

# Determination of EW Parameters Using H1 Data



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on behalf of the H1 Collaboration



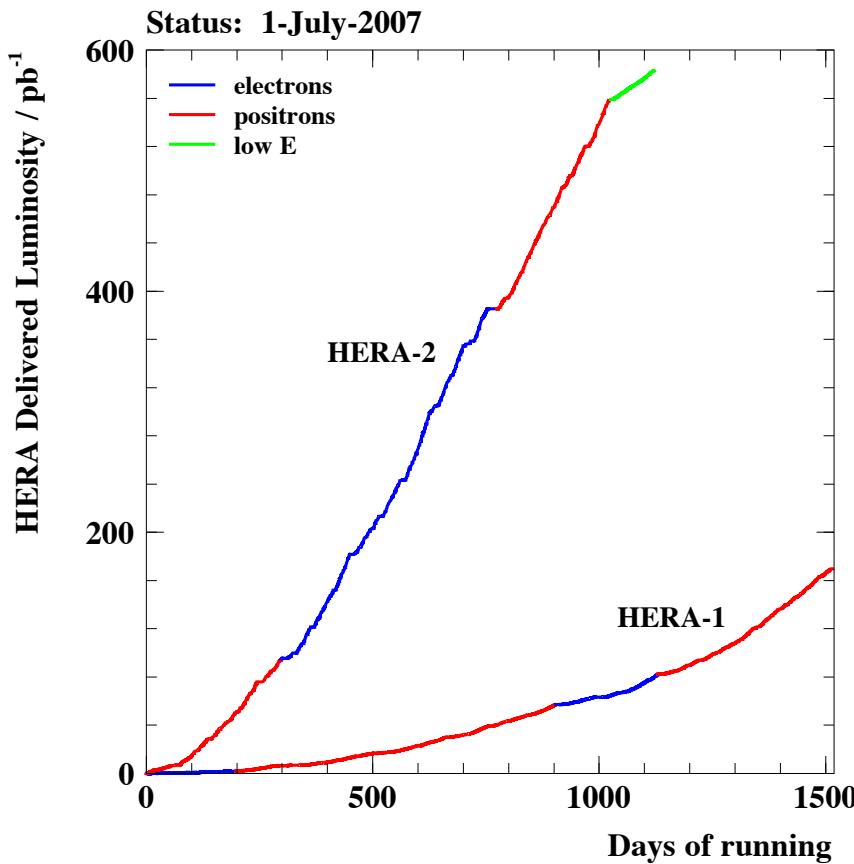
based on arXiv:1806.01176, submitted to EPJC

## Outline

- Introduction
- Analysis strategy
- Results
- Summary

# Introduction

ep collider, HERA, used to be the largest electron microscope  
A large number of precisely measured inclusive cross sections  
These are primary inputs for all modern PDF sets



## HERA-I (1992-2000):

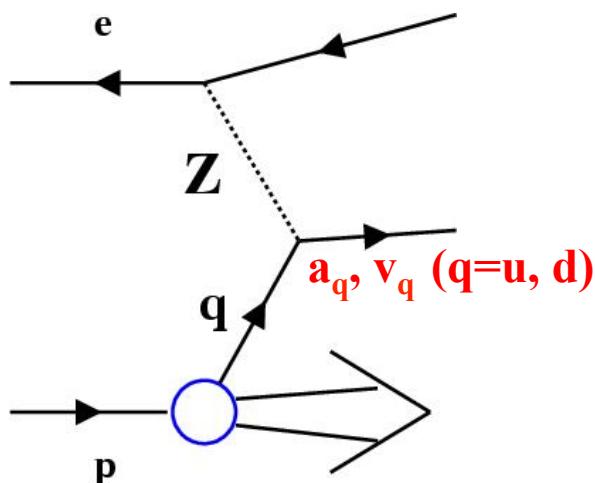
- First EW analysis by H1

## HERA-II (2003-2007):

- Increased lumi ( $\times 10$   $e^-$ ,  $\times 2$   $e^+$ )
- Longitudinally polarised  $e^\pm$

