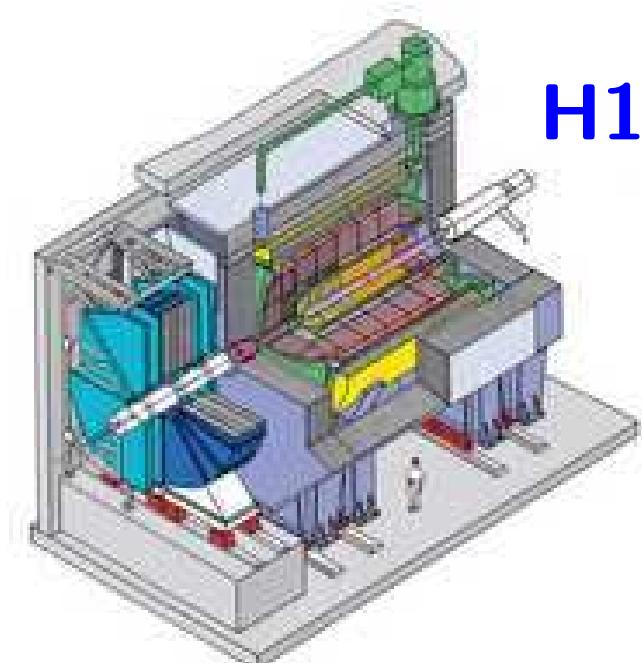


# Fragmentation of Charm into $D^+$ , $D^0$ , $D_s^+$ , $D^*$ and the Charm Fragmentation Function

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- Motivation for fragmentation study
- Fragmentation fractions  
( $D^+$ ,  $D^0$ ,  $D_s^+$ ,  $D^*$ )
- Fragmentation function ( $D^*$ )
- Conclusions



# Why Fragmentation?

Inclusive production cross-section of charm mesons:

$$\sigma(D) \sim f_{g/p}(x, \mu) \otimes ME \otimes D_{D/c}(x, \mu)$$

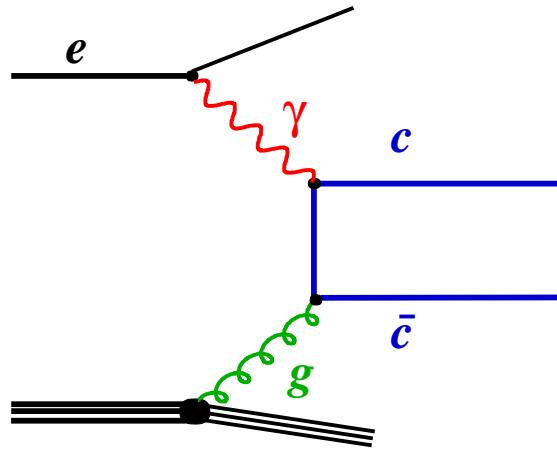
**Gluon Density Function**

*Experimentally determined*

**Hard Scattering**  
*(perturbative)*

**Fragmentation Function**

*Experimentally determined*



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# Experimental Study of Fragmentation

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## *Fragmentation*

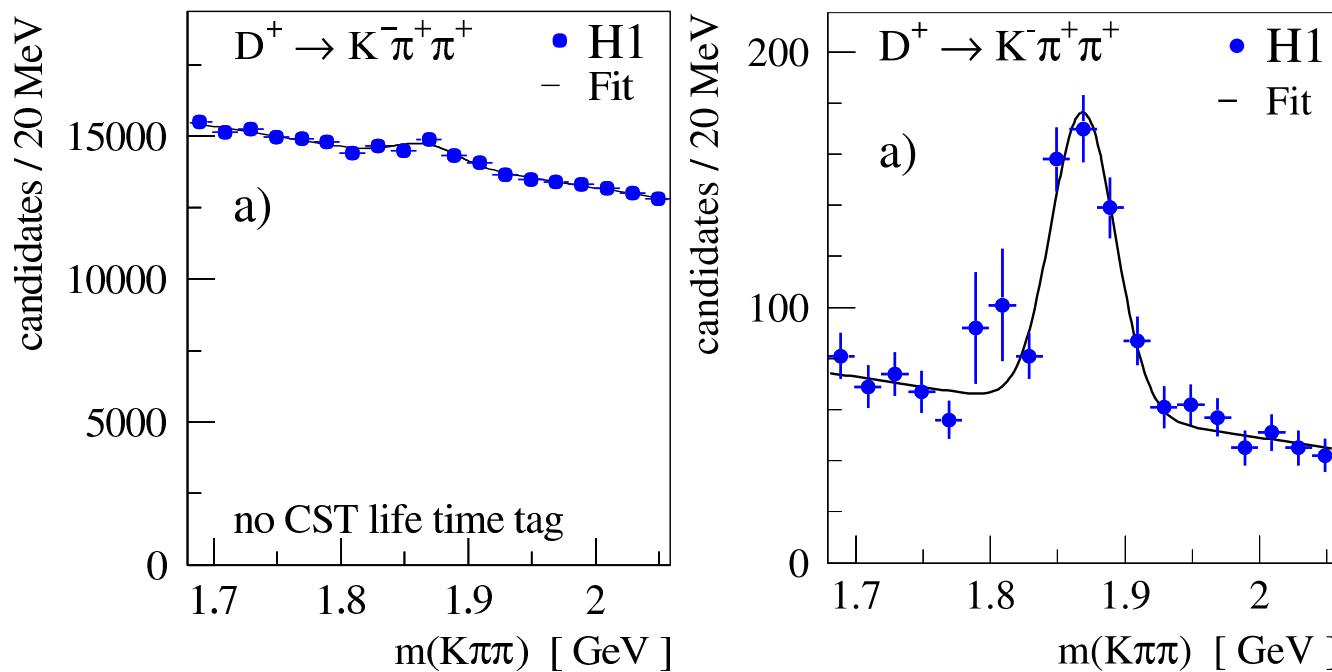
- ▷ nonperturbative process (transition from quark to hadron)  
     $\implies$  needs experimental study

