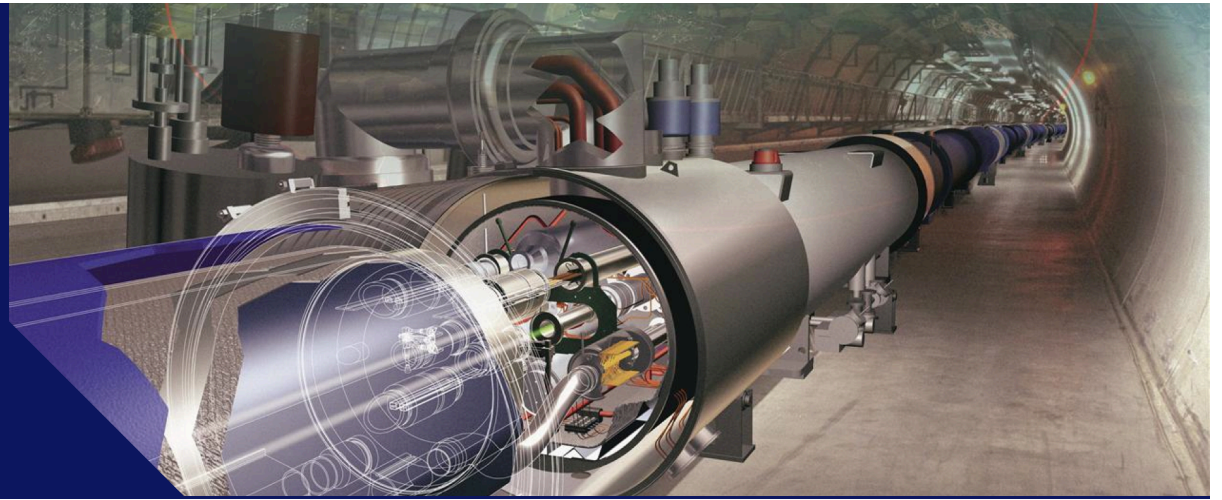


QCD@LHC 2019
Buffalo, New York
15 – 19 July 2019

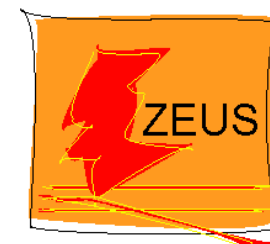


HERAPDF2.0 Jets NNLO

completion of the HERAPDF2.0 family of PDFs
and extraction of $\alpha_s(M_Z)$

Claire Gwenlan, Oxford

on behalf of the
H1, ZEUS, NNLOJet and APPLfast
collaborations



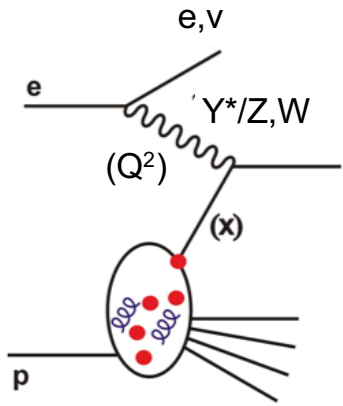
overview

[H1prelim-19-041](#)

[ZEUS-prel-19-001](#)

- **completing the HERAPDF2.0 family of PDFs**
- previously produced (arXiv: [1506.06042](#)): HERAPDF2.0LO, NLO and NNLO;
HERAPDF2.0Jets were only at NLO
- **HERAPDF2.0Jets updated here with NNLO jet predictions from NNLOJet, as implemented in APPLfast** (see also talk in this conference by K.Rabbertz)
- plus addition of new H1 low Q^2 jet data
- **NEW** PDFs at NNLO QCD for $\alpha_s(M_Z)=0.118$ and 0.115
- **PLUS** free $\alpha_s(M_Z)$ fit, with preferred value significantly lower at NNLO than at NLO
- **NNLO:**
$$\alpha_s(M_Z^2) = 0.1150 \pm 0.0008 \text{ (exp)}_{-0.0005}^{+0.0002} \text{ (model/par.)} \pm 0.0006 \text{ (had)} \pm 0.0027 \text{ (scale)}$$
- **NLO result, as published:**
$$\alpha_s(M_Z^2) = 0.1183 \pm 0.0009 \text{ (exp)} \pm 0.0005 \text{ (model/par.)} \pm 0.0012 \text{ (had)}_{-0.0030}^{+0.0037} \text{ (scale)}$$

HERA and DIS



o Kinematic variables:
 $Q^2 = -q^2 = -(k - k')^2$ Virtuality of the exchanged boson
 $x = \frac{Q^2}{2p \cdot q}$ Bjorken scaling parameter
 $y = \frac{p \cdot q}{p \cdot k}$ Inelasticity parameter
 $s = (k + p)^2 = \frac{Q^2}{xy}$ Invariant c.o.m.

Neutral Current:

LO expressions

$$\frac{d^2\sigma_{NC}^{\pm}}{dx dQ^2} = \frac{2\alpha\pi^2}{xQ^4} (Y_+ F_2 \mp Y_- xF_3 - y^2 F_L)$$

$$F_2 \sim \sum_i e_i^2 (xq_i + x\bar{q}_i) \quad xF_3 \sim \sum_i (xq_i - x\bar{q}_i) \quad F_L \sim \alpha_s \times g$$

quarks pdfs valence quarks gluon via $\mathcal{O}(\alpha_s)$

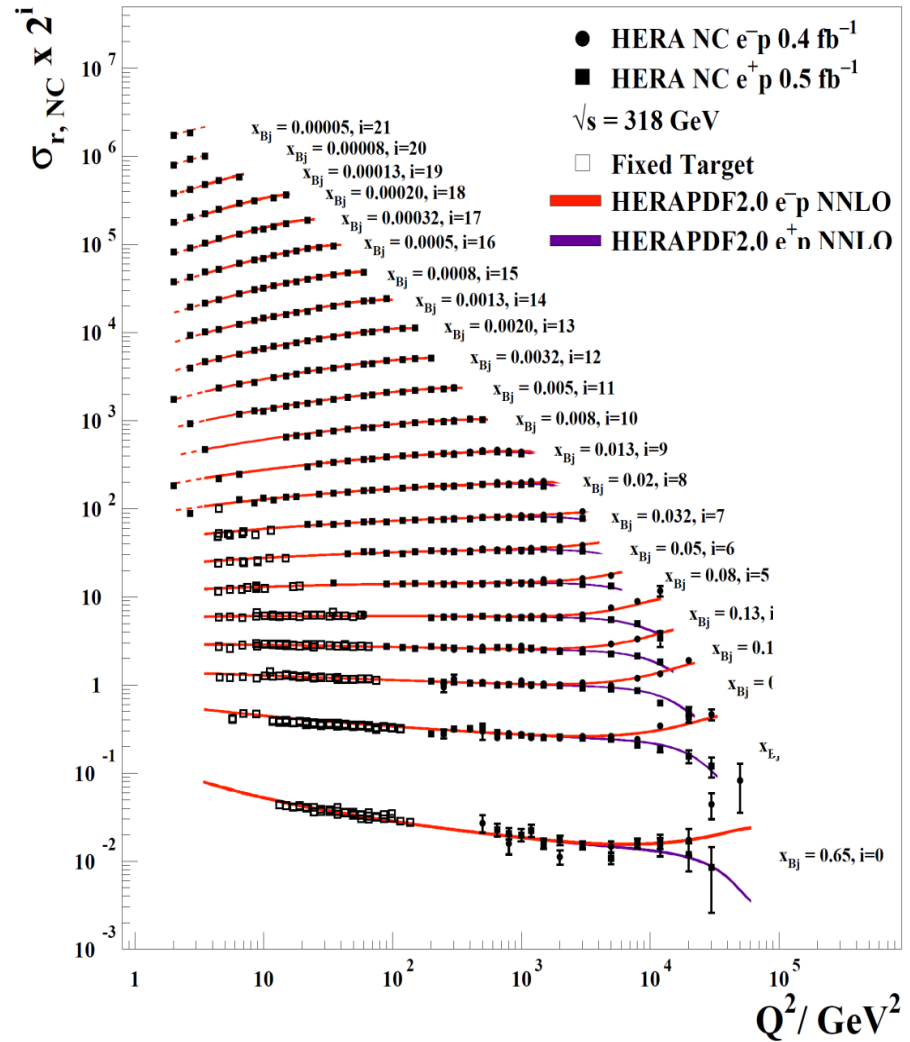
Charged Current:

$$\frac{d^2\sigma_{CC}^-}{dx dQ^2} = \frac{G_F^2}{2\pi} \frac{M_W^2}{M_W^2 + Q^2} (u + c + (1 - y^2)(\bar{d} + \bar{s}))$$

$$\frac{d^2\sigma_{CC}^+}{dx dQ^2} = \frac{G_F^2}{2\pi} \frac{M_W^2}{M_W^2 + Q^2} (\bar{u} + \bar{c} + (1 - y^2)(d + s))$$

flavour decomposition

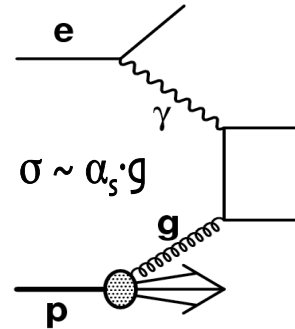
H1 and ZEUS



arXiv: [1506.06042](https://arxiv.org/abs/1506.06042)

why jet data?

simultaneous fit of DIS
inclusive and jet cross
sections **allows**
determination of
 $\alpha_s(M_Z)$



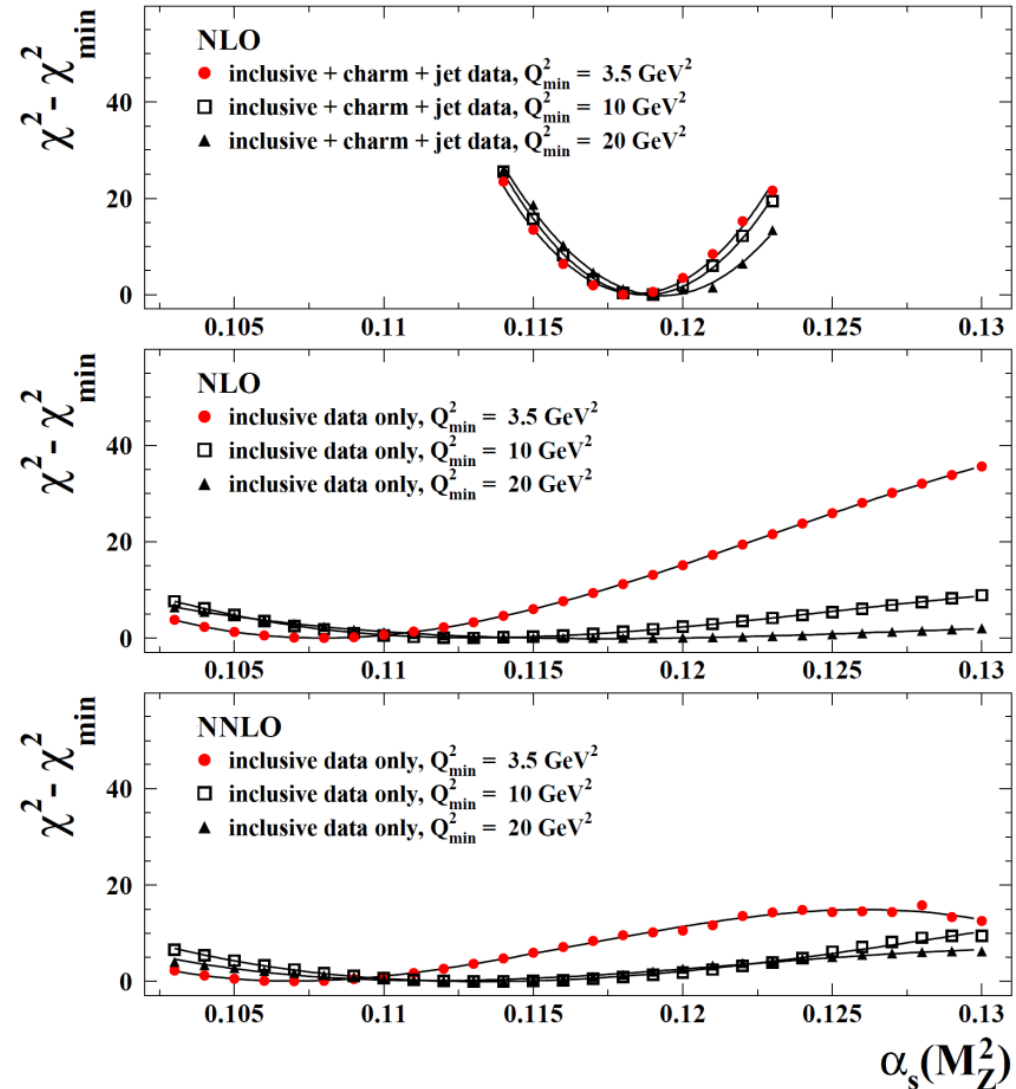
different dependencies on gluon and α_s
gives improved constraints on both

previous result at NLO \rightarrow
arXiv: [1506.06042](https://arxiv.org/abs/1506.06042)