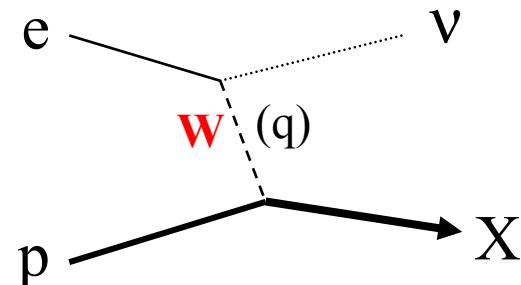
This talk reports refined and extended new EW analyses using all HERA-I & -II data

# Neutral and Charged Current DIS Interactions



Sensitive to EW parameters  
(e.g. light quark couplings &  $W$  boson mass) in space-like regime

$$a_q \equiv g_A^q, v_q \equiv g_V^q$$



## Event kinematics:

$Q^2 = -q^2$ : Boson virtuality

$x$ : Momentum fraction of struck partons

$y = Q^2/(sx)$ : Inelasticity

$\sqrt{s}$ : Centre-of-mass energy

# Unpolarised HERA-I NC Data

$$\frac{d^2\sigma_{\text{NC}}^\pm}{dxdQ^2} \sim Y_+ \tilde{F}_2 \mp Y_- x \tilde{F}_3$$

$g_V^e \sim 0 \rightarrow$  some of the terms are negligible  
but fully considered in the fit

$$\begin{aligned}\tilde{F}_2 &= F_2 - g_V^e \kappa_Z F_2^{\gamma Z} + (g_V^e g_V^e + g_A^e g_A^e) \kappa_Z^2 F_2^Z \\ x \tilde{F}_3 &= -g_A^e \kappa_Z x F_3^{\gamma Z} + 2g_V^e g_A^e \kappa_Z^2 x F_3^Z\end{aligned}$$

$$F_2^Z = x \sum_q (g_V^q g_V^q + g_A^q g_A^q) \{q + \bar{q}\}$$

$$x F_3^{\gamma Z} = 2x \sum_q Q_q g_A^q \{q - \bar{q}\}$$

$$Y_\pm = 1 \pm (1 - y)^2$$

$$\kappa_Z = \frac{Q^2}{Q^2 + m_Z^2} \frac{G_F m_Z^2}{2\sqrt{2}\pi\alpha}$$

$$g_A^f = \sqrt{\rho_{\text{NC}}} I_{L,f}^3$$

$$g_V^f = \sqrt{\rho_{\text{NC}}} (I_{L,f}^3 - 2Q_f \kappa_{\text{NC},q} \sin^2 \theta_W)$$

In on-shell scheme:

$$\sin^2 \theta_W = 1 - \frac{m_W^2}{m_Z^2}$$

$$G_F = \frac{\pi\alpha}{\sqrt{2}m_W^2} \left[ 1 - \frac{m_W^2}{m_Z^2} \right]^{-1} (1 + \Delta r)$$

$$\Delta r = \Delta r(\alpha, m_W, m_Z, m_t, m_h, \dots)$$

# Polarised HERA-II NC Data

$$\frac{d^2\sigma_{\text{NC}}^\pm}{dxdQ^2} \sim Y_+ \tilde{F}_2 \mp Y_- x \tilde{F}_3$$

$$\begin{aligned}\tilde{F}_2 &\simeq F_2 - P_e g_A^e \kappa_Z F_2^{\gamma Z} + (g_V^e g_V^e + g_A^e g_A^e) \kappa_Z^2 F_2^Z \\ x\tilde{F}_3 &\simeq -g_A^e \kappa_Z x F_3^{\gamma Z} + P_e g_A^e g_A^e \kappa_Z^2 x F_3^Z\end{aligned}$$