## *Questions to be addressed :*

- 1.) what is the probability of c-quark to fragment to different charmed mesons  
*(fragmentation fractions)*
- 2.) what fraction of the c-quark's energy is transferred to the charmed meson  
*(fragmentation function)*

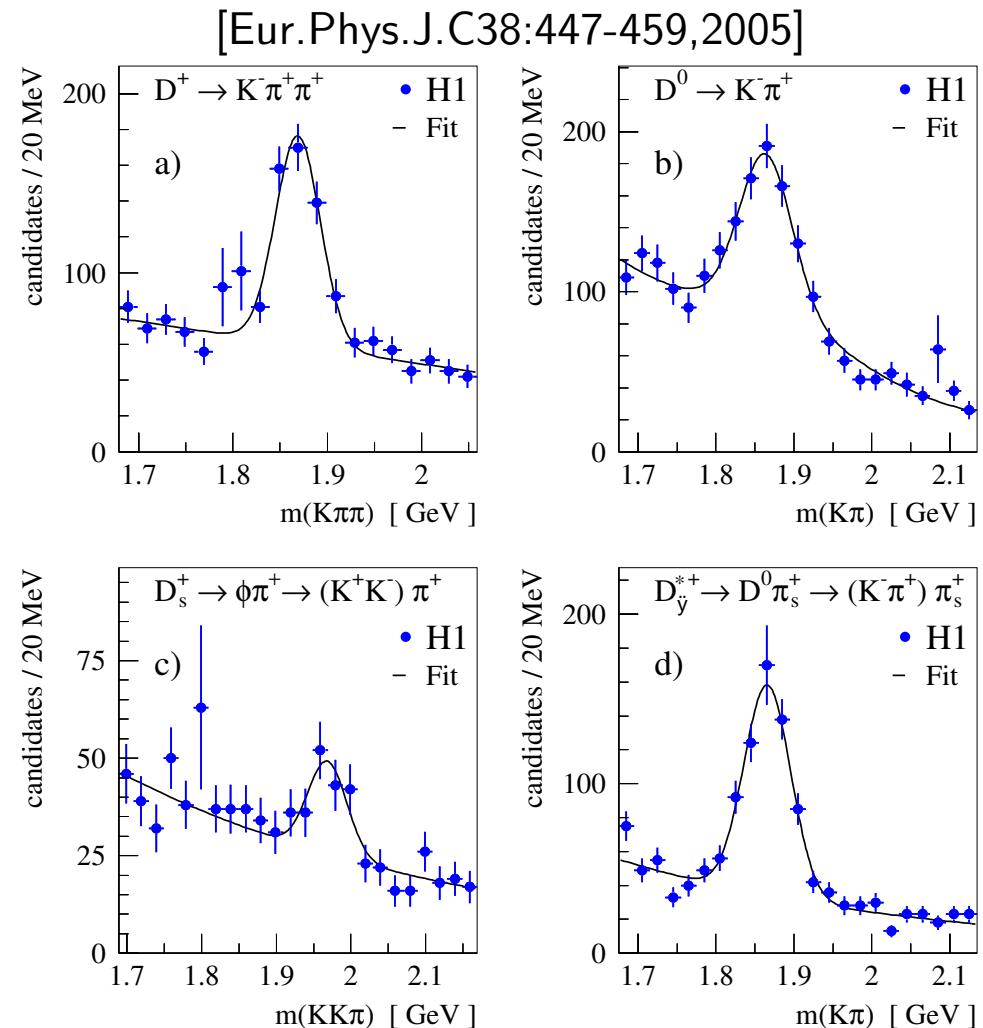
# Fragmentation Fractions of $D^+$ , $D^0$ , $D_s^+$ , $D^*$