NOW:

NNLO QCD calculations for DIS
jets available in **NNLOJet**
(arXiv: [1606.03991](https://arxiv.org/abs/1606.03991), [1703.05977](https://arxiv.org/abs/1703.05977)), and
implemented in **APPLfast**
(arXiv: [1906.05303](https://arxiv.org/abs/1906.05303))

H1 and ZEUS



jet data used in the current NNLO analysis

strong overlap with those used in previous NLO QCD analysis

| Data Set | taken | | $Q^2[\text{GeV}^2]$ range | | \mathcal{L} pb ⁻¹ | e^+/e^- | \sqrt{s} GeV | norma- lised | all points | used points |
|--|-------------|-----------|---------------------------|-------|-----------------------------------|-------------|-------------------|-----------------|---------------|----------------|
| | from | to | from | to | | | | | | |
| H1 HERA I normalised jets | 1999 | 2000 | 150 | 15000 | 65.4 | e^+p | 319 | yes | 24 | 24 |
| H1 HERA I jets at low Q^2 | 1999 | 2000 | 5 | 100 | 43.5 | e^+p | 319 | no | 28 | 16 |
| H1 normalised inclusive jets at high Q^2 | 2003 | 2007 | 150 | 15000 | 351 | e^+p/e^-p | 319 | yes | 30 | 24 |
| H1 normalised dijets at high Q^2 | 2003 | 2007 | 150 | 15000 | 351 | e^+p/e^-p | 319 | yes | 24 | 24 |
| H1 normalised inclusive jets at low Q^2 | 2005 | 2007 | 5.5 | 80 | 290 | e^+p/e^-p | 319 | yes | 48 | 32 |
| H1 normalised dijets at low Q^2 | 2005 | 2007 | 5.5 | 80 | 290 | e^+p/e^-p | 319 | yes | 48 | 32 |
| ZEUS inclusive jets | 1996 | 1997 | 125 | 10000 | 38.6 | e^+p | 301 | no | 30 | 30 |
| ZEUS dijets | 1998–2000 & | 2004–2007 | 125 | 20000 | 374 | e^+p/e^-p | 318 | no | 22 | 16 |

low Q^2 H1 datasets added (published 2016) that were not used in the previous NLO analysis

some other data sets removed cf. NLO analysis:

- trijet data, since no NNLO QCD calculations;
- 6 dijet data points at low pt, since predictions unreliable;
- low scale data $\mu = \sqrt{(Q^2 + pt^2)} < 13.5$ GeV, for which scale variations large

all systematic and statistical correlations implemented

scale choice for jet data

factorisation scale choice is $\mu_F^2=(Q^2+pt^2)$

cf. $\mu_F^2=Q^2$ in previous NLO analysis; updated since not a good choice for low Q^2 jet data; change makes almost no difference for high Q^2 jet data

renormalisation scale choice is $\mu_R^2=(Q^2+pt^2)$

cf. $\mu_R^2=(Q^2+pt^2)/2$ in previous NLO analysis

NB, optimal scale choice – where ‘optimal’ here means lower X^2 – is different for NLO vs NNLO;

NNLO fit with $\mu_R^2=(Q^2+pt^2)$ gives $\Delta X^2= -15$ cf. $\mu_R^2=(Q^2+pt^2)/2$ and vice versa for NLO fit

consequences of scale changes also explored

† pt denotes pt^{jet} in the case of inclusive jet cross sections and $\langle pt \rangle$ for dijets

HERA PDF approach

- **HERAPDF uses only HERA data**
- combination of HERA data yields very precise and consistent dataset for 4 different processes: **e+p** and **e-p neutral** and **charged current** reactions; also, for e+p, neutral current at 4 beam energies
- single consistent dataset; conventional χ^2 tolerance, $\Delta\chi^2 = 1$
- use of proton target means no need for heavy target/deuterium corrections
- d-valence extracted from CC e+p without assuming d in proton = u in neutron
- all data at $W > 15$ GeV, so high-x higher twist effects negligible
- **HERAPDF** evaluates model and parameterisation uncertainties in addition to experimental uncertainties
- **HERAPDF2.0** based on **FINAL combination of HERA I and HERA II data**, which supercedes the HERA I combination and all previous HERAPDFs
- **HERAPDF2.0Jets** add HERA jet data to this

HERAPDF parameterisation

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g},$$

$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2),$$

$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x),$$

$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.$$

QCD sum rules constrain
 A_g, A_{uv}, A_{dv}

$x\bar{s} = f_s x\bar{D}$ sets size of
strange PDF

constraints $B_U = B_D$ and
 $A_{\bar{U}} = A_{\bar{D}}(1 - f_s)$ ensure
 $x\bar{u} \rightarrow x\bar{d}$ as $x \rightarrow 0$

- **14 free parameters in central fit**, established by saturation of \mathbf{X}^2
- extra D, E parameters added to all PDF flavours for parameterisation uncertainties, $A_{g'}=0$ also checked
- QCDNUM used for QCD DGLAP evolution, within xFitter framework, and cross checked with independent code
- Thorne-Roberts Optimised Variable Flavour Number Scheme (RT-VFN)
- jet predictions from NNLOJet (arXiv:[1606.03991](https://arxiv.org/abs/1606.03991), [1703.05977](https://arxiv.org/abs/1703.05977)) interfaced to APPLfast (arXiv:[1906.05303](https://arxiv.org/abs/1906.05303))
- **$\alpha_s(M_Z)=0.118, 0.115$; plus free α_s fit**

HERAPDF sources of uncertainty

experimental:

Hessian uncertainties: 14 eigenvector pairs evaluated with $\Delta\chi^2=1$; cross checked uncertainties using rms of MC replicas

model:

variation of input assumptions; and c,b masses

$$f_s = 0.4 \pm 0.1$$

$$M_c = 1.47 \pm 0.06 \text{ GeV}$$

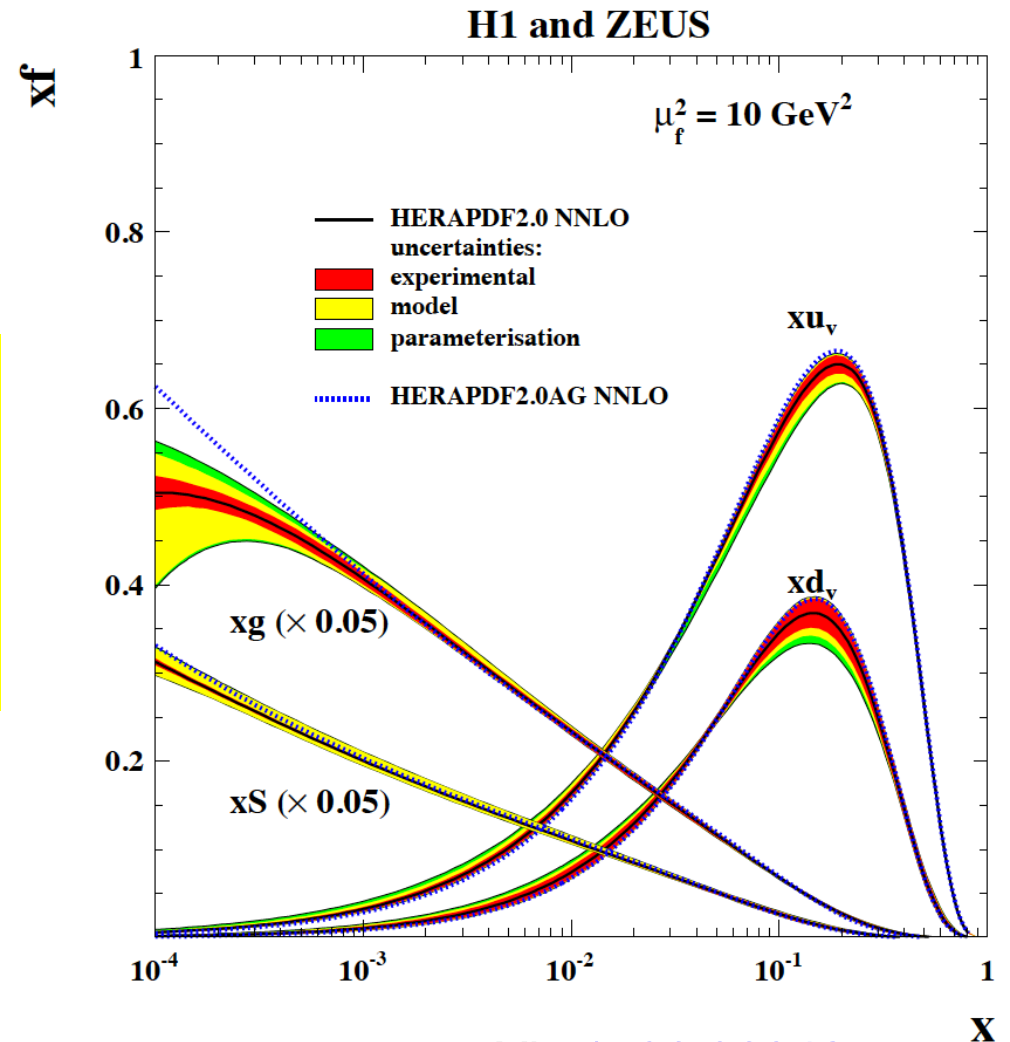
$$M_b = 4.5 \pm 0.25 \text{ GeV}$$

$$Q^2_{\text{min}} = 3.5_{-1}^{+1.5} \text{ GeV}^2$$

parameterisation:

variation of $Q^2_0 = 1.9 \pm 0.3 \text{ GeV}^2$, plus addition of 15th parameter(s)

(variations as for HERAPDF2.0 analysis)