$$F_2^{\gamma Z} = 2x \sum_q Q_q g_V^q \{q + \bar{q}\}$$

$$xF_3^Z = 2x \sum_q g_V^q g_A^q \{q - \bar{q}\}$$

Longitudinal polarised lepton beams at HERA-II introduces additional terms

$P_e$ : the degree of the longitudinal polarisation

Terms containing  $g_V^e$  have been neglected

# HERA-I and II CC Data

$$\frac{d^2\sigma_{\text{CC}}^\pm}{dx dQ^2} \simeq (1 \pm P_e) \frac{G_F^2}{4\pi x} \left[ \frac{m_W^2}{m_W^2 + Q^2} \right]^2 (Y_+ W_2^\pm \mp Y_- x W_3^\pm)$$

$$W_2^- = x (\rho_{\text{CC},eq}^2 U + \rho_{\text{CC},e\bar{q}}^2 \bar{D})$$
$$xW_3^- = x (\rho_{\text{CC},eq}^2 U - \rho_{\text{CC},e\bar{q}}^2 \bar{D})$$
$$U = u + c$$
$$\bar{D} = \bar{d} + \bar{s}$$

# Used Data Sets

HERA-I

HERA-II

	Data set	$Q^2$ -range [GeV $^2$ ]	$\sqrt{s}$ [GeV]	$\mathcal{L}$ [pb $^{-1}$ ]	No. of data points	Polarisation [%]
1	$e^+$ combined low- $Q^2$	(0.5) 8.5 – 150	301,319	20,22,97.6	94 (262)	–
2	$e^+$ combined low- $E_p$	(1.5) 8.5 – 90	225,252	12.2, 5.9	132 (136)	–
3	$e^+$ NC 94–97	150 – 30 000	301	35.6	130	–
4	$e^+$ CC 94–97	300 – 15 000	301	35.6	25	–
5	$e^-$ NC 98–99	150 – 30 000	319	16.4	126	–
6	$e^-$ CC 98–99	300 – 15 000	319	16.4	28	–
7	$e^-$ NC 98–99 high-y	100 – 800	319	16.4	13	–
8	$e^+$ NC 99–00	150 – 30 000	319	65.2	147	–
9	$e^+$ CC 99–00	300 – 15 000	319	65.2	28	–
10	$e^+$ NC L HERA-II	120 – 30 000	319	80.7	137	$-37.0 \pm 1.0$
11	$e^+$ CC L HERA-II	300 – 15 000	319	80.7	28	$-37.0 \pm 1.0$
12	$e^+$ NC R HERA-II	120 – 30 000	319	101.3	138	$+32.5 \pm 0.7$
13	$e^+$ CC R HERA-II	300 – 15 000	319	101.3	29	$+32.5 \pm 0.7$
14	$e^-$ NC L HERA-II	120 – 50 000	319	104.4	139	$-25.8 \pm 0.7$
15	$e^-$ CC L HERA-II	300 – 30 000	319	104.4	29	$-25.8 \pm 0.7$
16	$e^-$ NC R HERA-II	120 – 30 000	319	47.3	138	$+36.0 \pm 0.7$
17	$e^-$ CC R HERA-II	300 – 15 000	319	47.3	28	$+36.0 \pm 0.7$
18	$e^+$ NC HERA-II high-y	60 – 800	319	182.0	11	–
19	$e^-$ NC HERA-II high-y	60 – 800	319	151.7	11	–

For the first 2 data sets, only data above 8.5 GeV $^2$  are included

# Fit Strategy

- EW parameters fitted together with PDFs
  - so that their correlation is properly taken into account
  - the uncertainty of the EW parameters is not underestimated

- Fits performed with log-normal based likelihood function

$$\chi^2 = \sum_{ij} \log \frac{d_i}{\tilde{\sigma}_i} V_{ij}^{-1} \log \frac{d_j}{\tilde{\sigma}_j}$$

Correlation in data (d) taken into account in covariance matrix (V)

- Goodness of the fit (e.g. the PDF alone fit)
  - $\chi^2/\text{ndof}$ :  $1435/(1415-17)=1.03$

# Fit Strategy

- 5 sets of PDFs parameterised at starting scale  $Q_0^2=1.9 \text{ GeV}^2$

$$\begin{aligned}xg(x) &= A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g}, \\xu_v(x) &= A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1+E_{u_v} x^2), \\xd_v(x) &= A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}}, \\x\bar{U}(x) &= A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}}, \\x\bar{D}(x) &= A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}\end{aligned}$$