- ▷ Charm tagging: reconstruction of **secondary vertex** with the central silicon tracker
- ▷ signal to background ratio can be improved significantly by cut on decay length significance ( $S_l = l/\sigma_l$ )



# D Meson Signals

- ▷ Kinematic region:  
 $2 < Q^2 < 100 \text{ GeV}^2$   
 $0.05 < y < 0.7$   
 $p_t(D) > 2.5 \text{ GeV}$   
 $|\eta(D)| < 1.5$
- ▷ Invariant mass spectra fitted:  
Gaussian + background
- ▷ Visible cross-sections were determined



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## Fragmentation Fractions

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- ▷ Fragmentation fractions  $f(c \rightarrow D)$  deduced from measured  $\sigma_{vis}$  using AROMA Monte Carlo:

$$f(c \rightarrow D) = \frac{\sigma_{vis}(c\bar{c} \rightarrow D) - \sigma_{vis}^{MC}(b\bar{b} \rightarrow D)}{\sigma_{vis}^{MC}(c\bar{c} \rightarrow D)} \cdot f_{MC}(c \rightarrow D)$$

[Eur.Phys.J.C38:447-459,2005]

Fragmentation factors	$D^+$	$D^0$	$D_s^+$	$D^*$
H1: $f(c \rightarrow D)$	$0.203 \pm 0.026$	$0.560 \pm 0.046$	$0.151 \pm 0.055$	$0.263 \pm 0.032$
World Average: $f(c \rightarrow D)$	$0.232 \pm 0.018$	$0.549 \pm 0.026$	$0.101 \pm 0.027$	$0.235 \pm 0.010$

Results compatible with world average values.

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## Fragmentation Ratios

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- ▷ Ratio of u to d:  $R_{u/d} = c\bar{u}/c\bar{d}$
- ▷ Strangeness suppression factor:  $\gamma_s = 2c\bar{s}/(c\bar{u} + c\bar{d})$
- ▷ Fraction of vector D mesons:  $P_V = V/(V + PS)$

[Eur.Phys.J.C38:447-459,2005]

Ratio	H1 measurement				$e^+e^-$ experiments		
	value	stat.error	syst.error	theo.error	value	error	ref.
$P_V^d$	0.693	$\pm 0.045$	$\pm 0.004$	$\pm 0.009$	0.595	$\pm 0.045$	[42]
$P_V^{u+d}$	0.613	$\pm 0.061$	$\pm 0.033$	$\pm 0.008$	0.620	$\pm 0.014$	[43]
$R_{u/d}$	1.26	$\pm 0.20$	$\pm 0.11$	$\pm 0.04$	1.02	$\pm 0.12$	[42]
$\gamma_s$	0.36	$\pm 0.10$	$\pm 0.01$	$\pm 0.08$	0.31	$\pm 0.07$	[44]

H1  $ep$  data agree with  $e^+e^-$   
⇒ universality of charm fragmentation fractions

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## Fragmentation Function

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Fragmentation function describes the energy transfer from quark to a given meson.

### *e<sup>+</sup>e<sup>-</sup> collisions*

- ▷ natural choice      
$$z = \frac{E_{D^*}}{\sqrt{s}/2} = \frac{E_{D^*}}{E_{\text{beam}}}$$
- ▷ assuming LO processes - direct measurement of non perturbative fragmentation function

### *ep collisions*

- ▷ choice of z observable not so obvious
- ▷ **differences:** IPS contribution,  
different kinematics

# The Experimental Methods

## Jet Method :

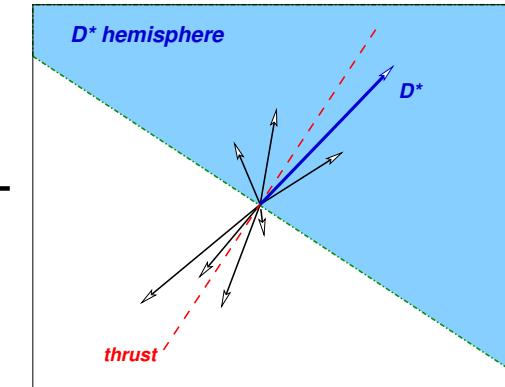
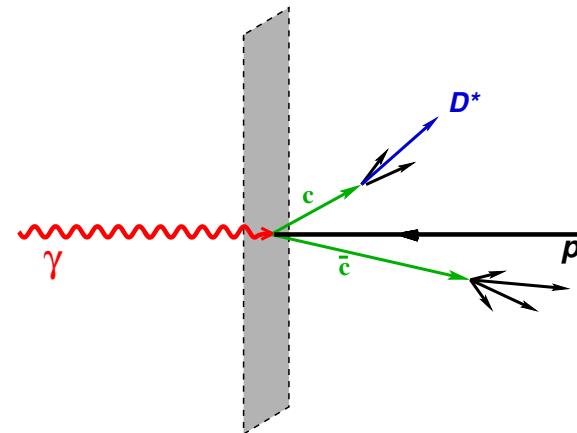
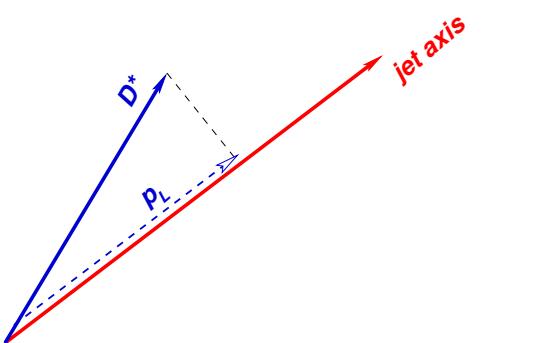
- ▷ the energy of  $c$ -quark is approximated by the energy of the reconstructed  $D^*$  jet