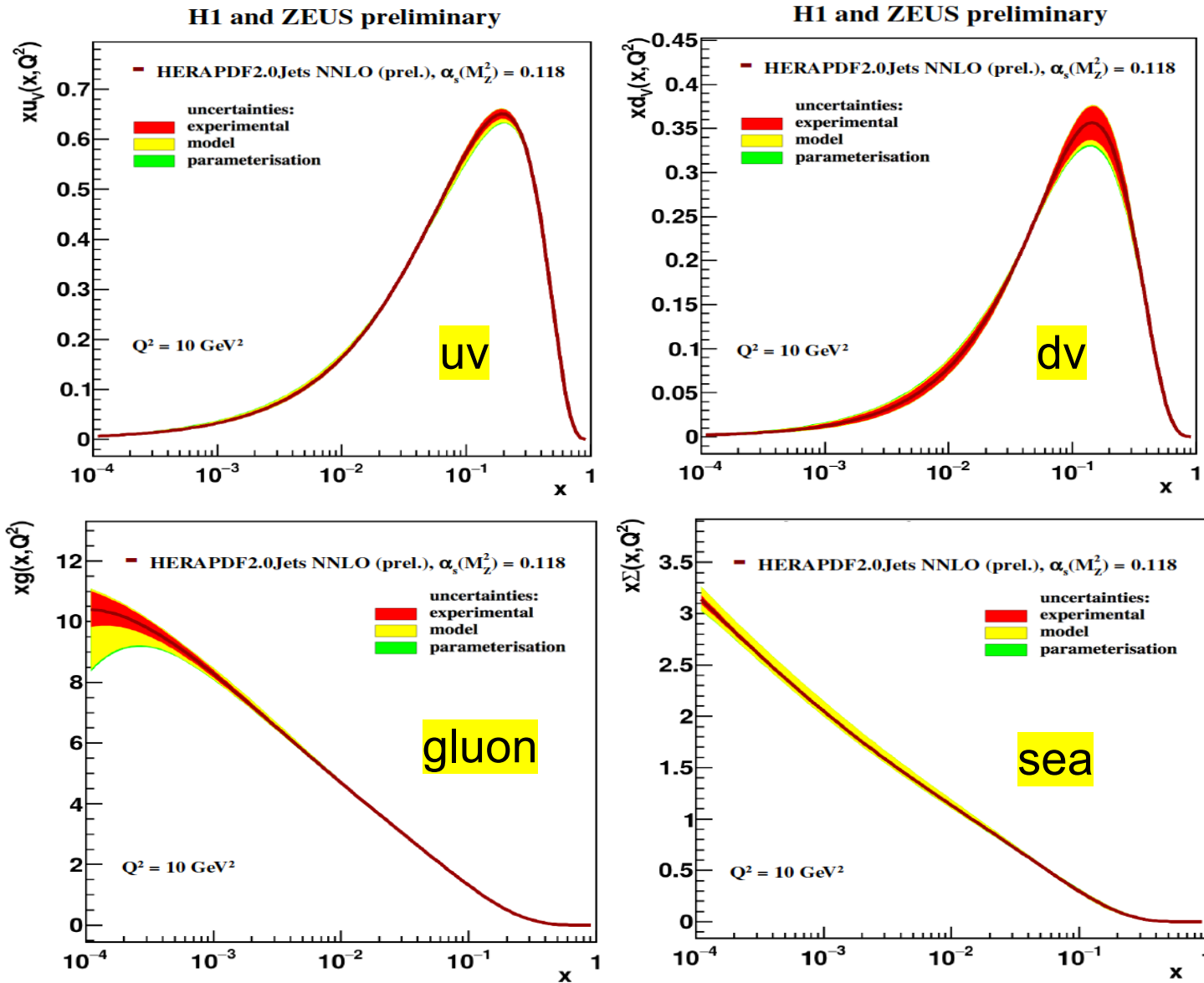


NB, for **jet cross sections**, hadronisation uncertainties also included

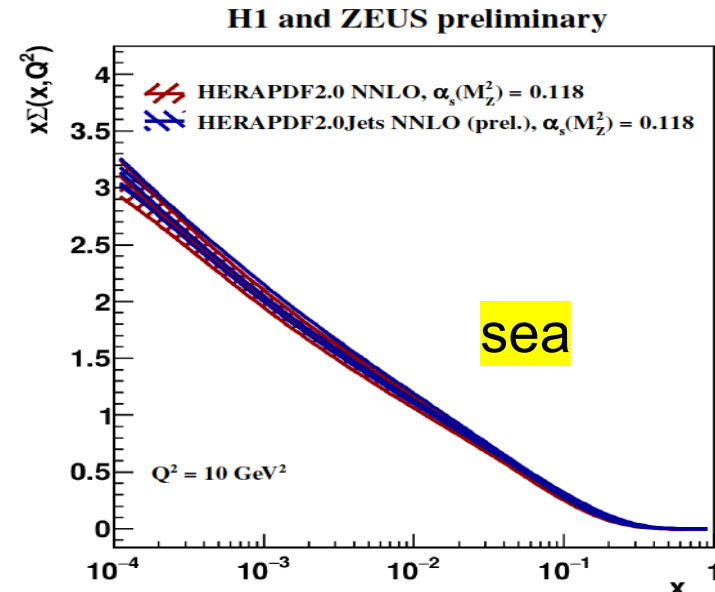
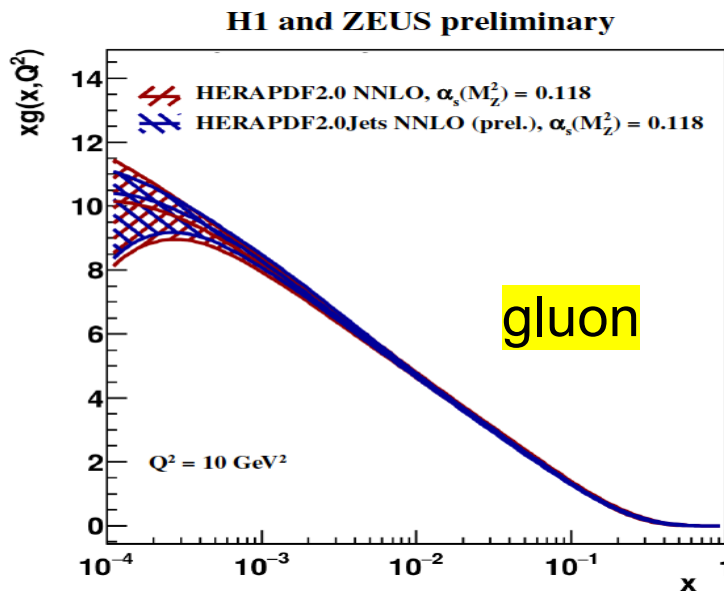
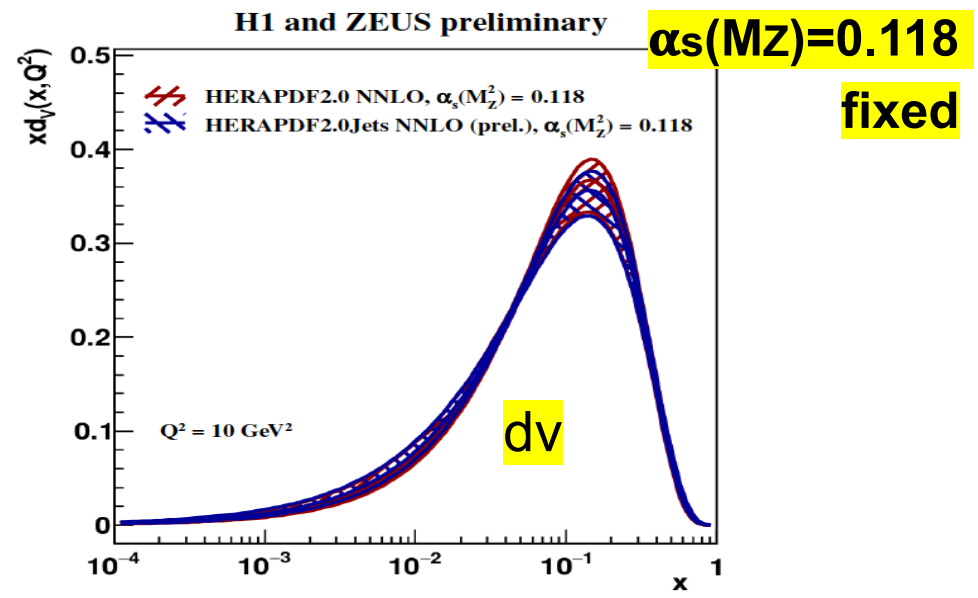
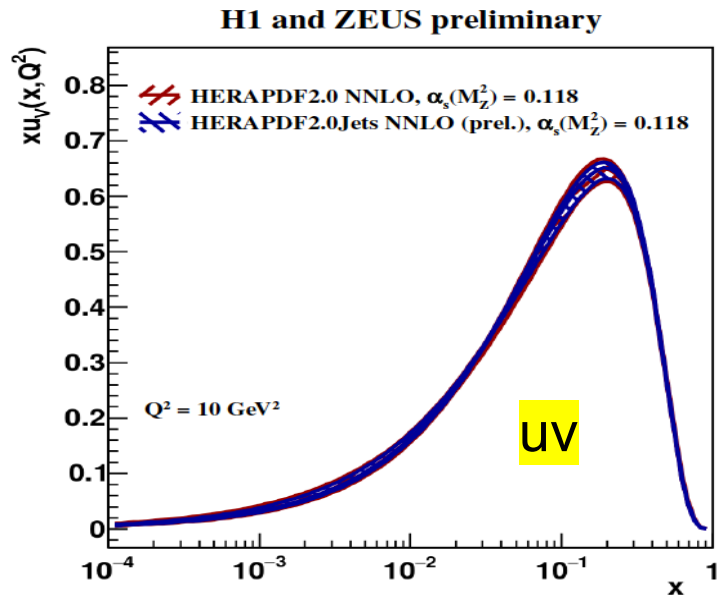
HERAPDF2.0Jets NNLO