Momentum sum rule and quark counting rules applied to constrain  
 $A_g, A_{u_v}, A_{d_v}$  ( $C'_g$  fixed to 25)

Other constraints applied:  $A_{\bar{U}} = A_{\bar{D}}, B_{\bar{U}} = B_{\bar{D}}$

- DGLAP evolution & cross section calculations in NNLO QCD  
and in NLO EW

# Determination of W Boson Mass

Determination performed in on-shell scheme:

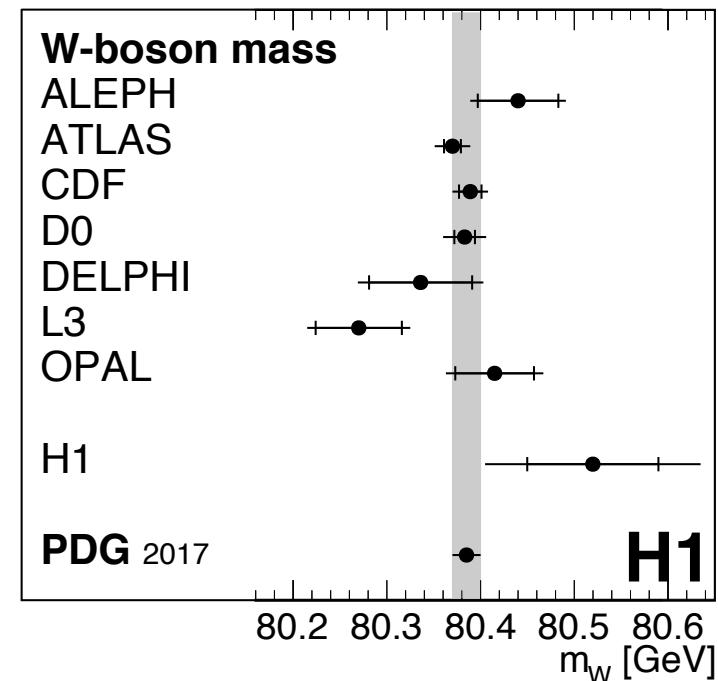
$$m_W = 80.520 \pm 0.070_{\text{stat}} \pm 0.055_{\text{syst}} \pm 0.074_{\text{PDF}} [\pm 0.115_{\text{total}}] \text{ GeV}$$

to be compared with HERA-I result:

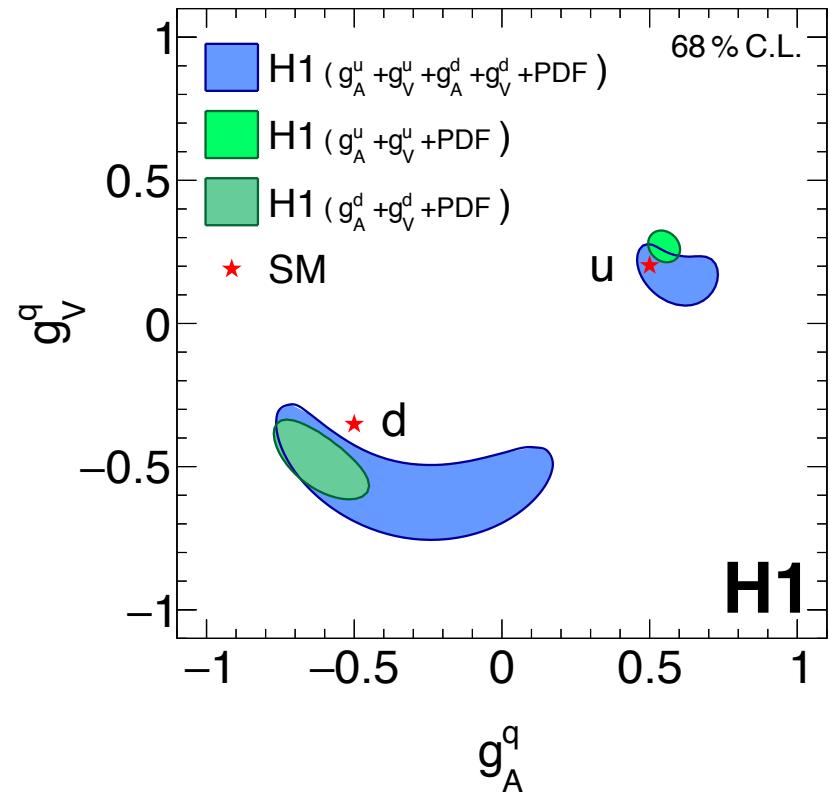
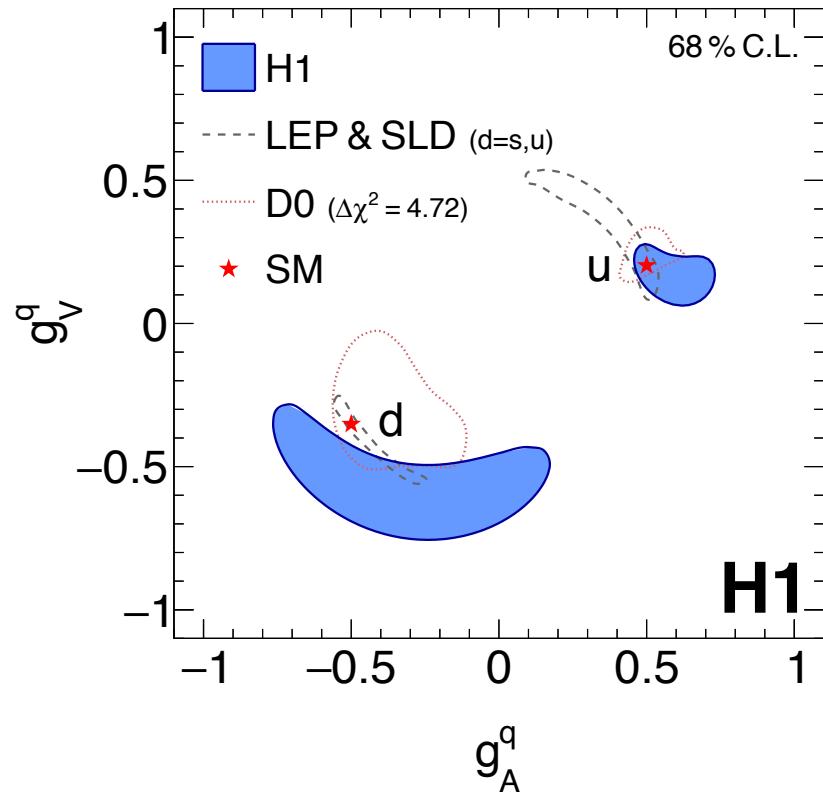
$$m_W = 80.786 \pm 0.205 (\text{exp})^{+0.063}_{-0.098} (\text{th}) \text{ GeV}$$

⇒ A factor ~2 improvement!

- The dominant sensitivity ( $\sim 120$  MeV) comes from the normalisation of the CC cross sections
- The quark and electron couplings to Z boson in the NC cross sections provides additional sensitivity of  $\sim 225$  MeV
- The W propagator term in CC cross sections provides a sensitivity of  $\sim 800$  MeV