$$z_{\text{jet}} = \frac{(E+p_L)_{D^*}}{(E+p)_{\text{jet}}}$$

## Hemisphere Method :

- ▷ in  $\gamma p$ -frame the  $c\bar{c}$  pair is balanced in  $p_t$   
 $\implies$  possibility to divide event into two hemispheres

$$z_{\text{hem}} = \frac{(E+p_L)_{D^*}}{\sum_{\text{hem}}(E+p)}$$

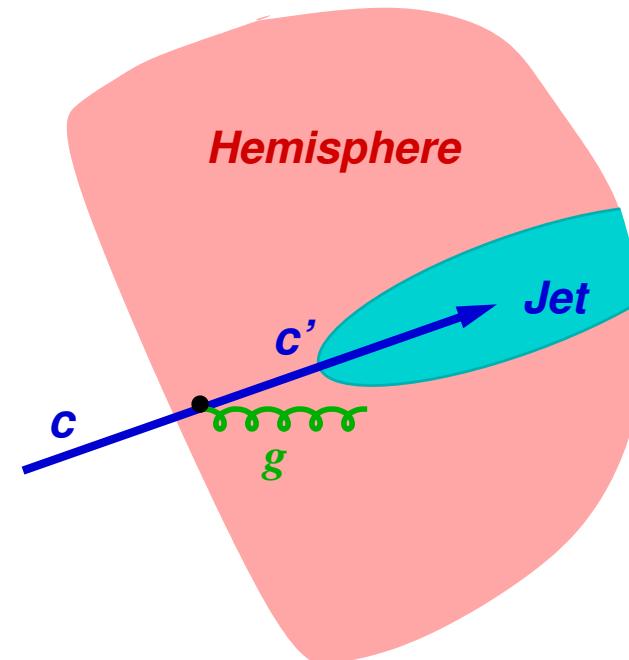


# Aspects of z(jet) & z(hem) Methods

Jet method and hemisphere method differ in case of gluon radiation:

## *Hemisphere method:*

- ▷ includes radiated gluons  
(fragmentation  $c \rightarrow D^*$ )
- ▷ closer to  $e^+e^-$



## *Jet method:*

- ▷ not sensitive to hard gluons from  $c$ -quark  
(fragmentation  $c' \rightarrow D^*$ )
- ▷ maybe closer to non-perturbative fragmentation function

⇒ **Comparison of both methods provides information about underlying physics.**

# *D<sup>\*</sup>* Tagging

**Golden channel:**

$$D^{*\mp} \rightarrow D^0\pi_s^\mp \rightarrow K^\pm\pi^\mp\pi_s^\mp$$

Kinematic cuts:

$$2 < Q^2 < 100 \text{ GeV}^2$$

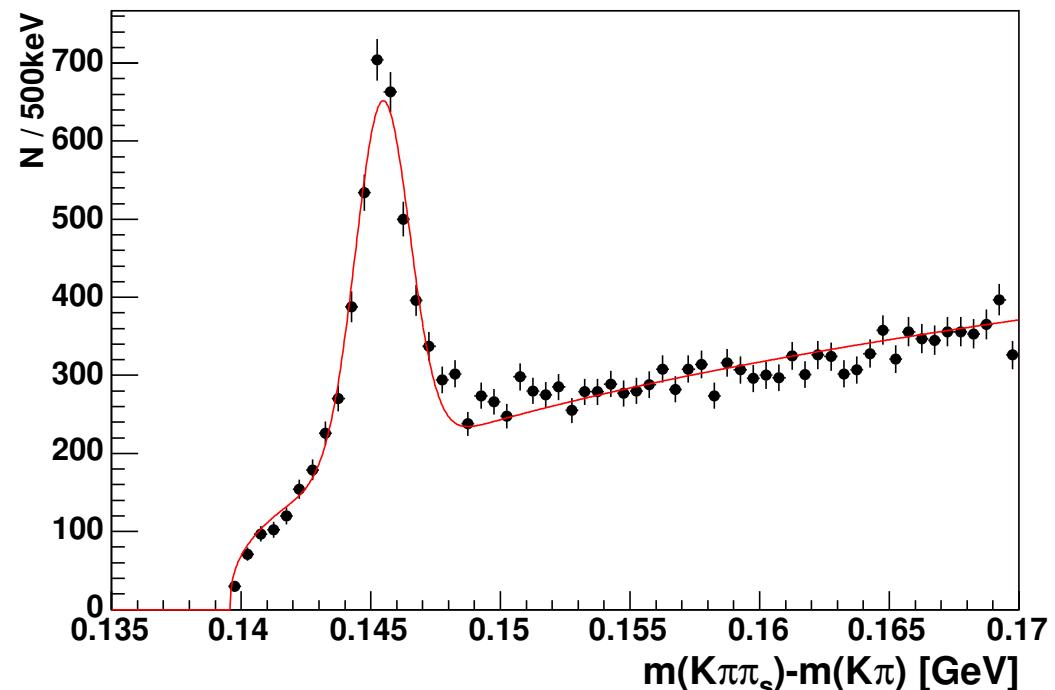
$$0.05 < y_e < 0.7$$

$$p_t(D^*) > 1.5 \text{ GeV}$$

$$|\eta(D^*)| < 1.5$$

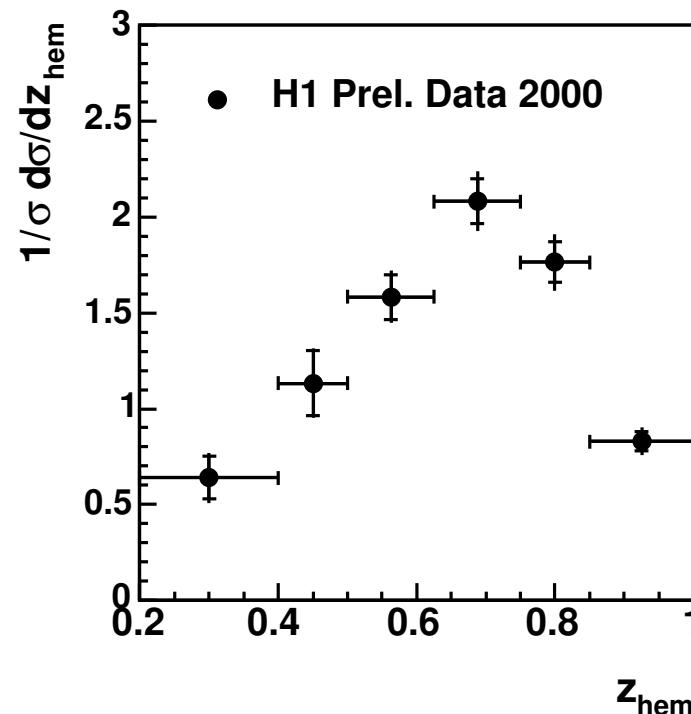
Jet method:

- ▷  $D^*$  treated as stable meson
- ▷ massive  $k_t$ -cluster jet algorithm applied in  $\gamma p$  frame

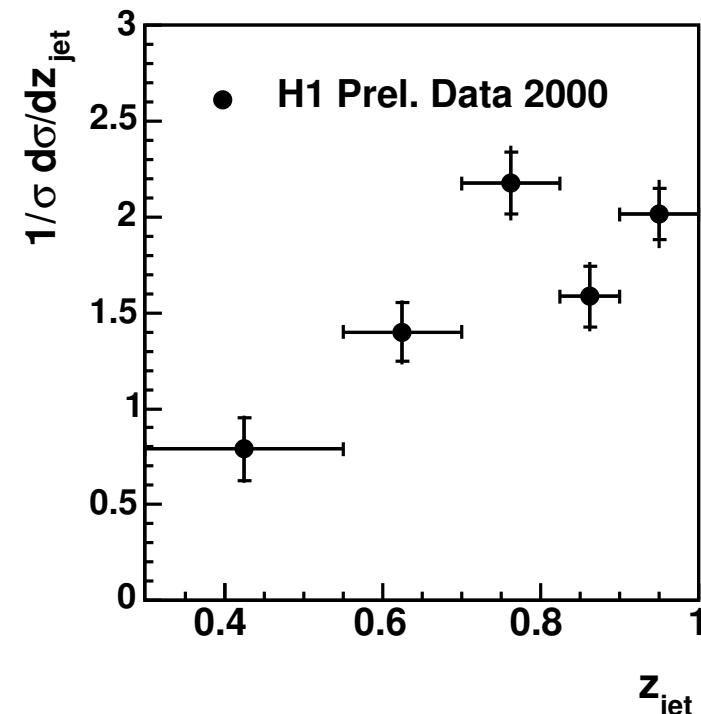


## Corrected Fragmentation Spectra

*Hemisphere method :*



*Jet method :*



Visible Range:

$$\eta_{\text{part}, \gamma p} > 0.$$

$$z > 0.2$$

$$p_t(D^*\text{jet}) > 3 \text{ GeV}$$

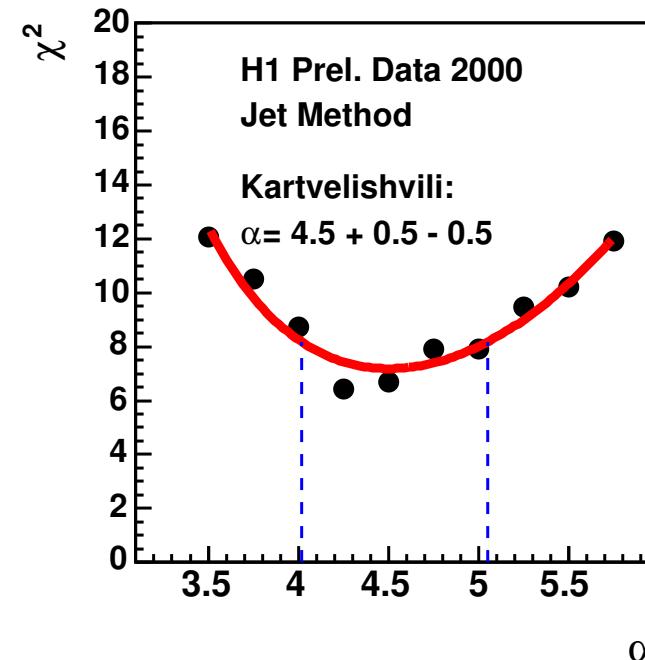
$$z > 0.3$$

# Extraction of Fragmentation Parameter

- ▷ Fragmentation parameters extracted for RAPGAP 3.1 MC (direct +resolved) with excited D-states (ALEPH tune)
- ▷ for fragmentation used:
  - a.) Peterson parametrization
  - b.) Kartvelishvili parametrization

## Extraction procedure:

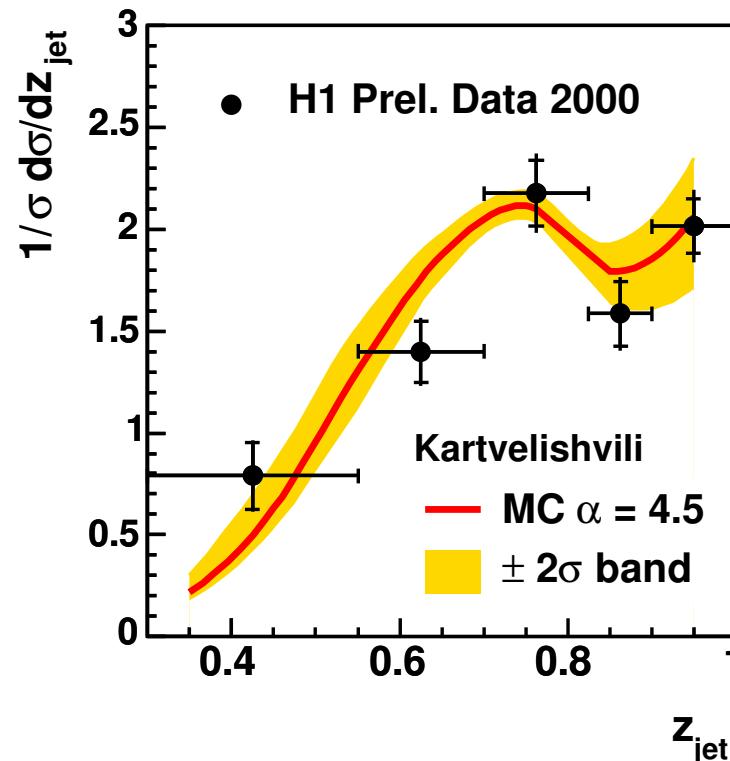
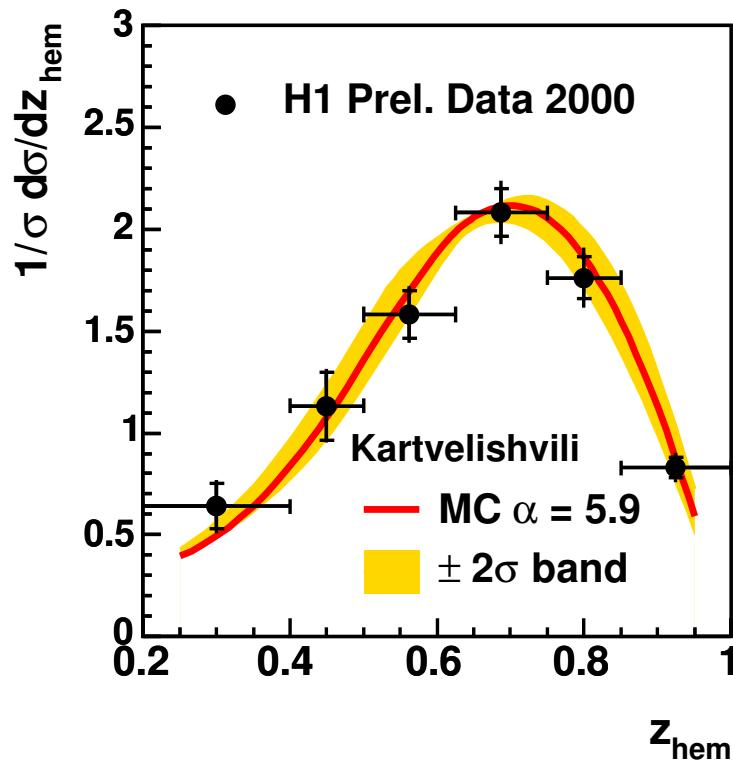
- ▷ MC-files generated for various frag. parameters and from the  $\chi^2$  the most optimal parameter value obtained (correlated systematic errors taken into account )



