ GeV, $m_b = 4.78 \pm 0.06$ GeV
- $\mu_R = \mu_F = \sqrt{Q^2 + 4m_Q^2}$, varied simultaneously by factor 2
- $\alpha_s^{n_f=3}(M_Z) = 0.105 \pm 0.002$ [$\alpha_s^{n_f=5}(M_Z) = 0.116 \pm 0.002$]
- HERAPDF1.0 FFNS, $n_f = 3$, assign 2% uncor. unc.
(checked vs HERAPDF2.0: see backup)
- c fragmentation: Kartvelishvili frag. function parametrised as step function with k_T kink (H1, ZEUS meas. [DESY-08-080, DESY-08-209])
- b fragmentation: Peterson $\epsilon_b = 0.0035 \pm 0.0020$ [NP B565 (2000) 245]
- charm fragmentation fractions [EPJ C76 (2016) 397]
- branching ratios PDG2016
- hadronisation uncertainties for data with jets in the final state

$$\chi^2(\mathbf{m}, \mathbf{b}) = \sum_{e=1}^{N_e} \sum_{i=1}^{N_m} \frac{\left(m_i - \sum_{j=1}^{N_s} \Gamma_i^{e,j} b^{e,j} - \mu_i^e\right)^2}{\sigma_i^{e2}} + \sum_{j=1}^{N_s} b^{e,j2}$$

Minimised in iterative procedure

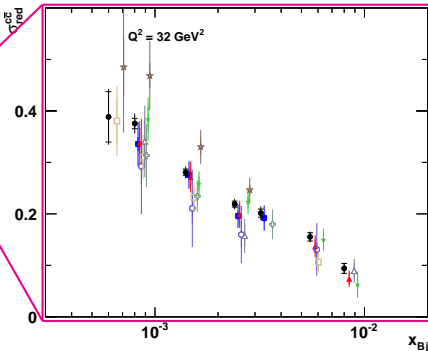
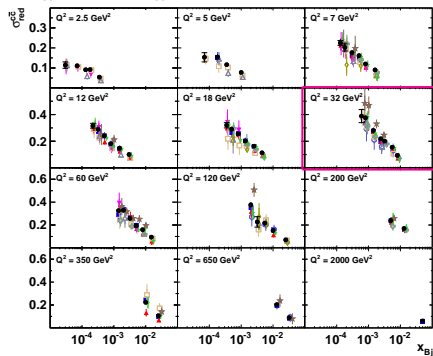
CHARM

H1 and ZEUS

H1 and ZEUS

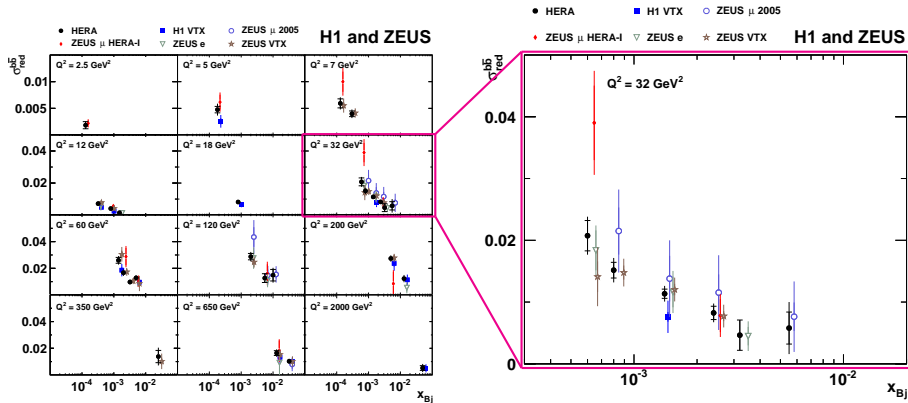
- HERA
- H1 D* HERA-I
- ZEUS D* 96-97
- ZEUS D* HERA-II
- H1 VTX
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- ZEUS D* 98-00
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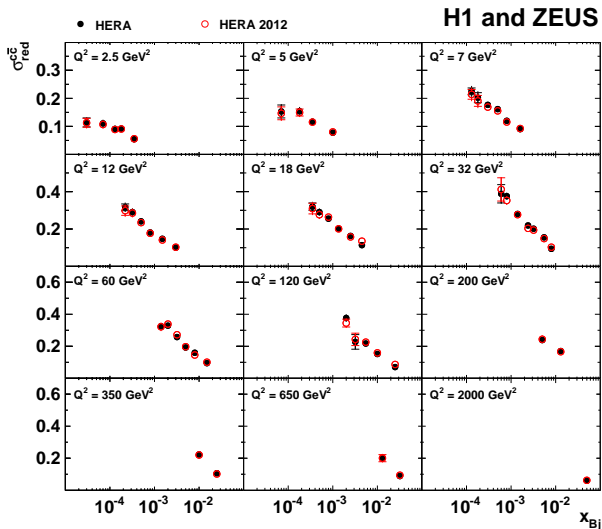
→ Significantly improved precision compared to input measurements