# Light Quark Couplings to Z Boson



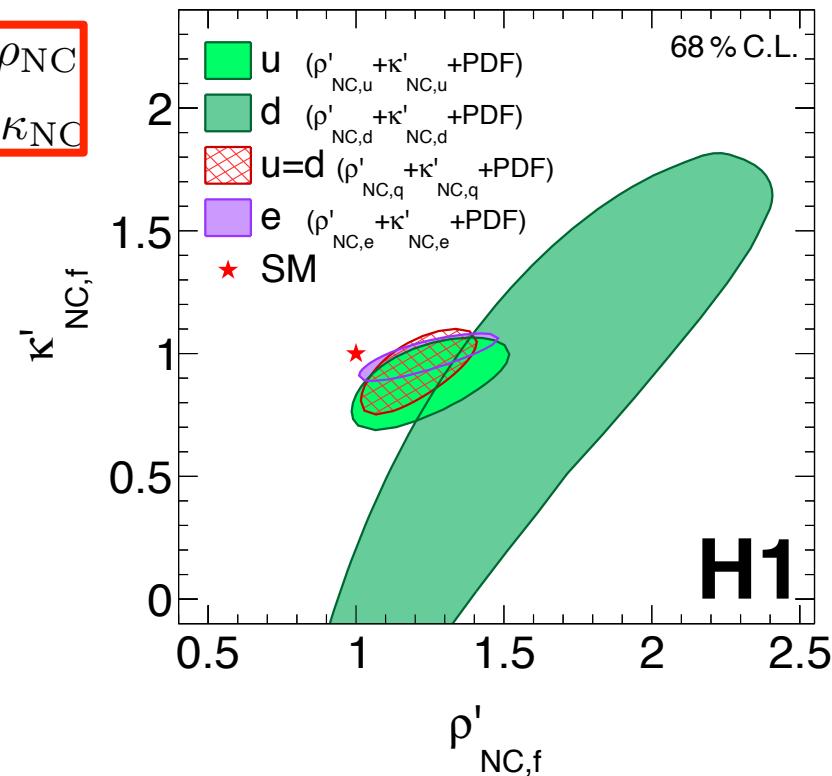
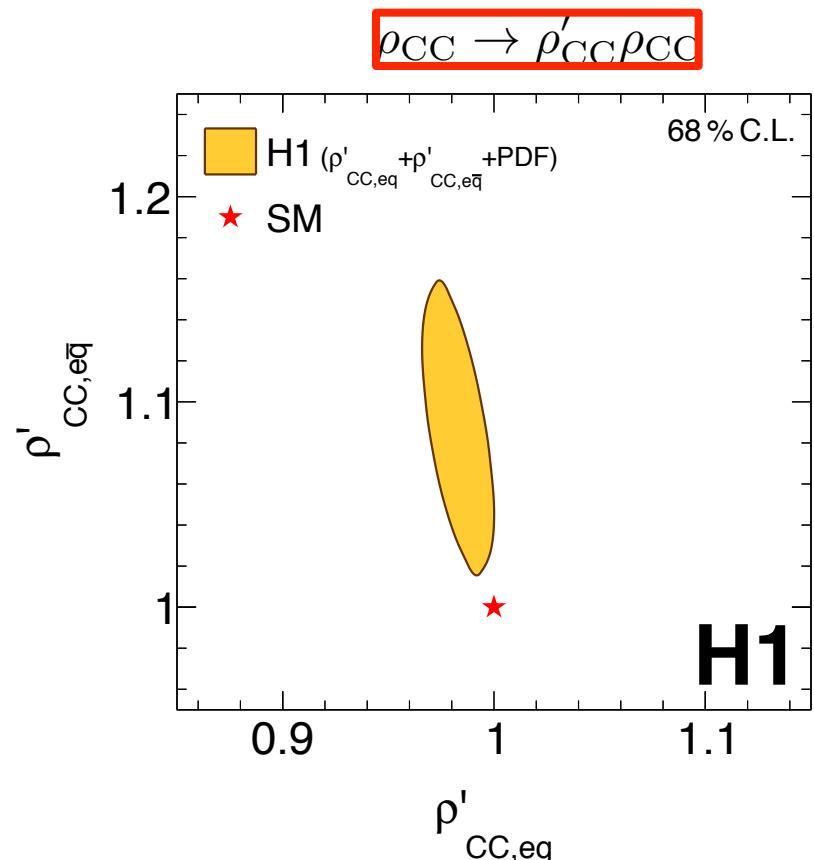
- Significant improvement over HERA-I determination
- 2-coupling fit is more precise due to the reduced correlation
- The results are competitive with other determinations