$\alpha_s(M_Z)=0.118$

fixed

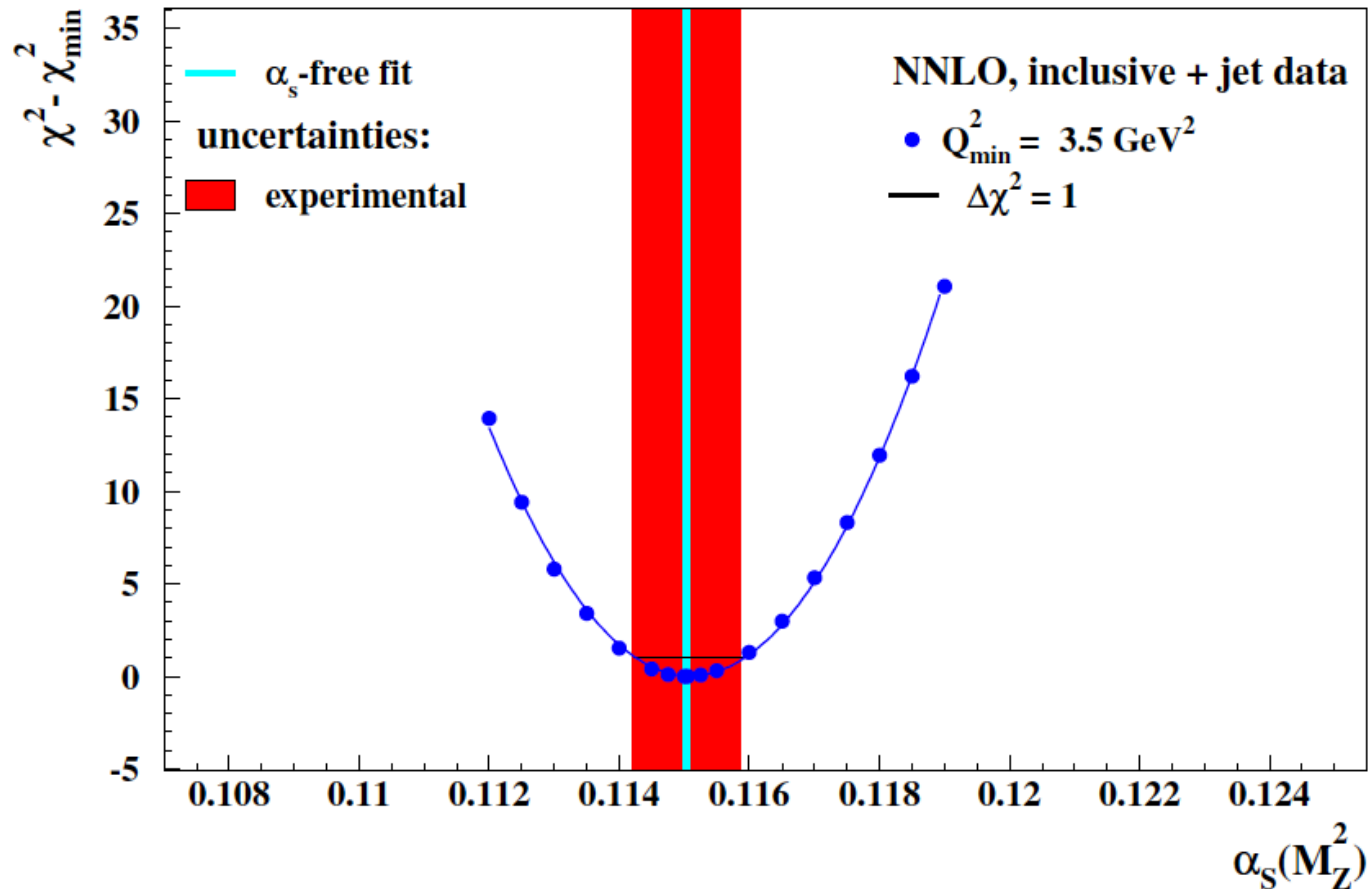


HERAPDF2.0 vs HERAPDF2.0Jets NNLO



HERAPDF2.0Jets NNLO α_s fits

H1 and ZEUS preliminary



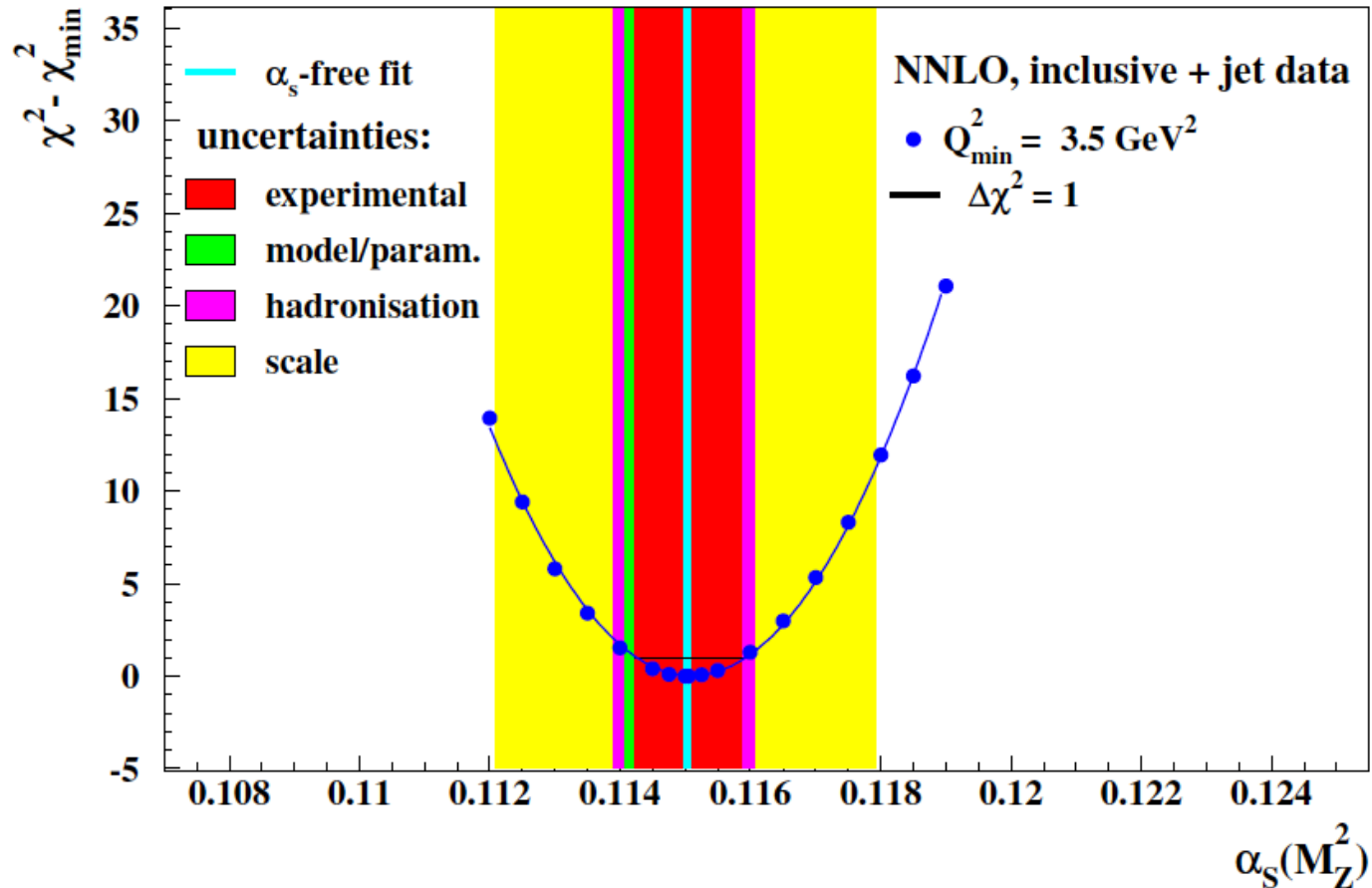
standard HERAPDF value is $\alpha_s(M_Z)=0.118$ (shown on previous slides)

fits also performed with **free $\alpha_s(M_Z)$** , compared here to **χ^2 scan over fixed $\alpha_s(M_Z)$**

perfect agreement in minimum and uncertainty

HERAPDF2.0 Jets NNLO α_s fits

H1 and ZEUS preliminary



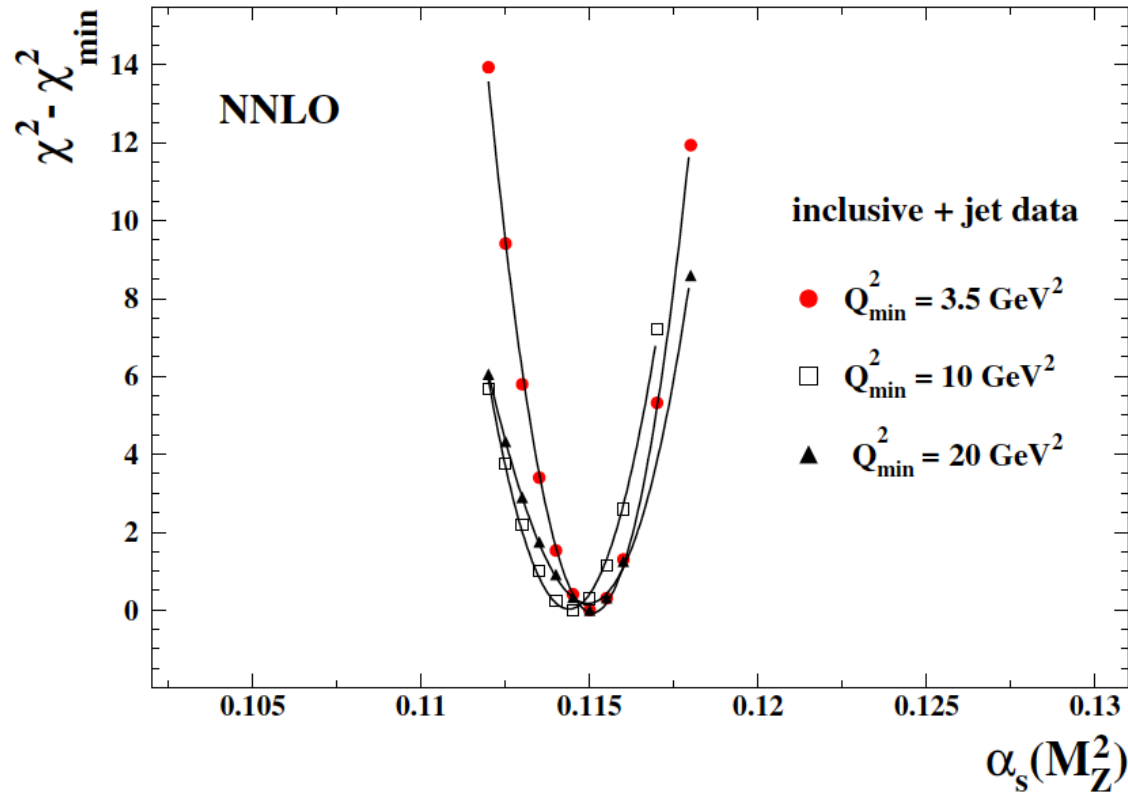
and with full uncertainties:

$$\alpha_s(M_Z^2) = 0.1150 \pm 0.0008 (\text{exp})_{-0.0005}^{+0.0002} (\text{model/par.}) \pm 0.0006 (\text{had}) \pm 0.0027 (\text{scale})$$

[NB, scale uncertainty dominates; 7-point variation considered, with μ_R , μ_F varied by factor of 2]

sensitivity to minimum Q^2 cut

H1 and ZEUS preliminary



central values from the 3 scans:

$$\alpha_s(M_Z^2) = 0.1150 \pm 0.0008 \text{ (exp)} \quad Q^2 > 3.5 \text{ GeV}^2$$

$$\alpha_s(M_Z^2) = 0.1144 \pm 0.0010 \text{ (exp)} \quad Q^2 > 10 \text{ GeV}^2$$

$$\alpha_s(M_Z^2) = 0.1148 \pm 0.0010 \text{ (exp)} \quad Q^2 > 20 \text{ GeV}^2$$

EG, arXiv:[1506.06042](https://arxiv.org/abs/1506.06042), [1710.05935](https://arxiv.org/abs/1710.05935)

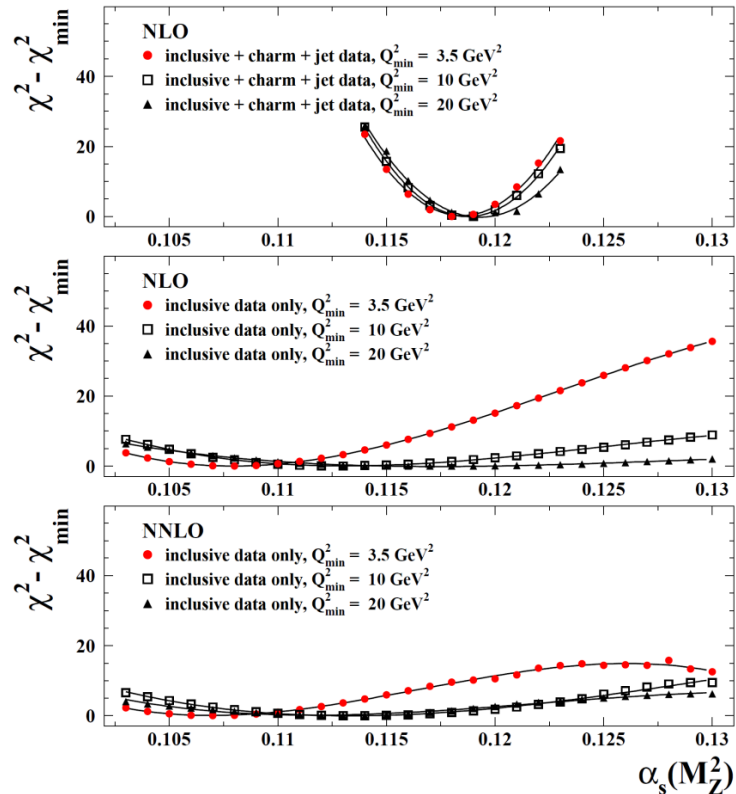
HERA data at low x , Q^2 may be subject to need for $\ln(1/x)$ resummation or higher twist effects;
 χ^2 scans also performed with harder minimum Q^2 cuts

no significant change to extracted value of $\alpha_s(M_Z)$

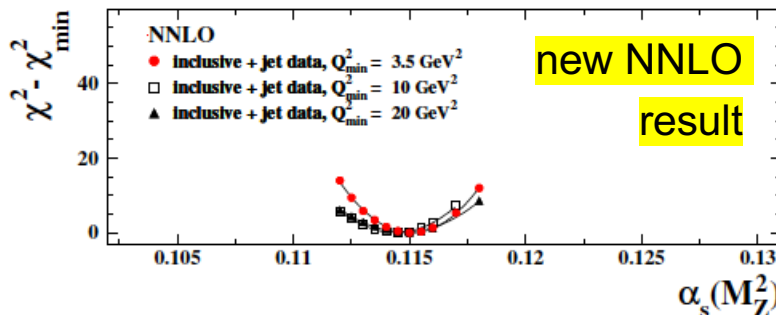
comparison to previous NLO result

arXiv: [1506.06042](https://arxiv.org/abs/1506.06042)

H1 and ZEUS



H1 and ZEUS preliminary



NNLO scans using inclusive and jet data are compared to previously published scans at NLO, plus corresponding scans using only inclusive data

similar level of precision at NNLO and NLO

smaller value of $\alpha_s(M_Z)$ preferred at NNLO

NB, conclusion holds independent of updated scale choices; with old scales, NNLO result would be even lower at 0.1135

NNLO:

$$\alpha_s(M_Z^2) = 0.1150 \pm 0.0008 \text{ (exp)}_{-0.0005}^{+0.0002} \text{ (model/par.)} : \\ \pm 0.0006 \text{ (had)} \pm 0.0027 \text{ (scale)}$$