BEAUTY



→ **Significantly improved precision compared to input measurements**

BACKUP. New charm data compared to previous HERA results



FFNS, BEAUTY

Predictions obtained with OPENQCDRAD interfaced in xFitter

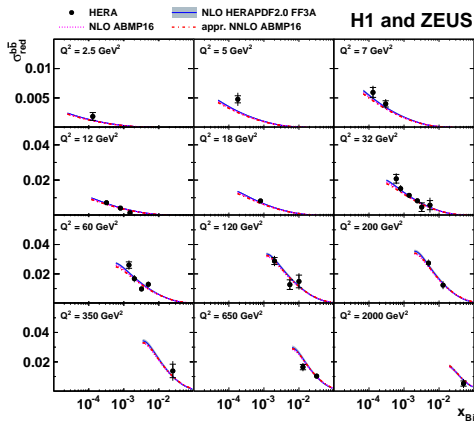
www-zeuthen.desy.de/~alekhin/OPENQCDRAD

www.xfitter.org

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FFNS, $n_f = 3$: reliable in this kinematic range

- overall fair description, somewhat different x slope
- description not improved at approximate NNLO



FFNS, BEAUTY

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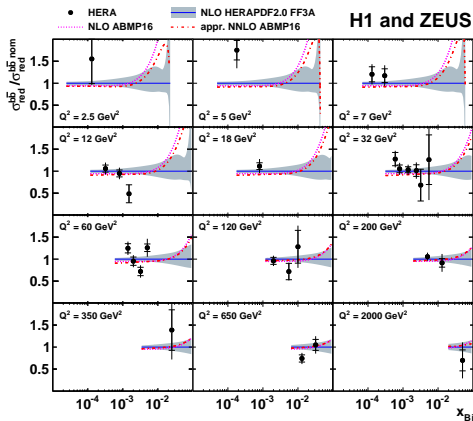
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[PDG2016]

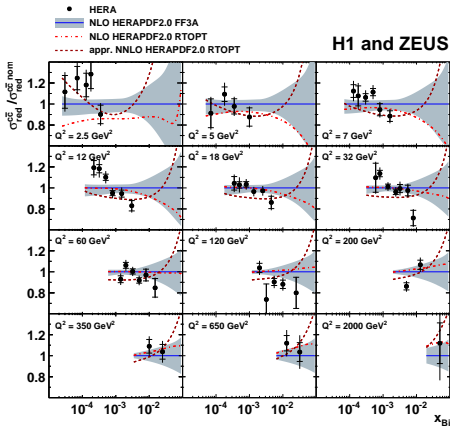
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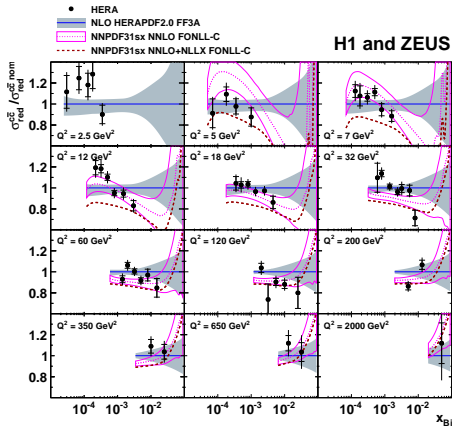


BACKUP. VFNS predictions compared to combined data

RTOPT [default HERAPDF2.0]



NNPDF3.1 w/ and w/o small-x resummation [1710.05935]



- considered VFNS predictions do not give better data description
- NNPDF3.1: better x_{Bj} slope, but worse normalisation and Q^2

BACKUP. QCD analysis settings

Similar to HERAPDF2.0 FF, using running HQ mass definition:

- xFitter-1.2.0
- Input data:
 - ▶ HERA $e^\pm p$ inclusive data, $Q_{\min}^2 > 3.5 \text{ GeV}^2$ [1506.06042]
 - ▶ new HERA c and b combined
- FFNS $n_f = 3$ ('FF ABM RUNM'), $(\alpha_s(F_L) = \alpha_s(F_2))$
- $\alpha_s^{n_f=3}(M_Z) = 0.106$
- free $m_c(m_c)$, $m_b(m_b)$, or PDG $m_c(m_c) = 1.27 \text{ GeV}$, $m_c(m_c) = 4.18 \text{ GeV}$
- DGLAP NLO [QCDNUM]
- PDF parametrisation: 14p HERAPDF at $\mu_{f0}^2 = 1.9 \text{ GeV}^2$, $f_s = 0.4$:

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g}$$

$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2)$$

$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}}$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x)$$

$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}$$

Additional constrains:

$$A_{\bar{U}} = A_{\bar{D}}(1 - f_s), B_{\bar{U}} = B_{\bar{D}}, C'_g = 25$$

$$\int_0^1 [\sum_i (q_i(x) + \bar{q}_i(x)) + g(x)] x dx = 1$$

$$\int_0^1 [u(x) - \bar{u}(x)] dx = 2,$$

$$\int_0^1 [d(x) - \bar{d}(x)] dx = 1$$

- fit ($\Delta\chi^2 = 1$), model (scales, α_s , f_s , Q_{\min}^2) and par. (μ_{f0} , $E_{u_v} = 0$) unc.

BACKUP. Discussion of HQ mass extraction

$$m_c(m_c) = 1290_{-41}^{+46}(\text{fit})_{-14}^{+62}(\text{mod})_{-31}^{+3}(\text{par}) \text{ MeV}$$

$$m_b(m_b) = 4049_{-109}^{+104}(\text{fit})_{-32}^{+90}(\text{mod})_{-31}^{+1}(\text{par}) \text{ MeV}$$

Results have sizable *model* and *parametrisation* uncertainty:

- *model* uncertainties dominated by *scale variations*
- *parametrisation* uncertainties dominated by reduced *13p form*: closely related to inclusive HERA data in the fit

Using inclusive HERA data only:

$$m_c(m_c) = 1798_{-134}^{+144}(\text{fit}) \text{ MeV}$$

$$m_b(m_b) = 8450_{-1810}^{+2280}(\text{fit}) \text{ MeV}$$

No full uncertainty evaluation, but observed large sensitivity to PDF parametrisation (\rightarrow 13p):

$$m_c(m_c) = 1798 \rightarrow 1450 \text{ MeV,}$$

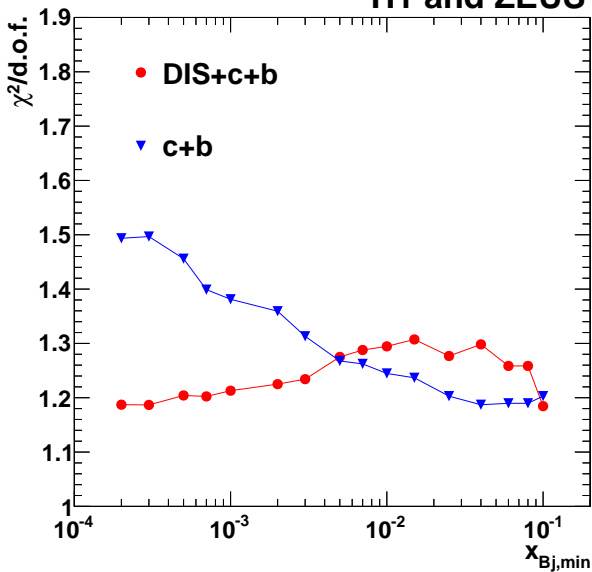
$$m_b(m_b) = 8450 \rightarrow 3995 \text{ MeV}$$

$$\begin{aligned} xg(x) &= A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g} \\ x u_v(x) &= A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + \boxed{E_{u_v}} x^2) \\ x d_v(x) &= A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}} \\ x \bar{U}(x) &= A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x) \\ x \bar{D}(x) &= A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}} \end{aligned}$$

$$13p: E_{u_v} = 0$$

- \Rightarrow inclusive HERA data alone cannot constrain HQ masses reliably
- \Rightarrow interplay of PDFs and HQ masses needs careful treatment