# Study BSM NC & CC Form Factors

- 4 fits for NC form factors
- 1 fit for CC form factors  
(all other parameters are set to their SM values)

$$\begin{aligned}\rho_{\text{NC}} &\rightarrow \rho'_{\text{NC}} \rho_{\text{NC}} \\ \kappa_{\text{NC}} &\rightarrow \kappa'_{\text{NC}} \kappa_{\text{NC}}\end{aligned}$$

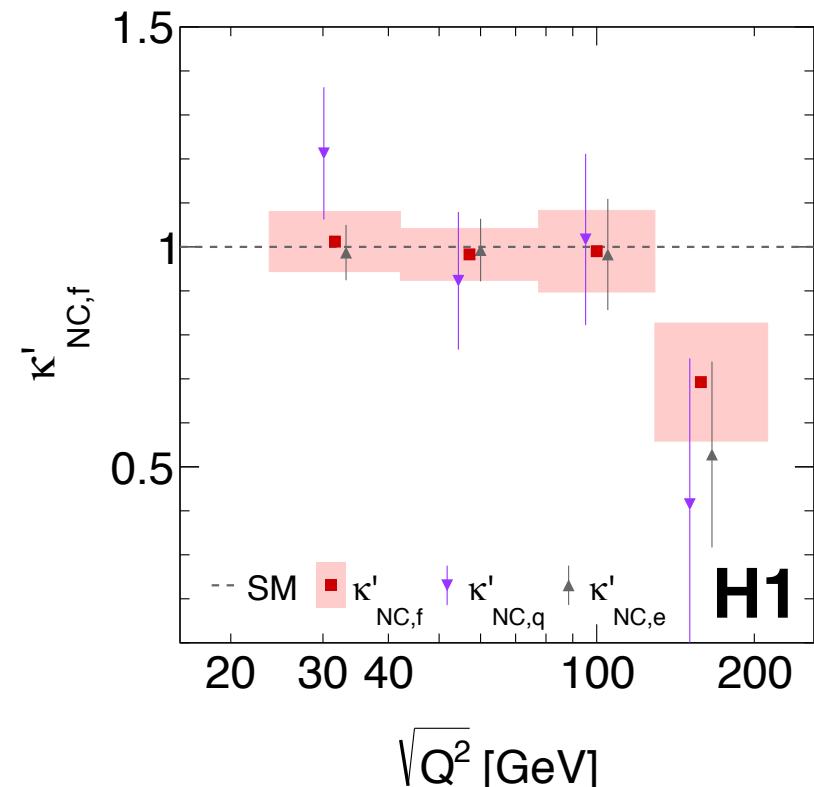
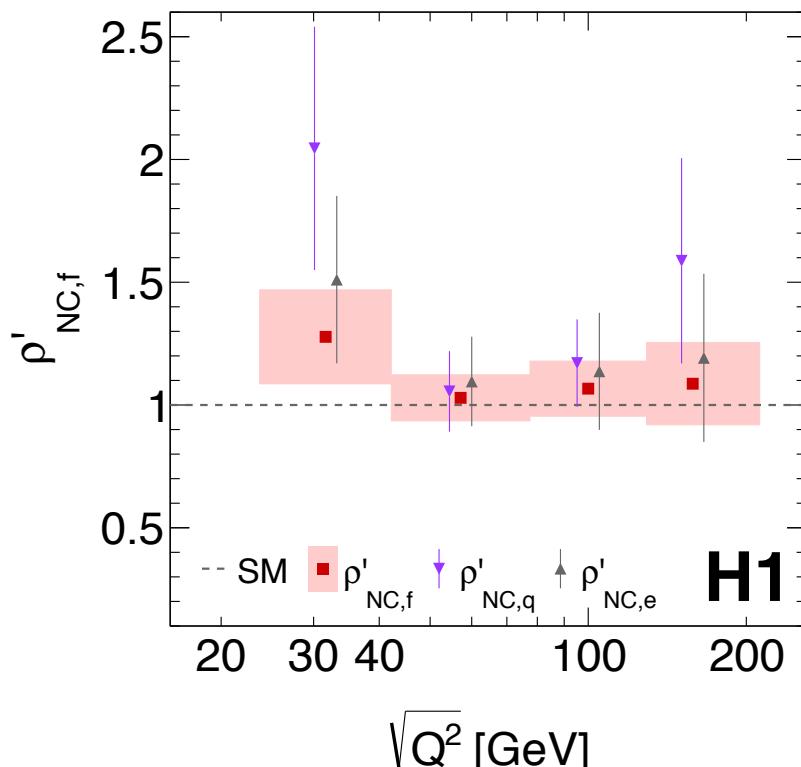
$$\begin{aligned}\rho_{\text{CC}} &\rightarrow \rho'_{\text{CC}} \rho_{\text{CC}} \\ \kappa_{\text{CC}} &\rightarrow \kappa'_{\text{CC}} \kappa_{\text{CC}}\end{aligned}$$