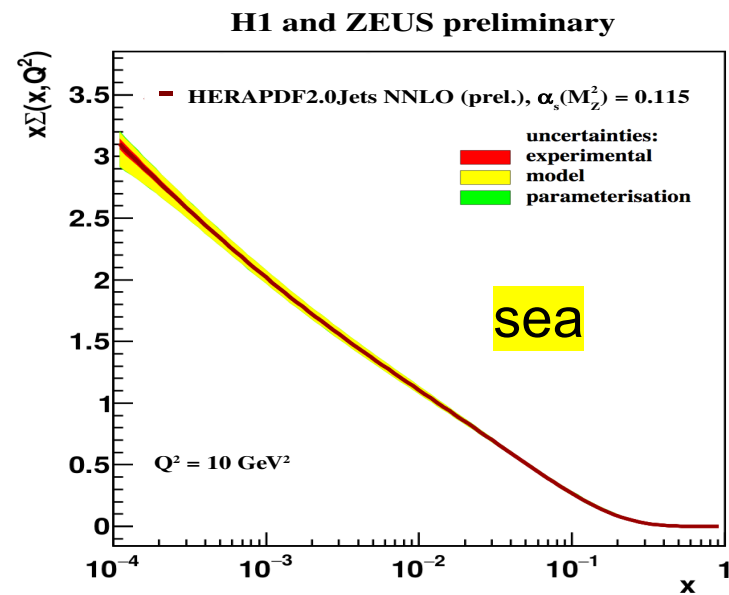
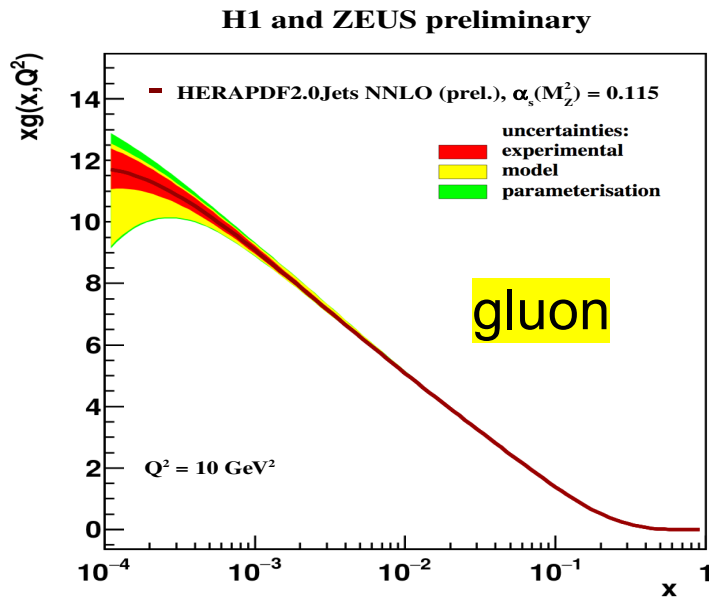
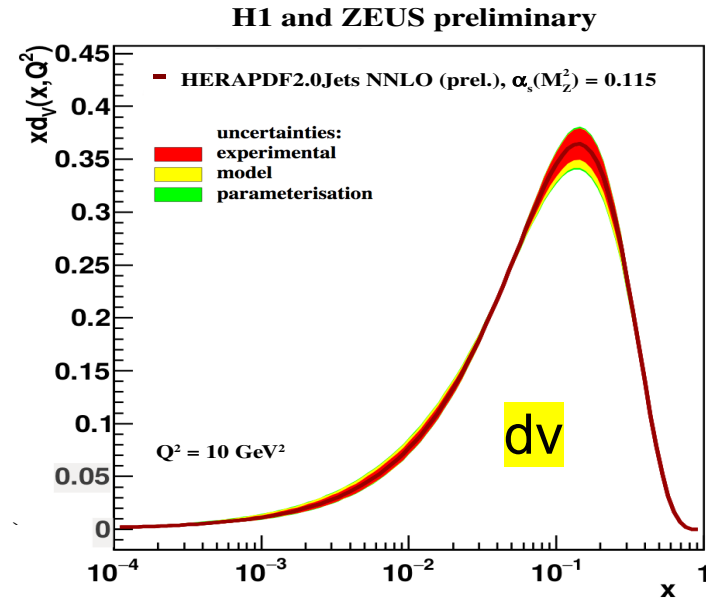
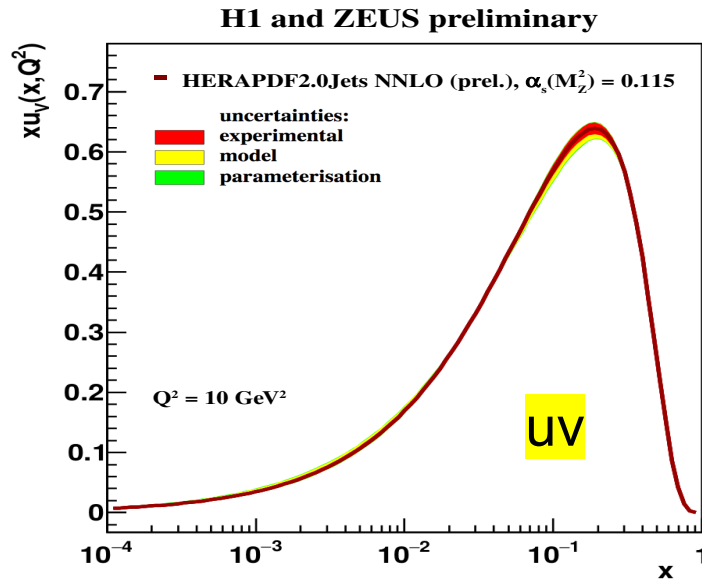
cf. **NLO:** arXiv: [1506.06042](https://arxiv.org/abs/1506.06042)

$$\alpha_s(M_Z^2) = 0.1183 \pm 0.0009 \text{ (exp)} \pm 0.0005 \text{ (model/par.)} \\ \pm 0.0012 \text{ (had)}_{-0.0030}^{+0.0037} \text{ (scale)}$$

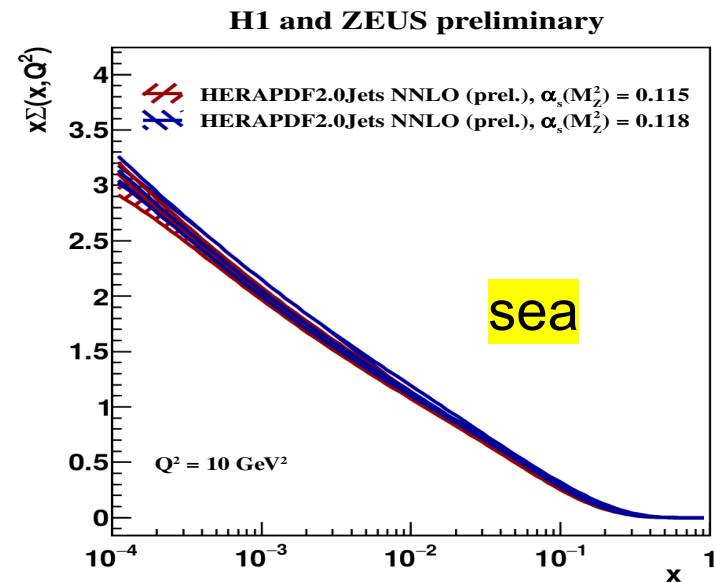
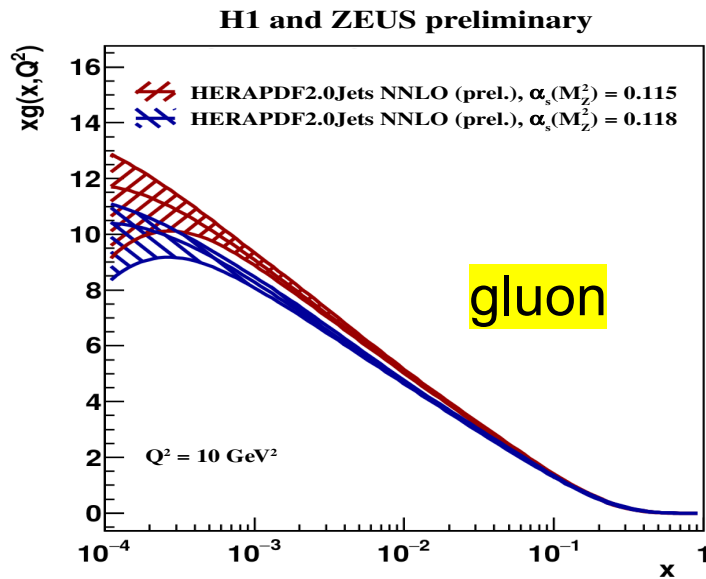
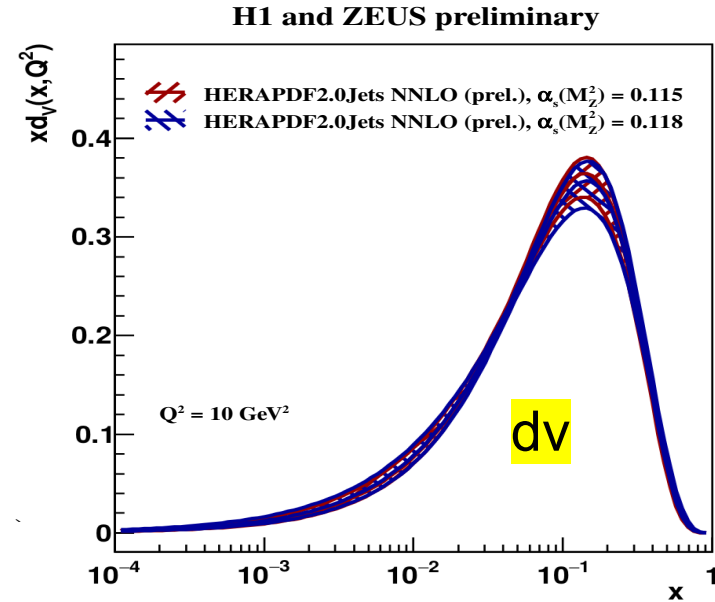
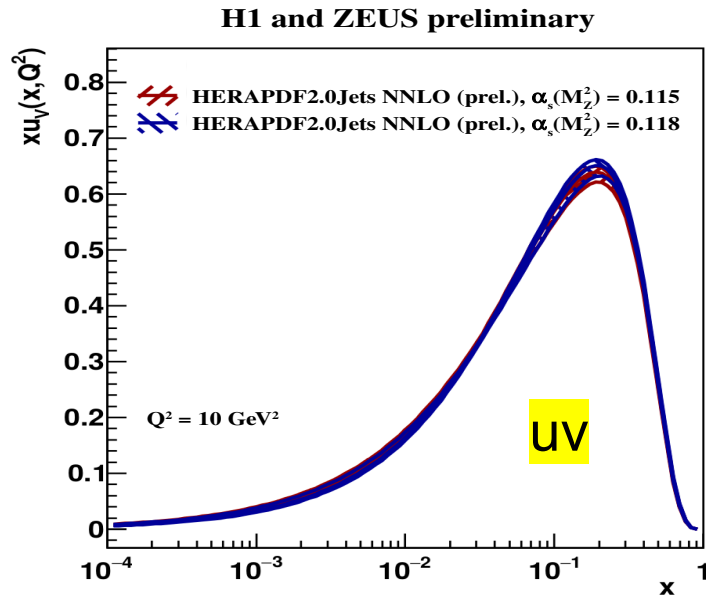
HERAPDF2.0Jets NNLO

$\alpha_s(M_Z)=0.115$

fixed

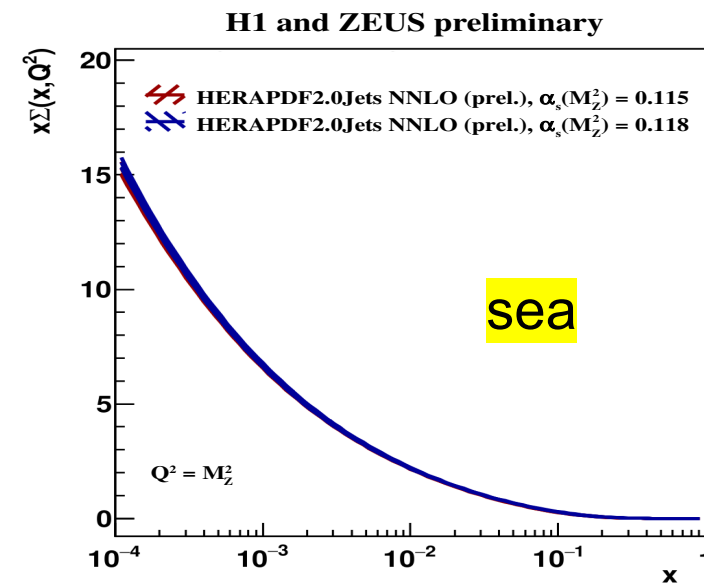
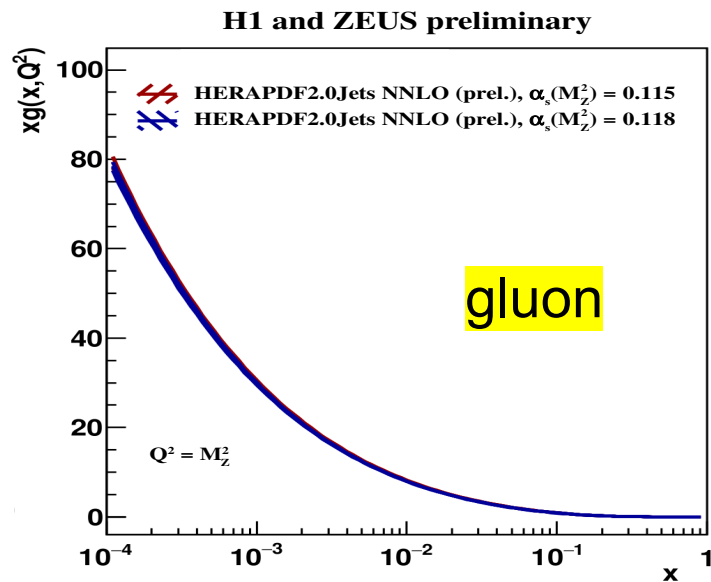
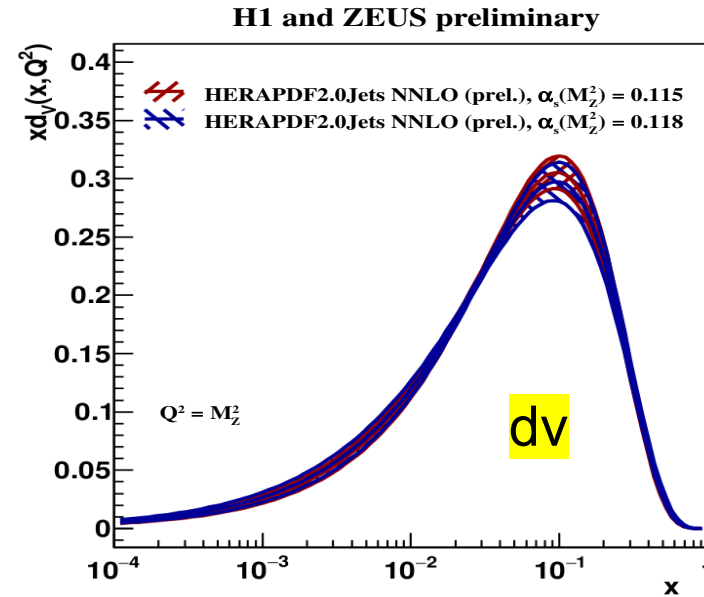
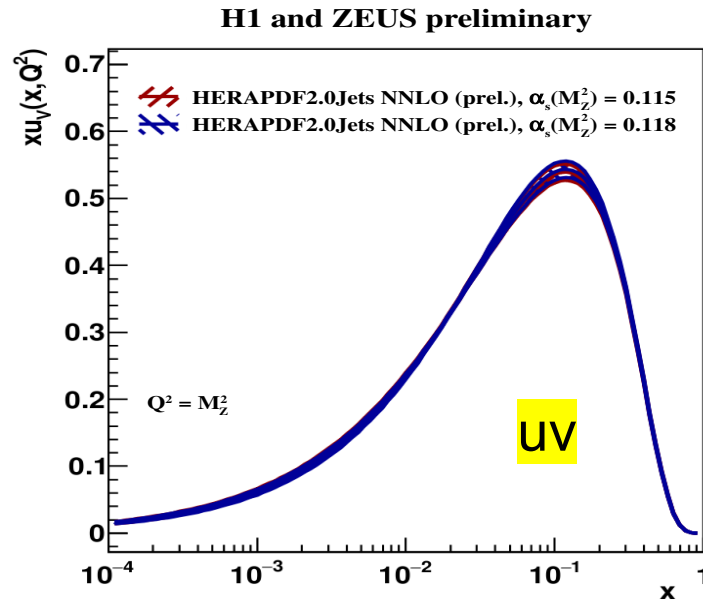