H1 and ZEUS



BACKUP. $m_c(m_c)$ extraction in FFNS and VFNS

JHEP 1608 (2016) 050



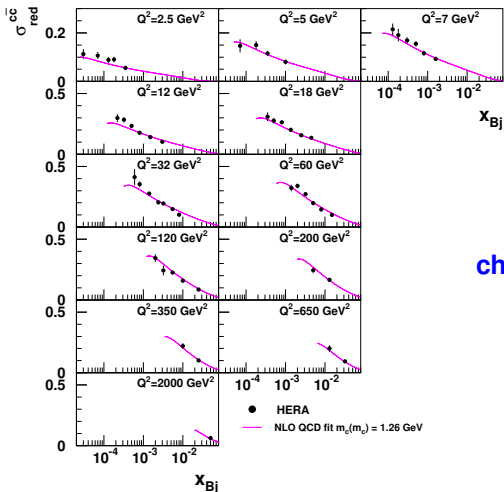
variation	FONLL-C	FFN
central	1.335 ± 0.043	1.318 ± 0.054
$Q_0^2 = 1.5$	$1.354 [+0.019]$	$1.329 [+0.011]$
D_{uv} non-zero	$1.340 [+0.005]$	$1.308 [-0.010]$
$f_s = 0.3$	$1.338 [+0.003]$	$1.320 [+0.002]$
$f_s = 0.5$	$1.332 [-0.003]$	$1.315 [-0.003]$
$m_b(m_b) = 3.93$ GeV	$1.330 [-0.005]$	$1.312 [-0.006]$
$m_b(m_b) = 4.43$ GeV	$1.343 [+0.008]$	$1.324 [+0.006]$
$\alpha_s(M_Z) = 0.1165$	$1.342 [+0.007]$	$1.332 [+0.014]$
$\alpha_s(M_Z) = 0.1195$	$1.329 [-0.006]$	$1.300 [-0.018]$
$\mu_F^2 = \mu_R^2 = 2 \cdot Q^2$	$1.347 [+0.012]$	$1.314 [-0.004]$
$\mu_F^2 = \mu_R^2 = Q^2/2$	$1.361 [+0.026]$	$1.363 [+0.045]$
FONLL Damping power = 1	$1.352 [+0.017]$	-
FONLL Damping power = 4	$1.327 [-0.008]$	-

A determination of $m_c(m_c)$ from HERA data using a matched heavy-flavor scheme

- consistent results obtained in FFNS and FONLL, with somewhat different decomposition of uncertainties
- \Rightarrow VFNS can be used for \overline{MS} mass extraction, if all uncertainties from extra parameters are considered

BACKUP. Running of charm mass from HERA DIS data

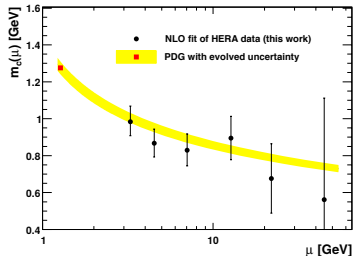
Gizsko et al., PLB775 (2017) 233 (work partially done within scope of PROSA, ZEUS and H1 coll.)



- Determined using earlier published HERA charm data [EPJ C73 (2013) 2311]
- $\overline{\text{MS}}$ charm mass $m_c(m_c)$ extracted in regions of Q^2 and translated to appropriate scale μ



check of QCD running mass concept



New combined HERA charm and beauty data

Eur.Phys.J. C78 (2018) 473

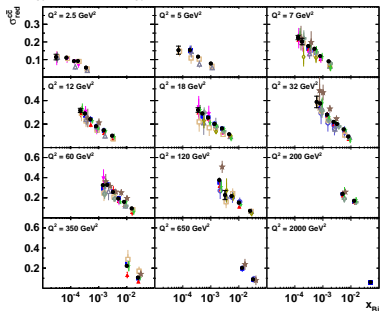
- improvement in precision w.r.t previous HERA results for charm
- first combined HERA results for beauty
- enable precise determination of charm and beauty masses
- reveal tension in describing both HF and inclusive HERA data

$$m_c(m_c) = 1290_{-41}^{+46}(\text{fit})_{-14}^{+62}(\text{mod})_{-31}^{+3}(\text{par}) \text{ MeV}$$

$$m_b(m_b) = 4049_{-109}^{+104}(\text{fit})_{-32}^{+90}(\text{mod})_{-31}^{+1}(\text{par}) \text{ MeV}$$

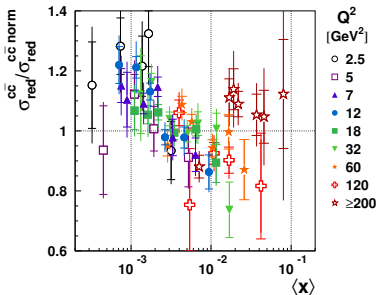
- HERA
- H1 D* HERA-I
- △ ZEUS D* 96-97
- ▽ ZEUS D* HERA-II
- H1 VTX
- ZEUS μ 2005
- ◇ ZEUS D*
- ▲ H1 D* HERA-II
- ZEUS D* 98-00
- ZEUS D*

H1 and ZEUS



O. Zenaiev

H1 and ZEUS



Heavy quark production at HERA

32 / 13