- Best constraint for CC form factors, NC form factors for d-type quark less constrained
- No significant deviations from SM

# Scale Dependence of BSM NC Form Factors

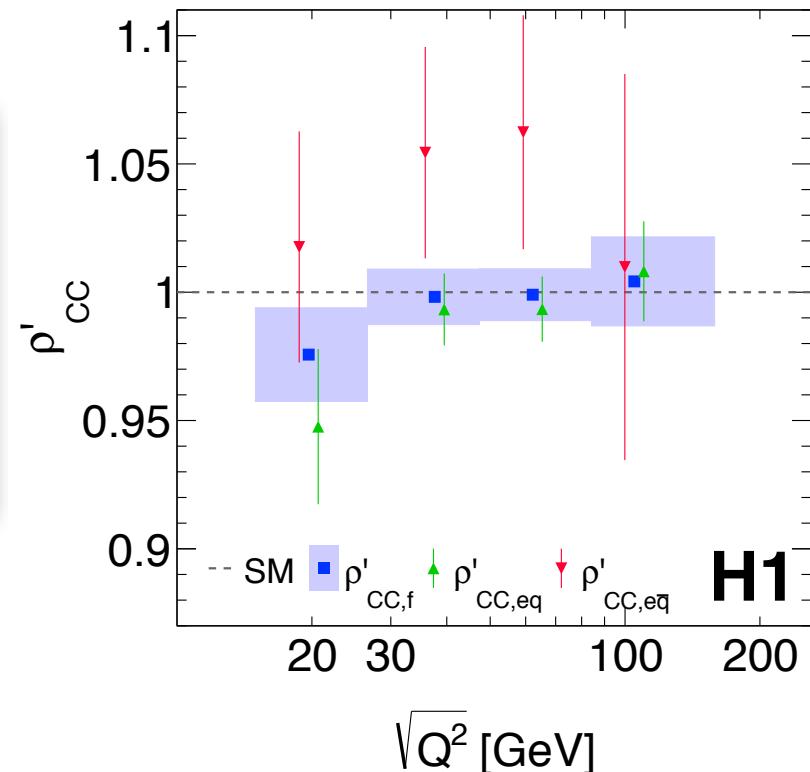
1. Fit quark form factors + PDFs only (set other parameters to their SM values)
2. Fit e form factors + PDFs only
3. Fit common fermion (e and quark) form factors + PDFs



► No significant scale dependence and deviation from SM

# Scale Dependence of BSM CC Form Factor

1. Fit up-type form factors + PDFs
2. Fit down-type form factors + PDFs
3. Fit common quark form factors + PDFs  
(all other parameters are set to their SM values)



- First scale dependence study for CC
- No significant scale dependence and deviation from SM

# Summary

- All HERA-I and HERA-II H1 data used to determine EW parameters together with PDFs
  - Precision wrt to HERA-I results improved by a factor of ~2
  - Thanks to the longitudinal polarised leptons beams and increased statistics precision of HERA-II high  $Q^2$  data
- The light quark couplings to Z boson are competitive to other determinations
  - Complementary test between space-like and time-like regimes
- BSM-like form factors and their scale dependence studied
  - First such study for CC
  - Within the uncertainties, no significant deviations from SM