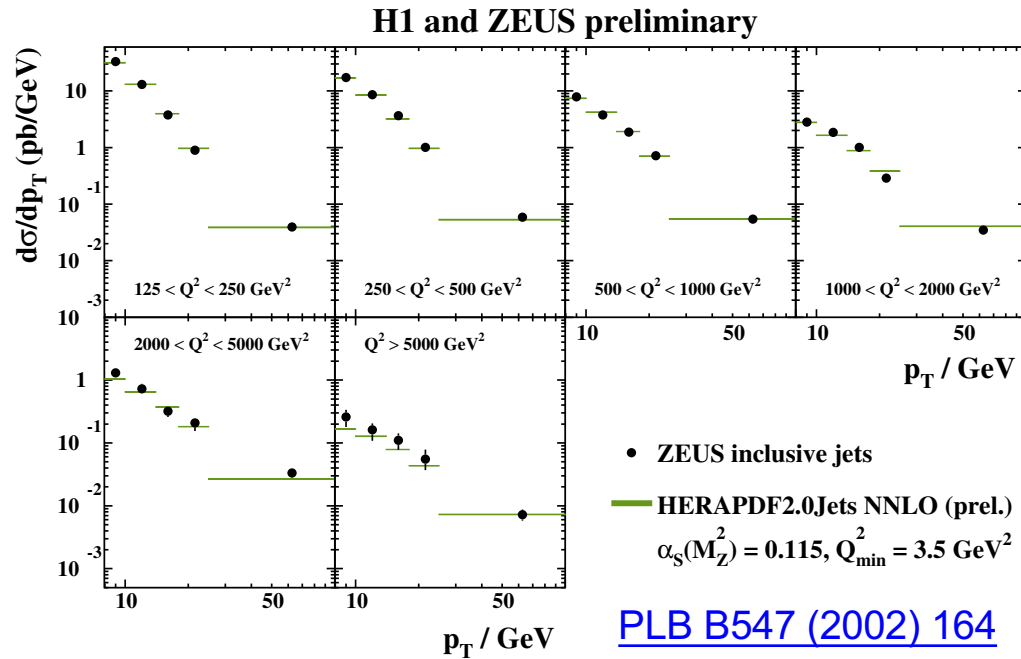
comparison of $\alpha_s(M_Z)=0.115$ and 0.118