# Kartvelishvili Fits

*Kartvelishvili :*

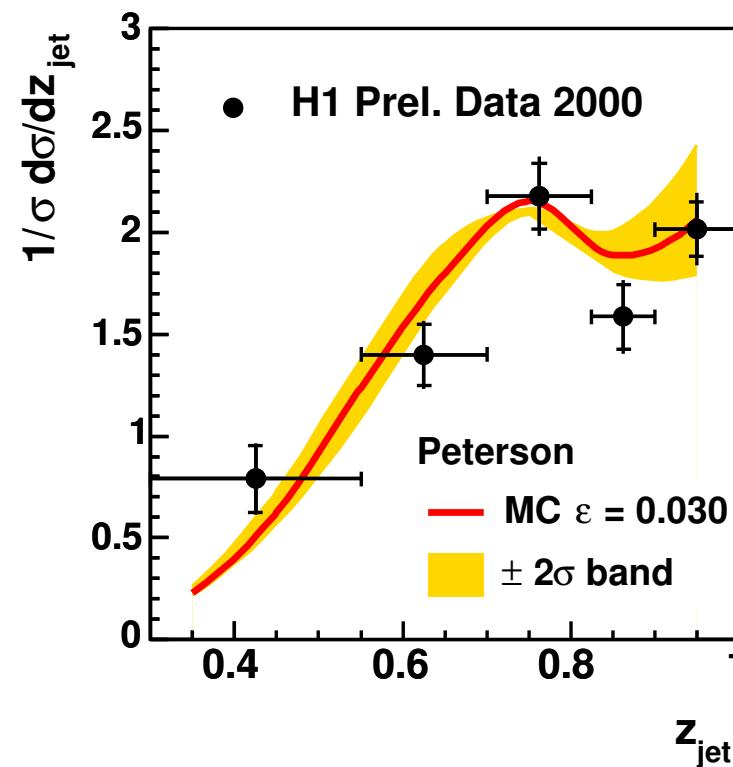
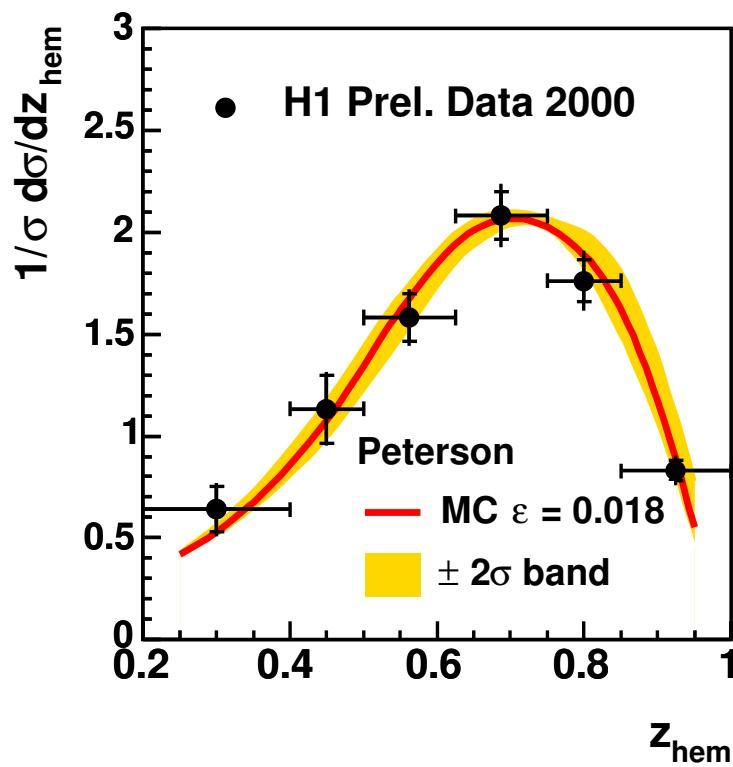
$$f(z) \sim z^{\alpha} (1 - z)$$



## Peterson Fits

*Peterson :*

$$f(z) \sim z^{-1} [1 - \frac{1}{z} - \frac{\varepsilon}{1-z}]^{-2}$$



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## Summary of the Fragmentation Function Results

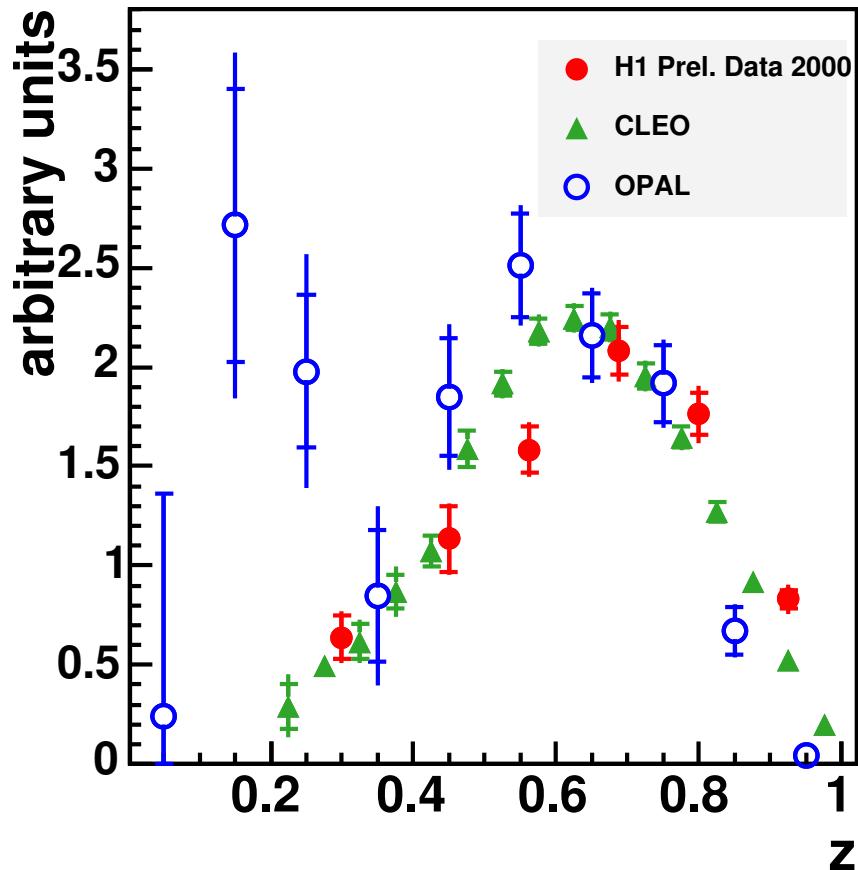
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- ▷ Kartvelishvili and Peterson parametrizations provide equally good descriptions of the data
- ▷ hemisphere method appears to give harder fragmentation function than the jet method
- ▷ difference ( $< 3\sigma$ ) between hemisphere and jet method result may indicate imperfect MC description of hadronic final state in charm events

H1 Prel. Data 2000

parametrization		Hemisphere method	Jet method
Peterson	$\varepsilon$	$0.018^{+0.004}_{-0.004}$	$0.030^{+0.006}_{-0.005}$
Kartvelishvili	$\alpha$	$5.9^{+0.7}_{-0.6}$	$4.5^{+0.5}_{-0.5}$

## Comparison with $e^+e^-$ Experiments



**H1** hemisphere method

$$\langle\sqrt{s}\rangle \approx 10 \text{ GeV}, \\ z = \frac{(E+p_L)_{D^*}}{\sum_{\text{hem}}(E+p)}$$

**CLEO**  $\sqrt{s} \approx 10 \text{ GeV}$ ,

$$z = p_{D^*}/p_{\max}$$

**OPAL**  $\sqrt{s} = 91.2 \text{ GeV}$ ,

$$z = 2E_{D^*}/\sqrt{s}$$

- ▶ although different observable definitions, spectra similar in shape

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## Conclusions

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- ▷ charm fragmentation has been studied
- ▷ extracted fragmentation fractions are in agreement with  $e^+e^-$
- ▷ fragmentation function for  $D^*$  was measured using two different methods (hemisphere and jet)
- ▷ parameters of Peterson and Kartvelishvili functions were extracted for LO+PS MC RAPGAP
- ▷ the observed differences in extracted parameters for the two methods indicate inadequacies in the description of the data by the model
- ▷ uncertainties due to charm fragmentation in other HERA measurements can be reduced (e.g.  $F_2^{c\bar{c}}$ )