comparison of $\alpha_s(M_Z)=0.115$ and 0.118

at higher
scale
 $Q^2=M_Z^2$

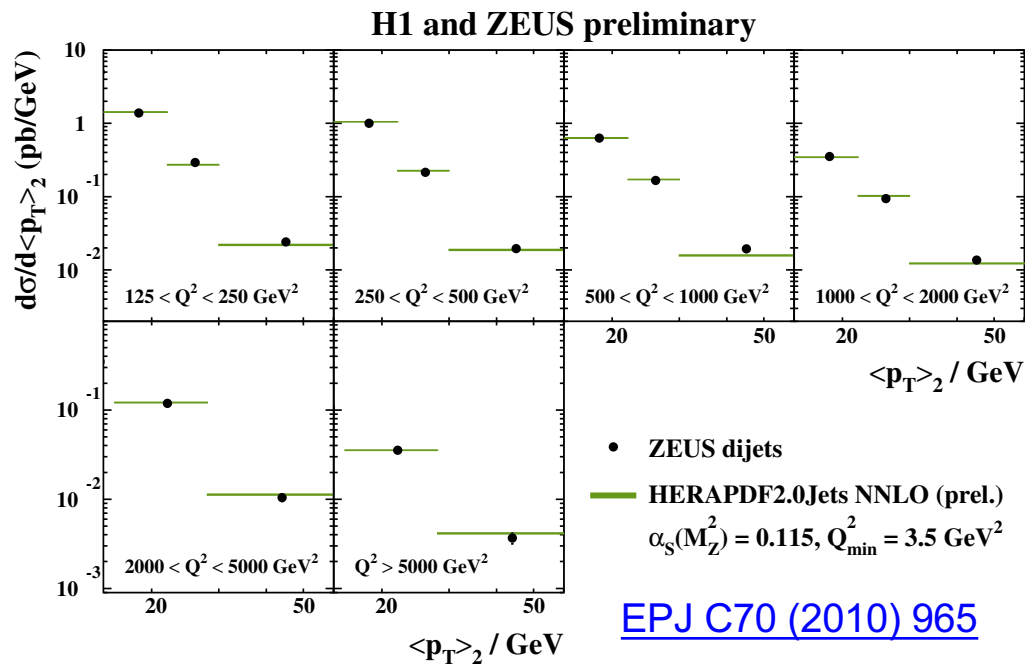




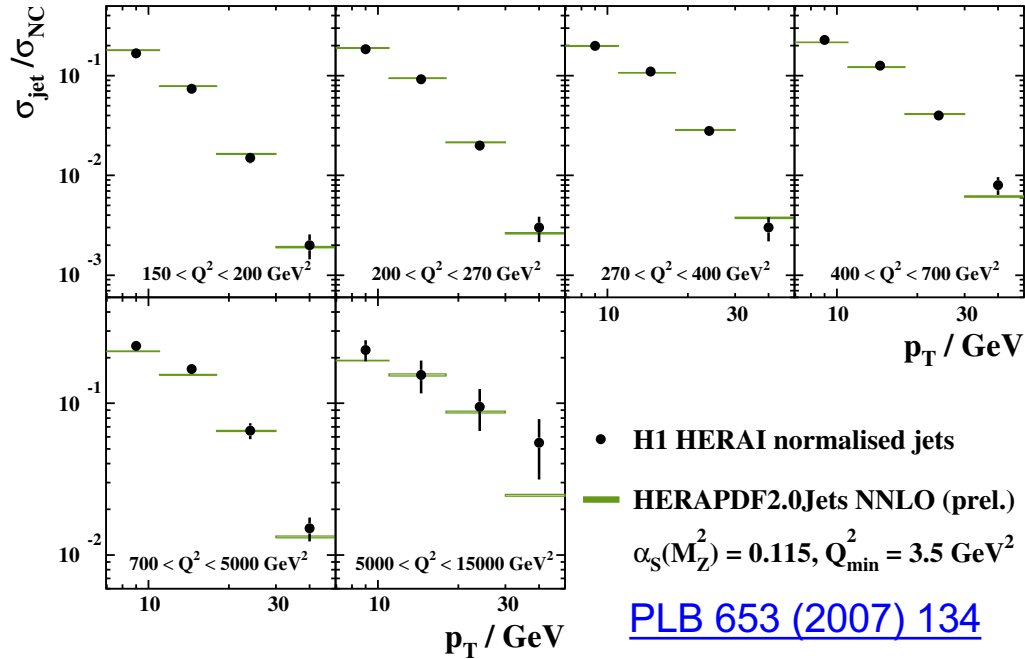
cf. HERA jet data

HERAPDF2.0JetsNLO

$\alpha_s(M_Z) = 0.115$



H1 and ZEUS preliminary

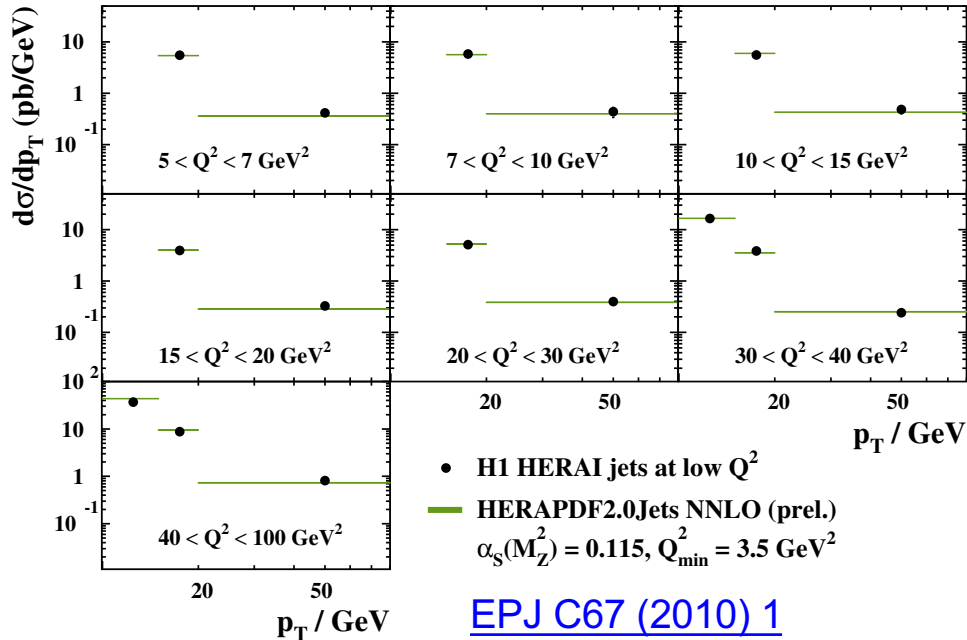


cf. HERA jet data

HERAPDF2.0JetsNLO

$\alpha_s(M_Z) = 0.115$

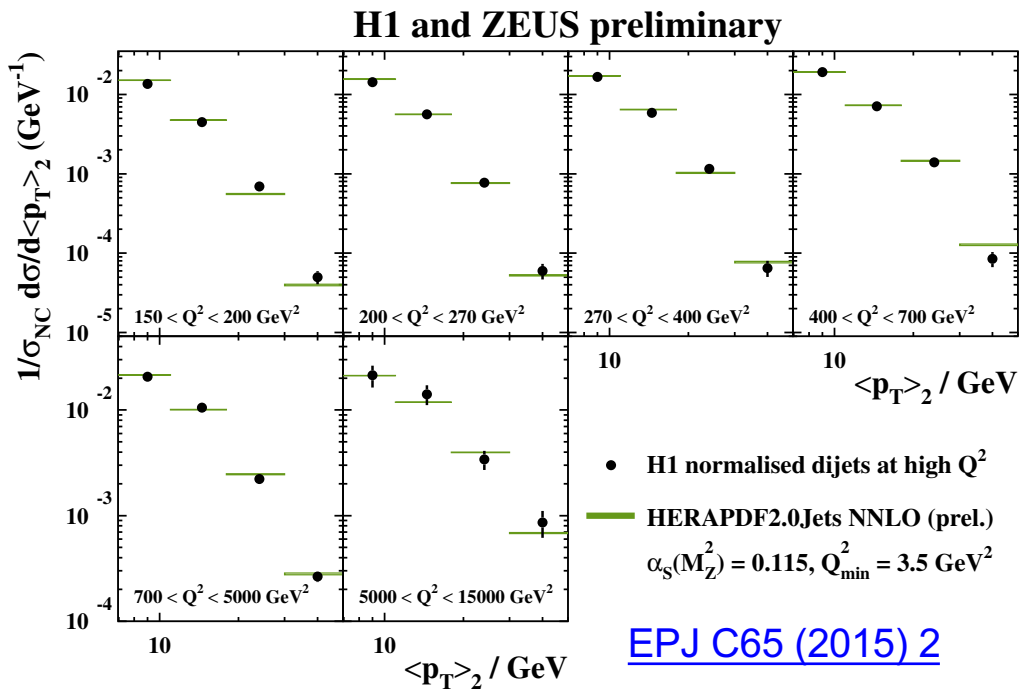
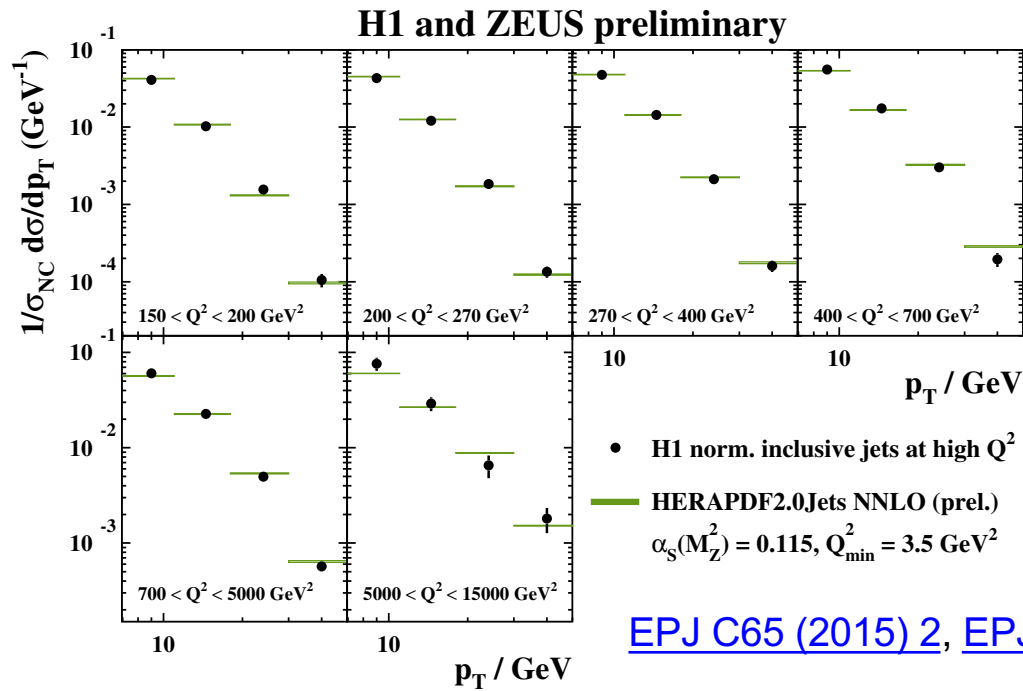
H1 and ZEUS preliminary



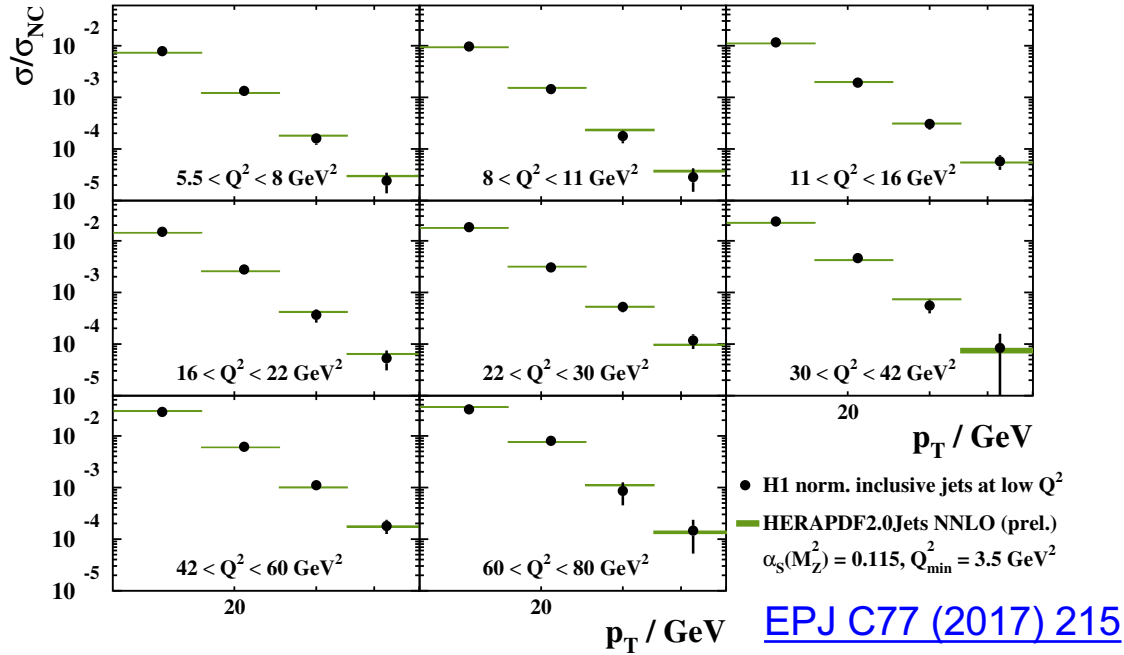
cf. HERA jet data

HERAPDF2.0JetsNLO

$\alpha_s(M_Z) = 0.115$



H1 and ZEUS preliminary

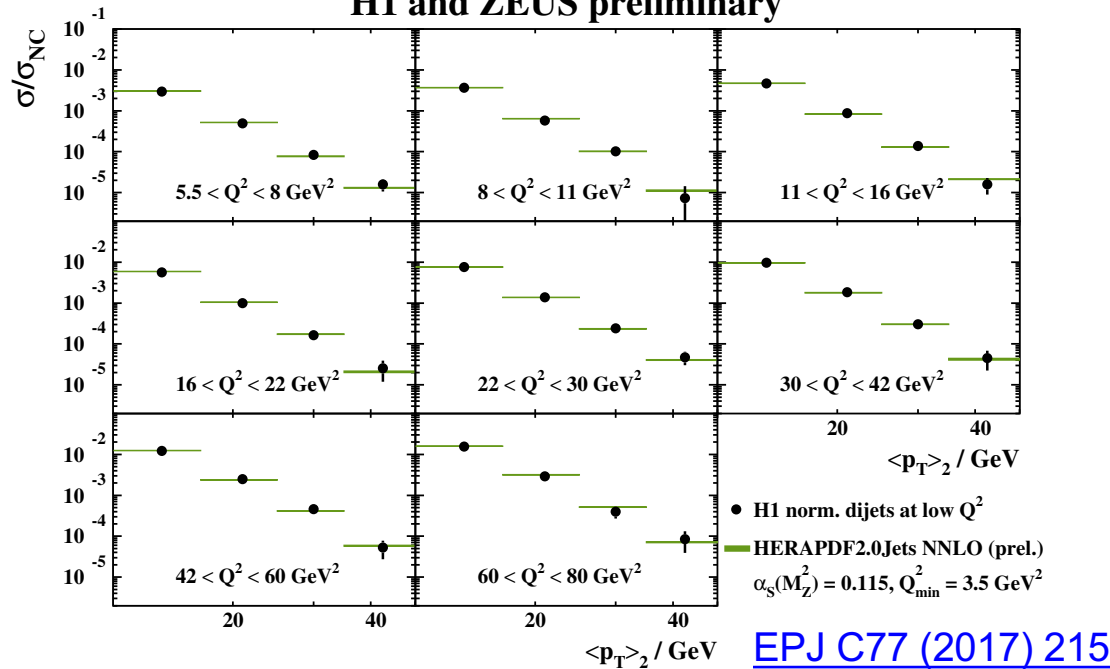


cf. HERA jet data

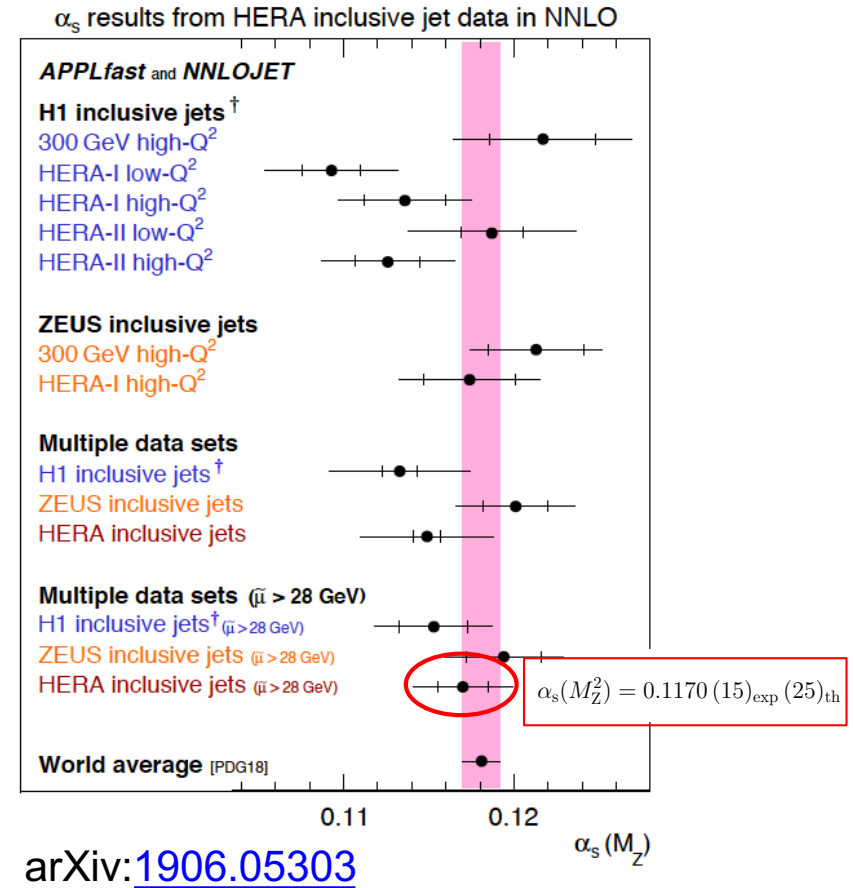
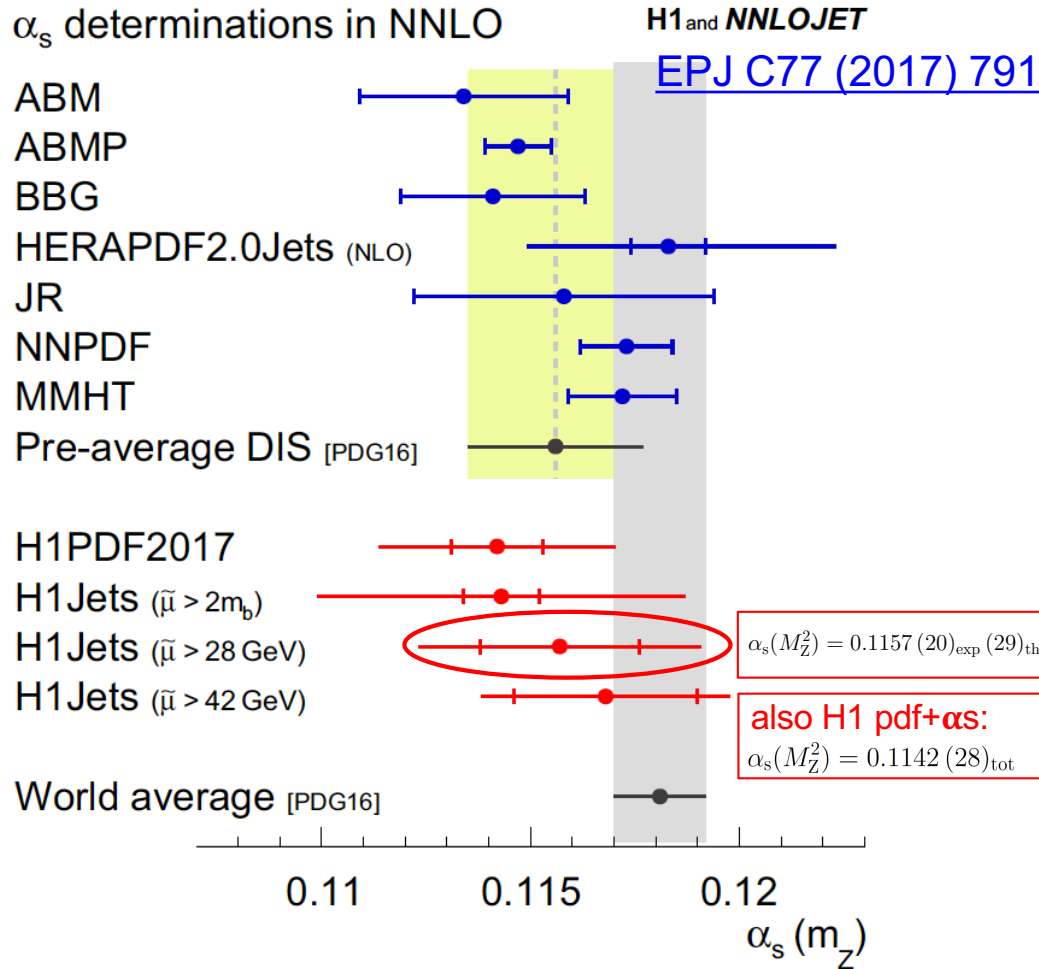
HERAPDF2.0JetsNLO

$\alpha_s(M_Z)=0.115$

H1 and ZEUS preliminary



cf. other NNLO determinations

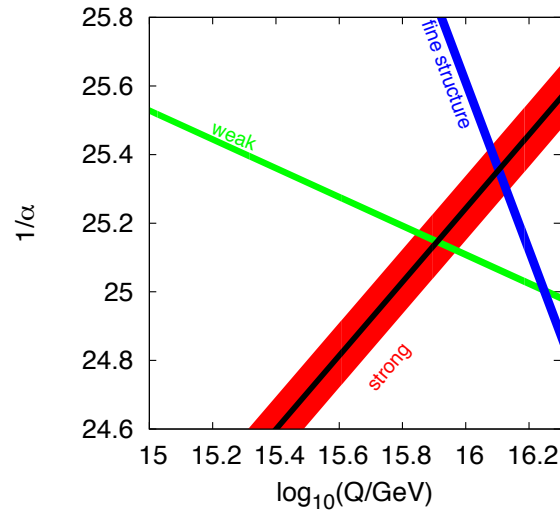


NNLO (this analysis): $\alpha_s(M_Z^2) = 0.1150(8)_{\text{exp}}(28)_{\text{th}}$

NNLOJet+APPLfast colls., **new result,**
HERA inclusive jets

see talk by K. Rabbertz, this conference

impact at LHC

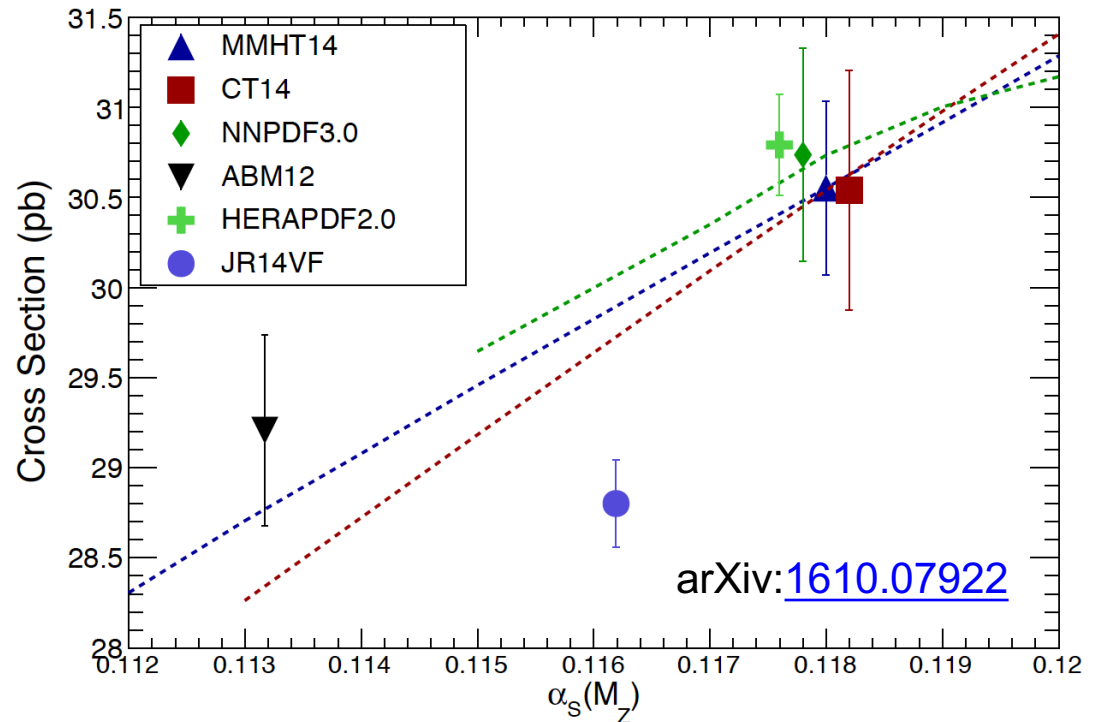


- α_s is least known coupling constant;
needed to constrain GUT scenarios;
cross section predictions, including Higgs; ...

PDG18: $\alpha_s = 0.1181 \pm 0.0011$

($\alpha_s = 0.1174 \pm 0.0016$; w/o lattice QCD)

Gluon-Fusion Higgs production, LHC 13 TeV



- what is true central value and uncertainty?
new precise determinations have important role to play

summary

HERAPDF2.0 family of PDFs completed by performing an NNLO fit including HERA DIS jet data

possible only due to recent **theoretical** and **grid technology** developments (NNLOJet, APPLfast; see talk by K.Rabbertz)

TWO new PDF sets:

HERAPDF2.0JetsNNLO $\alpha_s(M_Z)=0.118$ (the PDG value)

HERAPDF2.0JetsNNLO $\alpha_s(M_Z)=0.115$ (value favoured by our new fits)

the jet data allows us to constrain $\alpha_s(M_Z)$; NNLO value:

$$\alpha_s(M_Z^2) = 0.1150 \pm 0.0008 (\text{exp})_{-0.0005}^{+0.0002} (\text{model/par.}) \pm 0.0006 (\text{had}) \pm 0.0027 (\text{scale})$$

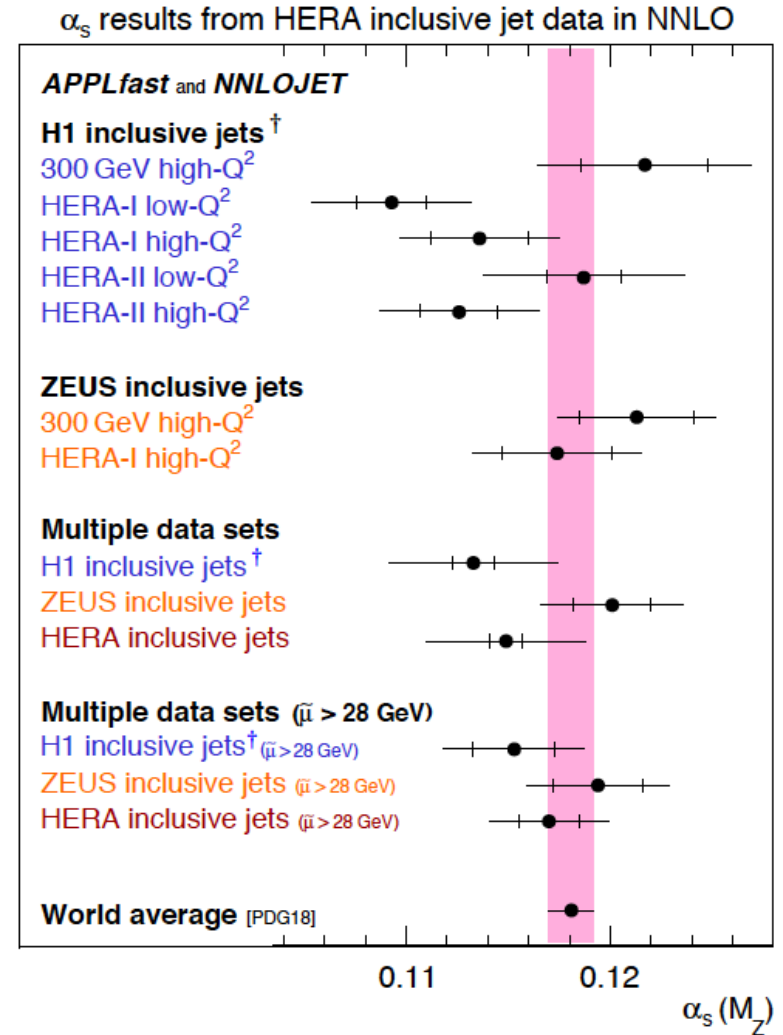
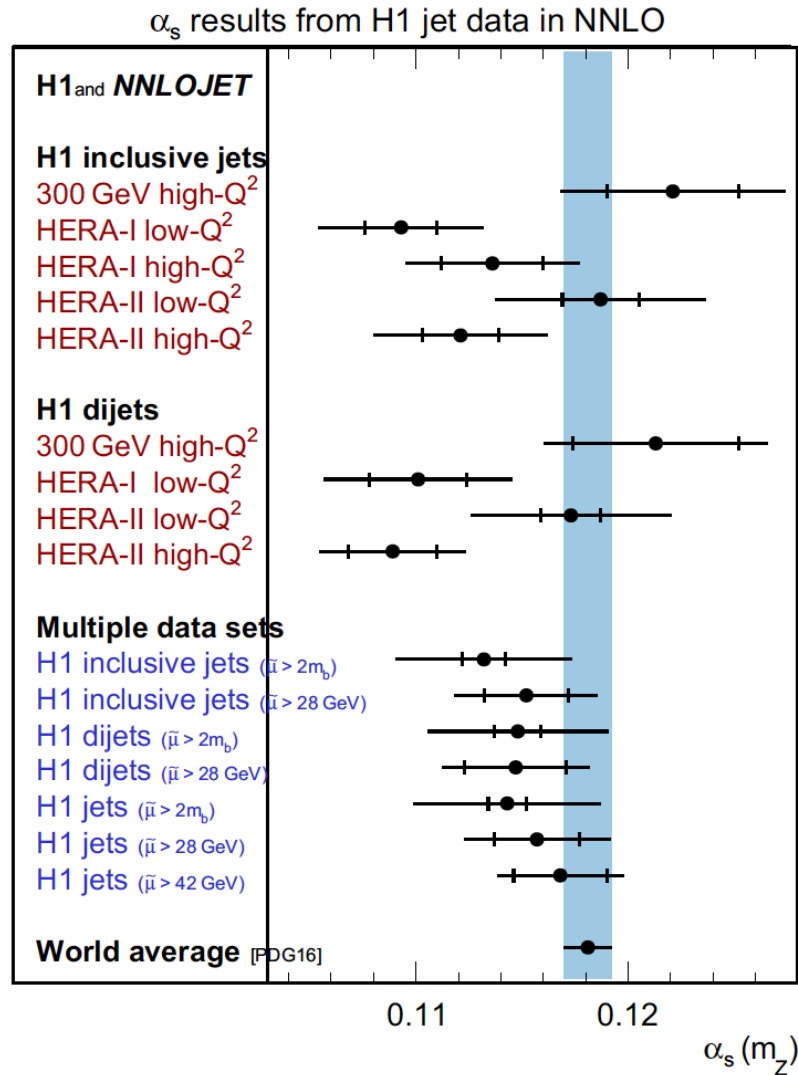
cf. NLO value:

$$\alpha_s(M_Z^2) = 0.1183 \pm 0.0009 (\text{exp}) \pm 0.0005 (\text{model/par.}) \pm 0.0012 (\text{had})_{-0.0030}^{+0.0037} (\text{scale})$$

systematic shift downwards at NNLO even taking scale change into account

extras

cf. other NNLO results using HERA jets



H1, NNLOJet, APPLfast colls., [EPJ C77 \(2017\) 791](#)

NNLOJET+APPLfast, arXiv:[1906.05303](#)